# Supplement to Physical Activity Classification with Dynamic, Discriminative Methods

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#### 1 Introduction

In this supplement we present additional results showing the performance of each method in the simulation study and in the applications as measured by the macro  $F_1$  score, as well as a description of the mixed effects models used to estimate mean performance for each model and assess whether the differences in model performance were statistically significant.

### 2 Conditional Random Field Estimation Algorithm

A detailed description of the estimation algorithm used for the **CRF** is in Algorithm 1.

### 3 Simulation Study

In the main manuscript, we summarized results for the simulation study using the proportion of windows that were classified correctly. Here we display summaries of the macro  $F_1$  scores achieved by each method. The macro  $F_1$  score is defined as

$$F_1 = 2 \frac{\text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}, \text{ where}$$

$$\text{Precision} = \frac{1}{S} \sum_{s=1}^{S} \frac{\text{TP}_s}{\text{TP}_s + \text{FP}_s} \text{ and}$$

Algorithm 1. CRF Estimation Algorithm

 $Method: estimate\_CRF$ 

Inputs: Labeled data  $\{(\mathbf{y}_i, \mathbf{x}_i), i = 1, \dots, N\}$ 

Outputs: CRF parameter estimates.

- 1. Initialize all parameter estimates  $\widehat{\boldsymbol{\zeta}}$ ,  $\widehat{\boldsymbol{\omega}}$ , and  $\widehat{\boldsymbol{\beta}}$  to  $\underline{\boldsymbol{\varrho}}$ .
- 2. For  $b = 1, ..., M_{bag}$ , repeat the following:
  - (a) Draw a sample of N observation sequences with replacement from the set of all observation sequences. Collect the sampled sequences in  $\mathcal{B}^b$  and the unsampled sequences in  $\mathcal{O}^b$ .
  - (b) Call **boost**\_ $CRF(\mathcal{B}^b, \mathcal{O}^b)$ ; the return value is the vector  $(\widehat{\boldsymbol{\zeta}}^b, \widehat{\boldsymbol{\omega}}^b, \widehat{\boldsymbol{\beta}}^b)$ .

(c) Set 
$$\widehat{\zeta} = \widehat{\zeta} + \frac{1}{M_{bag}} \widehat{\zeta}^b$$
,  $\widehat{\omega} = \widehat{\omega} + \frac{1}{M_{bag}} \widehat{\omega}^b$ , and  $\widehat{\beta} = \widehat{\beta} + \frac{1}{M_{bag}} \widehat{\beta}^b$ .

3. Return the combined parameter estimates  $(\widehat{\boldsymbol{\zeta}}, \widehat{\boldsymbol{\omega}}, \widehat{\boldsymbol{\beta}})$ .

Method: boost\_CRF

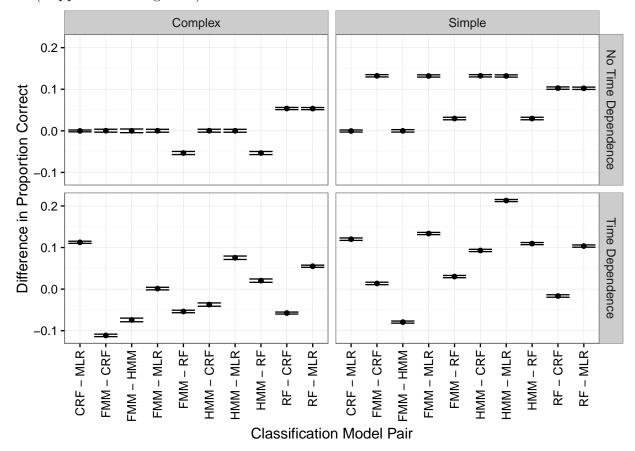
**Inputs:** Labeled data  $\{(\mathbf{y}_i, \mathbf{x}_i), i = 1, \dots, N_{train}\}$  and  $\{(\mathbf{y}_i, \mathbf{x}_i), i = 1, \dots, N_{validation}\}$ . **Outputs:** CRF parameter estimates.

