## CSC 404 - HOMEWORK 1 - NAME: Chris Ganzel

**Problem 1** (River crossing with a middle island!). On one bank of a river are **four** missionaries and **four** cannibals. There is one boat available that can hold **up to two** people and that they would like to use to cross the river. The river contains a middle island that can be used to assist the movement of missionaries and cannibals across the river. (Here we are allowed to cross from bank-to-bank without stopping at the middle island. If this were not allowed, we could not transport two cannibals across if a missionary were on the middle island.)

If the cannibals ever outnumber the missionaries on either of the river's banks, the missionaries will get eaten. How can the boat be used to safely carry all the missionaries and cannibals across the river?



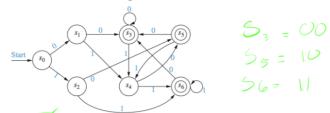
a. Solve the riddle by drawing a diagram indicating the movement of missionaries and cannibals. Record the number of movements used.

kf	st Shore	Right Shore
	0	<u> </u>
0	ч, <i>ч</i>	0,0
Α,	4,2	3 0,2
2	4,3 4	0,1
3	40	> 0,4
4	u,, е	0,3
5	١٫١	3,3
6	2,2	2,2
7	0,2	7 4/2
8	013	4,1
9	0,0	4,4

b. (Bonus) Solve the original riddle with the assumption that shore-to-shore travel is not allowed (i.e., you must stop at the middle island). Does this change the number of movements used?

- c. (Bonus) Solve the riddle with N=5 missionaries and N=5 cannibals (without and with shore-to-shore movement)
- d. (Bonus) Attempts at implementing a search algorithm (in a language of your choice) to construct a path from initial state to end state in the Missionaries and Cannibals (+ Middle Island) Riddle?

**Problem 2.** (Why do you hate 01?) Consider the following deterministic finite-state automaton (D.



a. Determine which of the following are accepted by the DFA. What state do they end at?

$$w_1 = 101010(42!)$$

$$w_2 = 000111$$

$$w_3 = 011100$$

101

$$w_4 = 10100111001(1337!)$$

54

b. Identify all bit-strings of length 3 that are accepted by the DFA.

	000
_	

001

c. Identify all bit-strings of length 4 that are accepted by the DFA.

000	00	0001	0010	0011	0100
100	00	1001	1010	1011	1100

0110 0111

1101 1110 1111

d. Identify all bit-strings of length 5 that are accepted by the DFA.

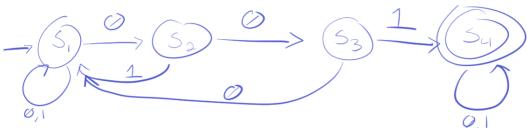
00000	00001	00010	00011	00100	00101	00110	00111
01000	01001	01010	01011	01100	01 01	01110	01111
10000	10001	10010	10011	10100	10101	10110	10111
11000	11001	11010	11011	11100	12101	11110	11111
					1		

e. (Bonus) Describe (in words) the set of bit-strings recognized by this DFA. (Hopefully you see a pattern in the mess that is this machine.)

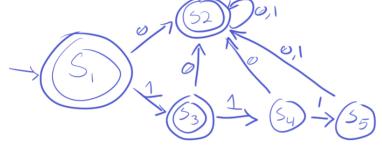
f. Blank space – add some sweet pictures – yay! Fun fact, binary numbers that end with 01 are congruent to 1 modulo 4.

**Problem 3.** (Yay designing DFAs - Enjoy!) For each of the following, construct a deterministic finite-state automaton (DFA) that recognizes the given set.

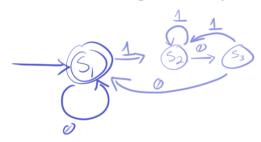
a. Set of all bit-strings that contain the substring 001. (Use at most 4 states)



b. Set of all bit-strings except 11 and 111 (Use at most 5 states)



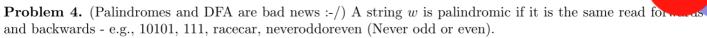
c. Set of all bit-strings where every 1 is followed by at least two 0s. (e.g., 0, 100, 01000, 1001000,...)



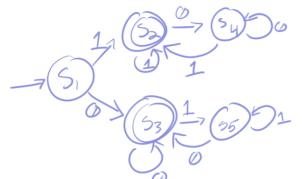
d. Set of all bit-strings that contain an even number of 0s and an even number of 1s. (Use 4 states)



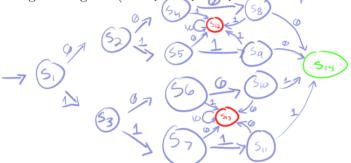
e. (Bonus) Set of bit-strings that contain an equal number of occurrences of the substrings 01 and 10. Note 101 is accepted because 101 contains a single 10 and a single 01, but 1010 is not because it contains two 10s and one 01.



- a. Construct a deterministic finite-state automaton with fixed input length  $\ell=3$  (all words/strings are of length
  - 3) that recognizes the palindromic bit-strings of length 3 (000,010,101,111). (Solve with 6 states or fewer.)



- 1/20 = 54 1/20 = 56 1/20 = 54 1/20 = 54 1/20 = 56
- b. Construct a deterministic finite-state automaton with fixed input length  $\ell=4$  that recognizes the palindromic bit-strings of length 4 (0000,0110,1001,1111).



- = Fail dump
- = sucess dump
- c. (Bonus) Construct a deterministic finite-state automaton with fixed input length  $\ell = 5$  that recognizes the palindromic bit-strings of length 5 (00000,00100,01010,10001,10001,10101,11111).

d. (Bonus) What issues emerge when you attempt to construct a DFA that recognizes all bit string palindromes? (This is one of the examples the prompts us to look at additional models of computation)

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We don't have any means of storing duta or referring to elements lariables

that have already been addressed in the string. this makes it difficult to tackle variable-length strings, since we have to planfor all possible cases.

also complicating things is a lack of any comparator method-, which reinforces the requirement that we anticipate all cases in advance, and prepure all

Problems the larger the string, the ferther back we must recall without any means of string, indexing saferring to data, we have to pepure a unique path for each new polindrome.