# ENGR 463 Final Exam Project

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Part A: Variable Speed, Constant Load Test

Setup variables and dependencies as well as given data

```
[]: |#dependencies
     from pint import UnitRegistry
     import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     #unit setup
     ureg = UnitRegistry()
     m = ureg.meter
     g = ureg.gram
     kg = ureg.kilogram
     s = ureg.second
     min = ureg.minute
     hr = ureg.hour
     rpm = ureg.revolution / min
     turns = ureg.turn
     kPa = ureg.kilopascal
     W = ureg.watt
     N = ureg.newton
     K = ureg.kelvin
     #variable array setup
     speed = ureg.Quantity(np.array([1500, 2000, 2500, 3000, 3500, 4000]), rpm)
     torque = ureg.Quantity(np.array([1.8, 1.8, 1.8, 1.8, 1.8, 1.8]), N * m)
     Qdot_shaft = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W) #_
      \hookrightarrow Qdot\_shaft
     Qdot_in = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W) #_
      \hookrightarrowheat input
```

```
efficiency = np.array([None, None, None, None, None, None]) # n_th percent
MEP = ureg.Quantity(np.array([None, None, None, None, None, None]), kPa) # mean_
⇔effective pressure
bsfc = ureg.Quantity(np.array([None, None, None, None, None, None]), g / (W *__
 →hr)) # brake specific fuel consumption
Qdot_exhaust = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W)__
 →# exhaust heat
Qdot fins = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W) #1
 ⇔fins heat
mdot_air = ureg.Quantity(np.array([None, None, None, None, None, None]), kg/s)_u
 →# mass flow rate of air
mdot_fuel = ureg.Quantity(np.array([5.55E-05, 5.64E-05, 6.83E-05, 8.26E-05, 0.
→000104, 0.000118]), kg / s) # mass flow rate of fuel
deltaT = ureg.Quantity(np.array([247, 247, 247, 291, 330, 350]), K) #_J
⇒temperature difference
#qiven value
D = 10**-4 * m**3 # displacement of the engine: given 100cc
#constants
rho_air = 1.2 * ureg.kilogram / ureg.meter**3
Cp_air = 1.006 * ureg.kilojoule / (ureg.kilogram * ureg.kelvin)
LHV_gas = 45.2 * ureg.kilojoule / ureg.gram
```

#### Calculations

#### Table A

```
[]: # Create a dictionary with the column names and data
data = {
    'Speed (RPM)': speed.magnitude,
    'Torque (N * m)': torque.magnitude,
    'Power Shaft (W)': Qdot_shaft.magnitude,
```

```
'Power Input (W)': Qdot_in.magnitude,
         'Efficiency (%)': efficiency magnitude,
         'MEP (kPa)': MEP magnitude,
         'BSFC (g/(W*h))': bsfc.magnitude,
         'Exhaust Heat (W)': Qdot_exhaust.magnitude,
         'Fins Heat (W)': Qdot_fins.magnitude,
         'Air Mass Flow (kg/s)': mdot_air.magnitude,
         'Fuel Mass Flow (kg/s)': mdot_fuel.magnitude,
         'Delta T (delta_K)': deltaT.magnitude
     }
     # Create a DataFrame from the dictionary and add a caption
     df = pd.DataFrame(data)
     df
[]:
                     Torque (N * m) Power Shaft (W) Power Input (W)
        Speed (RPM)
               1500
                                 1.8
                                           282.743339
                                                                2508.60 \
               2000
     1
                                 1.8
                                           376.991118
                                                                2549.28
     2
               2500
                                 1.8
                                           471.238898
                                                                3087.16
     3
               3000
                                 1.8
                                           565.486678
                                                                3733.52
     4
               3500
                                 1.8
                                           659.734457
                                                                4700.80
     5
               4000
                                 1.8
                                           753.982237
                                                                5333.60
                                     BSFC (g/(W*h))
        Efficiency (%)
                         MEP (kPa)
                                                     Exhaust Heat (W)
     0
             11.270961 226.194671
                                           0.706648
                                                               372.723 \
     1
                                                               496.964
             14.788141
                        226.194671
                                           0.538580
     2
             15.264479
                        226.194671
                                           0.521774
                                                               621.205
     3
             15.146207
                        226.194671
                                           0.525848
                                                               878.238
     4
             14.034514
                        226.194671
                                           0.567501
                                                              1161.930
     5
             14.136460
                        226.194671
                                           0.563408
                                                              1408.400
        Fins Heat (W)
                       Air Mass Flow (kg/s) Fuel Mass Flow (kg/s)
     0
          1853.133661
                                      0.0015
                                                            0.000056
     1
          1675.324882
                                      0.0020
                                                            0.000056
     2
                                      0.0025
                                                            0.000068
          1994.716102
     3
          2289.795322
                                      0.0030
                                                            0.000083
     4
                                                            0.000104
          2879.135543
                                      0.0035
          3171.217763
                                      0.0040
                                                            0.000118
        Delta T (delta_K)
     0
                      247
                      247
     1
     2
                      247
     3
                      291
     4
                      330
     5
                      350
```