- 1. Initialize m=0, validation\_score $[0]=-\infty$ ,  $\widehat{\beta}=\underline{0}$ ,  $\widehat{\zeta}_s=\log(\frac{n_s}{n_S})$  and  $\widehat{\omega}_{r,s}=\log(\frac{n_{r,s}}{n_{S,S}})$  for all  $r,s=1,\ldots,S$ . Here,  $n_s$  is the number of occurrences of state s and  $n_{r,s}$  is the number of transitions from state r to state s in the training data set.
- 2. Repeat the following until the first occurrence of the largest element of validation\_score is not within the last M\_search\_threshold values stored in validation\_score:
  - $\begin{array}{llll} (a) \ Set & m & = & m + 1, & \mathtt{attempt\_num} & = & 0, & and & \mathtt{validation\_score}[m] & = & \mathtt{validation\_score}[m-1]. \end{array}$
  - (b) Repeat the following until validation\_score[m] > validation\_score[m-1] or attempt\_num = max\_attempts:
    - i. Set attempt\_num = attempt\_num + 1,  $\tilde{\omega} = \hat{\omega}$  and  $\tilde{\beta} = \hat{\beta}$ .
    - ii. Randomly select the set  $A^m \subset \{1, \ldots, D\}$  of active features for the mth update. The number of active features is a user specified parameter.
    - iii. Using a numerical optimization routine, update  $\tilde{\omega}$  and  $\tilde{\beta}$  to the constrained local maximum likelihood estimates based on the training data, holding the parameter estimates for elements of  $\tilde{\beta}$  not in the active feature set fixed.
    - iv. Using the estimates from step 2(b)iii, predict the values of  $\mathbf{y}_i$  for the validation data set. If the proportion of time points at which the prediction was correct is greater than  $validation\_score[m]$ , store it in  $validation\_score[m]$  and  $set \widehat{\boldsymbol{\omega}} = \widetilde{\boldsymbol{\omega}}$  and  $\widehat{\boldsymbol{\beta}} = \widetilde{\boldsymbol{\beta}}$ .
- 3. Return  $(\widehat{\boldsymbol{\zeta}}, \widehat{\boldsymbol{\omega}}, \widehat{\boldsymbol{\beta}})$ .

Recall = 
$$\frac{1}{S} \sum_{s=1}^{S} \frac{\text{TP}_s}{\text{TP}_s + \text{FN}_s}$$

Here,  $TP_s$ ,  $FP_s$ , and  $FN_s$  are respectively the true positive rate, false positive rate, and false negative rate for class i. This score is a useful complement to the overall proportion correct because it incorporates both precision and recall and gives equal weight weight to all classes, whereas the proportion correct gives more weight to more prevalent classes [Sokolova and Lapalme, 2009].

For the simulation study, the relative performance of the methods as measured by the macro  $F_1$  score was the same as it was when the methods were evaluated using the proportion correct (Supplemental Figure 2).



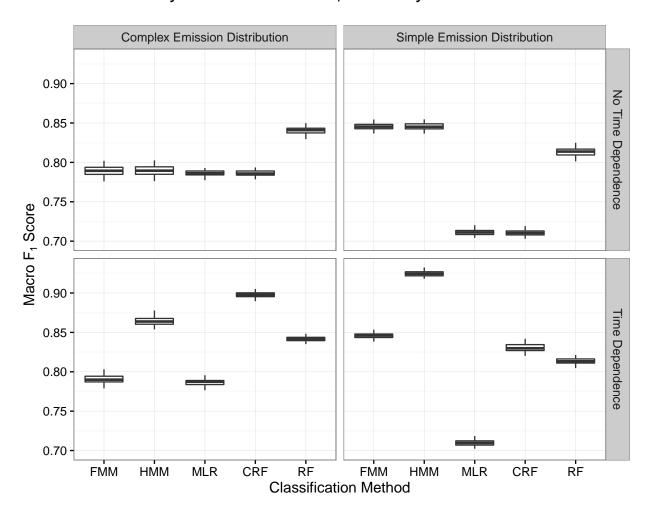
Estimates of pairwise differences in the mean proportion of time points classified correctly for each pair of models, separately for each combination of complexity level of the feature emission distributions and presence or absence of temporal dependence in the data generating process. The confidence intervals are from a linear mixed effects model and have a familywise confidence level of 95%.

