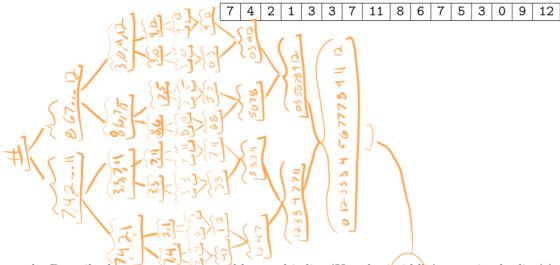
## CSC 404 - ACTIVITY/PROJECT 8 - NAME:

## Problem 1.

a. Describe how Mergesort would sort this list (i.e., draw the nice graph to show how things come together).



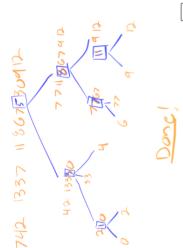
b. Describe how Quicksort would sort this list (Use the 'middle' entry in the list(s) as your pivot)

3 3 7 11 8 6 7 5 3 0 9 12

2

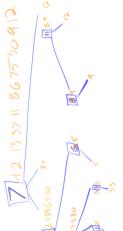
1

4



c. Describe how  $\mathtt{Quicksort}$  would sort this list (Use the first entry in the  $\mathrm{list}(s)$  as your pivot)

7 4 2 1 3 3 7 11 8 6 7 5 3 0 9 12



Apologies.

after zaming book out I realize

that the color choice was

not the best.

d. Implement Mergesort and Quicksort in a language of your choice (be adventurous/have fun). Then test the above lists (as well as some other fun lists).

**Problem 2** (Let's...find 4 - Weee!). Suppose someone picks a number x from a set of n numbers. A second person tries to guess the number by successively selecting subsets of the n numbers and asking the first person whether x is in each set. The first person answers either 'yes' or 'no'. We can find x using  $\log_2(n)$  queries ( $\lceil \log_2(n) \rceil$  if n is not a power of 2) by successively splitting the sets used in each query in half.

The following algorithm, findX, returns the mystery value x of an input list L.

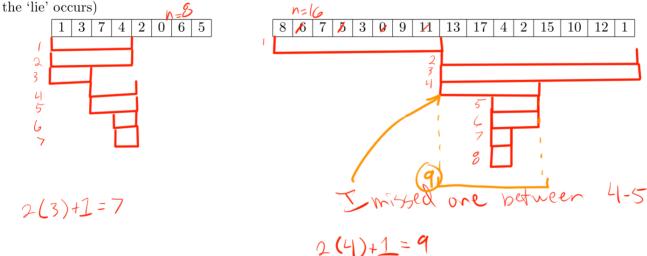
- 1. if len(L) < 2, then return L
- 2. else
  - a. L1 = first half of L
  - b. L2 = second half of L
  - c. If x in L1, then return findX(L1,x)
  - d. else return findX(L2,x)
- 3. return L
- a. Demonstrate this algorithm by finding the '4' in the following lists:



b. Implement this algorithm in a language of your choice and run it on the above lists (still looking for the mystery 4). I know, it is a really exciting function with the most exciting output - more about this in the next problem!

**Problem 3.** Ulam's problem ask for the number of queries required to find x, supposing that the first person is allowed to **lie** exactly once.

a. Option 1: [Ask each Question Twice!] Show that by asking each question twice, given a number x and a set with n elements, and asking one more question when we find the lie. Ulam's problem can be solved in at most  $2\log_2(n) + 1$  queries. Demonstrate this process by finding the 4 in the following lists (you may choose when



b. (Bonus) Option 2: [Divide-and-Conquer!] Show that by dividing the initial set of n elements into four parts, each with n/4 elements, 1/4 of the elements can be eliminated using two queries. [Hint: Use two queries, where each of the queries asks whether the element is in the union of two of the subsets with n/4 elements and where one of the subsets of n/4 elements is used in both queries.] Demonstrate this process by finding the 4 in the following lists (you may choose when the 'lie' occurs)

| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                             |                               |           |                       |                         |
|--------------------------------------------------------------------------------------------------|-------------------------------|-----------|-----------------------|-------------------------|
| -1+3+7+4+2+0+6+5+ +8+6+7+5+3+0+9+11+13+17+4+2+15+10+                                             | 1 0 - 1 0 0 0 -               |           | 0 0 0 11 10           | 4 -   4   0   4 -   4 0 |
| - 1 + 3 + 7 + 4 + 2 + 0 + 0 + 3 + + 6 + 0 + 7 + 3 + 3 + 0 + 9 + 11 + 13 + 17 + 4 + 2 + 13 + 10 + | 1   9   7   4   9   6   6   5 | 101617161 | . 9   0   0   11   19 | . 17   4   1)   15   10 |
|                                                                                                  | 1   3   7   4   2   0   0   3 | 10101131  |                       | 4                       |

c. (Bonus) Is the naive way to solve Ulam's problem by asking each question twice or the divide-and-conquer method more efficient?