### Graphs

```
[]: # Plot Qdot_shaft, Qdot_in, Qdot_exhaust, Qdot_fins vs RPM
             plt.figure()
             plt.plot(df['Speed (RPM)'], df['Power Input (W)'], label="Input Power: Gasoline_
               ⇔(chemical)")
             plt.plot(df['Speed (RPM)'], df['Fins Heat (W)'], label="Output Power: Fins_
                plt.plot(df['Speed (RPM)'], df['Exhaust Heat (W)'], label="Output Power:
                ⇔Exhaust (heat)")
             plt.plot(df['Speed (RPM)'], df['Power Shaft (W)'], label="Output Power: Shaft_
               plt.xlabel('Speed (RPM)')
             plt.ylabel('Power (W)')
             plt.legend()
             plt.title('Engine Performance vs Speed (RPM)')
             plt.show()
             # Plot fuel flow rate vs rpm
             plt.figure()
             plt.plot(df['Speed (RPM)'], df['Fuel Mass Flow (kg/s)'])
             plt.xlabel('Speed (RPM)')
             plt.ylabel('Fuel Mass Flow (kg/s)')
             plt.title('Fuel Mass Flow vs Speed (RPM)')
             plt.show()
             # Plot Qdot_shaft, Qdot_in vs fuel flow rate
             plt.figure()
             plt.plot(df['Fuel Mass Flow (kg/s)'], df['Power Input (W)'], label="Power Input:

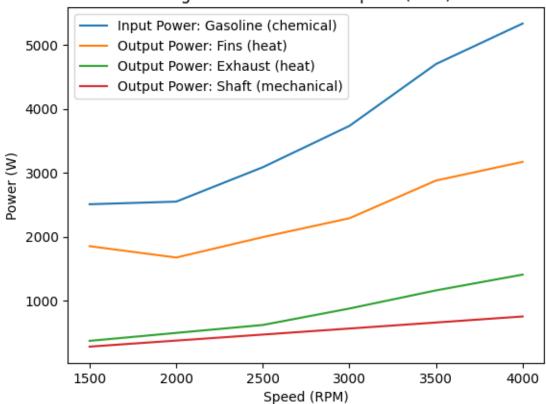
Gasoline (chemical)")

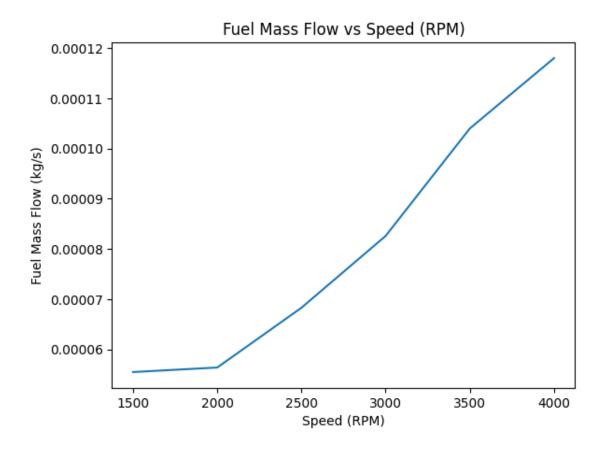
Gasoline (chemical)

             plt.plot(df['Fuel Mass Flow (kg/s)'], df['Power Shaft (W)'], label="Power_⊔

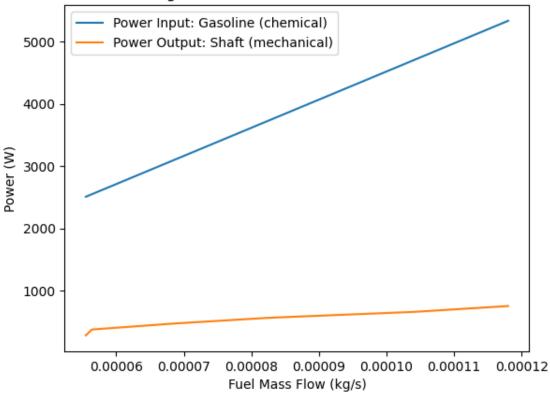
→Output: Shaft (mechanical)")
             plt.xlabel('Fuel Mass Flow (kg/s)')
             plt.ylabel('Power (W)')
             plt.legend()
             plt.title('Engine Performance vs Fuel Mass Flow')
             plt.show()
```

# Engine Performance vs Speed (RPM)





## Engine Performance vs Fuel Mass Flow



Part B: Constant Speed (1500 RPM), Variable Load Test

## Setup variables and dependencies as well as given data

```
[]: #variable array setup
     percent_load = np.array([0.75, 1, 1.25, 1.5, 1.75, 2]) # percent
     speed = ureg.Quantity(np.array([1500, 1500, 1500, 1500, 1500, 1500]), rpm) # rpm
     torque = ureg.Quantity(np.array([1.35, 1.8, None, None, None, None]), N * m) #__
      \hookrightarrowtorque
     Qdot_shaft = ureg.Quantity(np.array([None, None, None, None, None, None]), W) #__
      \hookrightarrow Qdot\_shaft
     Qdot_in = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W) #__
      ⇔heat input
     efficiency = np.array([None, None, None, None, None]) # n_th percent
     MEP = ureg.Quantity(np.array([169.64, 226.19, None, None, None, None]), kPa) #__
      →mean effective pressure
     bsfc = ureg.Quantity(np.array([None, None, None, None, None, None]), g / (W *_U
      →hr)) # brake specific fuel consumption
     Qdot_exhaust = ureg.Quantity(np.array([None, None, None, None, None, None, None]), W)__
      →# exhaust heat
```

```
Qdot_fins = ureg.Quantity(np.array([None, None, None, None, None, None]), W) #___
fins heat

mdot_air = ureg.Quantity(np.array([None, None, None, None, None, None]), kg/s)___
# mass flow rate of air

mdot_fuel = ureg.Quantity(np.array([4.931E-05, 5.547E-05, 8.452E-05, 8.452E-05,]
$\times 9.342E-05, 0.000118]$), kg / s) # mass flow rate of fuel

deltaT = ureg.Quantity(np.array([235, 247, 250, 288, 314, 345]), K) #___
$\times temperature difference$
```

## Calculations

```
[]: # Calculate slope of load-torque line
     slope = (torque[1].magnitude - torque[0].magnitude) / (percent_load[1] -__
      →percent load[0])
     # Calculate torque for remaining percent loads
     for i in range(2, len(percent_load)):
         torque[i] = (slope * (percent_load[i] - percent_load[1]) + torque[1].
      ⇒magnitude) * N * m
     mdot_air = (rho_air * D * speed) / (2*turns) # The 2 is present in the
      -denominator because engine will only draw air every second revolution
     mdot_air = mdot_air.to(kg / s)
     Qdot_exhaust = mdot_air * Cp_air * deltaT
     Qdot_exhaust = Qdot_exhaust.to(W)
     Qdot_in = mdot_fuel * LHV_gas
     Qdot_in = Qdot_in.to(W)
     Qdot_shaft = speed*torque
     Qdot shaft = Qdot shaft.to(W)
     Qdot fins = Qdot in - Qdot exhaust - Qdot shaft
     efficiency = (Qdot_shaft / Qdot_in)*100 # n_th percent
     bsfc = mdot_fuel / Qdot_shaft
     bsfc = bsfc.to(g / (W * hr))
     MEP = (4 * np.pi * torque) / D
     MEP = MEP.to(kPa)
```

#### Table B

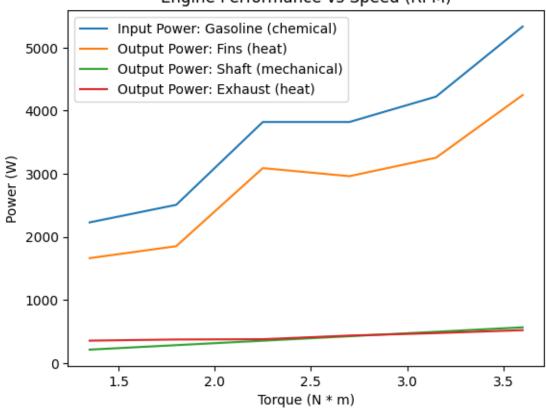
```
'Exhaust Heat (W)': Qdot_exhaust.magnitude,
         'Fins Heat (W)': Qdot_fins.magnitude,
         'Air Mass Flow (kg/s)': mdot_air.magnitude,
         'Fuel Mass Flow (kg/s)': mdot_fuel.magnitude,
         'Delta T (delta_K)': deltaT.magnitude
     }
     # Create a DataFrame from the dictionary and add a caption
     df = pd.DataFrame(data)
[]:
        Percent Load (%)
                           Speed (RPM) Torque (N * m) Power Shaft (W)
                    0.75
                                                 1.35
                                  1500
                                                            212.057504
     1
                    1.00
                                  1500
                                                  1.8
                                                            282.743339
     2
                                                 2.25
                    1.25
                                  1500
                                                            353.429174
     3
                    1.50
                                                  2.7
                                  1500
                                                            424.115008
     4
                    1.75
                                  1500
                                                 3.15
                                                            494.800843
     5
                    2.00
                                                  3.6
                                                            565.486678
                                  1500
        Power Input (W) Efficiency (%)
                                          MEP (kPa) BSFC (g/(W*h))
               2228.812
                               9.514374
     0
                                         169.646003
                                                           0.837113
     1
               2507.244
                              11.277057
                                         226.194671
                                                           0.706266
     2
               3820.304
                              9.251336 282.743339
                                                           0.860914
     3
               3820.304
                              11.101604
                                         339.292007
                                                           0.717428
     4
               4222.584
                              11.717963 395.840674
                                                           0.679692
     5
               5333.600
                              10.602345 452.389342
                                                           0.751211
        Exhaust Heat (W) Fins Heat (W) Air Mass Flow (kg/s)
     0
                 354.615
                           1662.139496
                                                        0.0015
     1
                 372.723
                           1851.777661
                                                        0.0015
                           3089.624826
     2
                 377.250
                                                        0.0015
     3
                 434.592
                           2961.596992
                                                        0.0015
     4
                 473.826
                           3253.957157
                                                       0.0015
     5
                 520.605
                           4247.508322
                                                       0.0015
        Fuel Mass Flow (kg/s) Delta T (delta K)
     0
                     0.000049
                                              235
     1
                     0.000055
                                              247
     2
                                              250
                     0.000085
     3
                     0.000085
                                              288
     4
                     0.000093
                                              314
     5
                     0.000118
                                              345
```

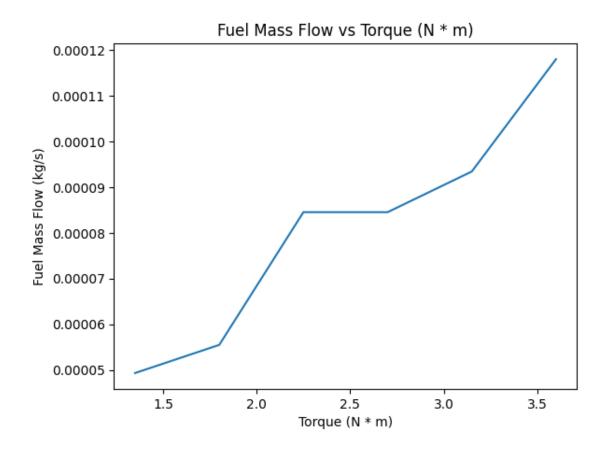
#### Graphs

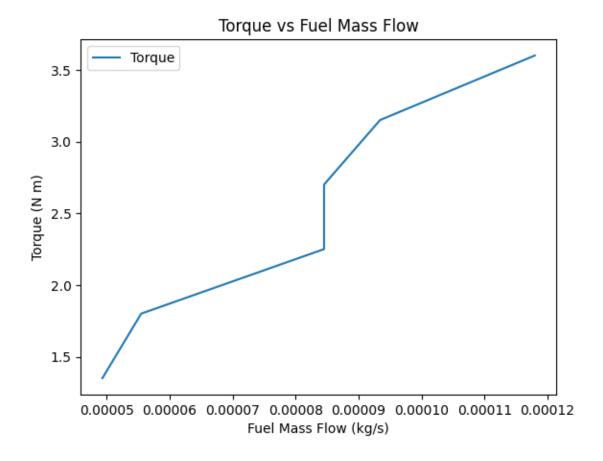
```
[]: # Plot Qdot_shaft, Qdot_in, Qdot_exhaust, Qdot_fins vs Torque plt.figure()
```

```
plt.plot(df['Torque (N * m)'], df['Power Input (W)'], label="Input Power:
 Gasoline (chemical)")
plt.plot(df['Torque (N * m)'], df['Fins Heat (W)'], label="Output Power: Fins⊔
 plt.plot(df['Torque (N * m)'], df['Power Shaft (W)'], label="Output Power:
 ⇔Shaft (mechanical)")
plt.plot(df['Torque (N * m)'], df['Exhaust Heat (W)'], label="Output Power:
 ⇔Exhaust (heat)")
plt.xlabel('Torque (N * m)')
plt.ylabel('Power (W)')
plt.legend()
plt.title('Engine Performance vs Speed (RPM)')
plt.show()
# Plot fuel flow rate vs rpm
plt.figure()
plt.plot(df['Torque (N * m)'], df['Fuel Mass Flow (kg/s)'])
plt.xlabel('Torque (N * m)')
plt.ylabel('Fuel Mass Flow (kg/s)')
plt.title('Fuel Mass Flow vs Torque (N * m)')
plt.show()
# Plot Qdot_shaft, Qdot_in vs fuel flow rate
plt.figure()
plt.plot(df['Fuel Mass Flow (kg/s)'], df['Torque (N * m)'], label="Torque")
plt.xlabel('Fuel Mass Flow (kg/s)')
plt.ylabel('Torque (N m)')
plt.legend()
plt.title('Torque vs Fuel Mass Flow')
plt.show()
```









#### **Conclusion Questions**

1) Comment on the efficiency of engine for both loading cases (Table A vs. Table B). How could we improve the efficiency of the engine? Do these results make sense?

Efficiency is higher for higher RPM's and lower loads. This makes sense because the engine is running faster and therefore has more power to spare. We could improve the efficiency of the engine by increasing the compression ratio, which would increase the power output of the engine. These results make sense because the engine is more efficient at higher RPM's and lower loads. 2) What are some of the things we would need to be conscious of in our experiment to obtain reliable results?

We would have to be conscious that the engine is warmed up before we start the experiment. We would also have to be aware of how the engine is performing, making sure that it does not overheat and cause errant results. Engine should not run too lean or too rich. We would want to make sure the oil and gas is fresh to make sure we don't lose more efficiency then we would expect. It is also imperative that there are no leaks in the system.

3) Why may it be important to allow an engine to warm up before placing it under test (in terms of reliable results)?

Engines are more efficient when they are warm. This is because the oil is more viscous when it is

cold, and therefore causes more friction. More friction will decrease efficiency.