## 4 Applications

Tables 1 and 2 list the accelerometer features used for the data from Mannini et al. [2013] and Sasaki et al. [2016] respectively. The prevalence of different levels of activity type and intensity for each dataset are in 3.

Supplemental Figure 1: Box plots showing the proportion of time points classified correctly in the simulation study. A separate box plot is displayed for each combination of the complexity level of the feature emission distributions and the classification method. Each point corresponds to a combination of distribution complexity, classification method, and simulation index.

#### Simulation Study Results: Macro F<sub>1</sub> Score by Classification Method



Supplemental Figure 2: Box plots showing the macro  $F_1$  score combining precision and recall across all three classes in the simulation study. A separate box plot is displayed for each combination of the complexity level of the feature emission distributions, the Bayes error rate, and the classification method. Each point corresponds to a combination of distribution complexity, Bayes error rate, classification method, and simulation index.

Domain	Feature						
Time	Mean						
	Standard deviation						
_	Minimum and maximum						
Frequency	Frequency and power of the first dominant frequency between $0.3~\mathrm{Hz}$ and $15~\mathrm{Hz}$						
	Frequency and power of the second dominant frequency between 0.3 Hz and 15 Hz						
	Total power between 0.3 Hz and 15 Hz						
	Ratio of the power of the first dominant frequency between 0.3 Hz and 15 Hz and the total power between 0.3 Hz and 15 Hz						
	Frequency and power of the first dominant frequency between $0.3~\mathrm{Hz}$ and $3~\mathrm{Hz}$						
	Ratio of the frequency of the first dominant frequency between 0.3 Hz and 15 Hz in the current window and in the previous window						

Table 1: Features extracted from the accelerometer signal in preprocessing the data from Mannini et al. [2013]. All features are computed using the acceleration vector magnitude.

Domain	Feature	X	Y	Z	VM	$\theta$	$\phi$
Time	Mean	Y	Y	Y	Y	Y	Y
-	The 10th, 25th, 50th, 75th, and 90th percentiles					Y	Y
-	Lag 1 autocorrelation	Y	Y	Y	Y	N	N
-	Entropy: We place the observed VM values into 10	N	N	N	Y	N	N
	bins of equal size and calculate the proportion falling						
	into each bin, $p_1, \ldots, p_{10}$ . The estimated entropy is						
	then $-\frac{1}{10} \sum_{i=1}^{10} p_i log(p_i)$						
Frequency	Frequency and power of the first dominant frequency	Y	Y	Y	Y	N	N
	Frequency and power of the second dominant	Y	Y	Y	Y	N	N
	frequency						
	Total power: The sum of the estimated power for all	Y	Y	Y	Y	N	N
	frequencies.						
	Frequency and power of the first dominant frequency	Y	Y	Y	Y	N	N
	in the band from $0.3$ to $3~\mathrm{Hz}$						
	Ratio of power of first dominant frequency in the band	Y	Y	Y	Y	N	N
	from 0.3 to 3Hz to power of first dominant frequency						
	overall						
	Entropy of the spectral density: After normalizing the	Y	Y	Y	Y	N	N
	estimated powers so that they sum to 1, we apply the						
	entropy calculation above.						

Table 2: Features extracted from the accelerometer signal in preprocessing the data from Sasaki et al. [2016]. The right-hand 6 columns indicate whether the listed feature was computed for each of the three axes on which acceleration was measured, vector magnitude, polar angle, and azimuthal angle.

Response	Data Set	Activity Class and Prevalence						
Intensity		Sedentary	Light	Moderate	Vigorous	Transition		
	Mannini Lab, Ankle	35.2%	4.8%	55.5%	4.5%	-		
	Mannini Lab, Wrist	35.5%	4.8%	55.3%	4.4%	-		
	Sasaki Lab	18.4%	44.2%	35.7%	0%	1.7~%		
	Sasaki Free Living	24.7%	41.5%	23.6%	0.8%	9.4%		
Type		Sedentary	Ambulation	Cycling	Other			
	Mannini Lab, Ankle Mannini	39.9%	33.2%	13.8%	13.1%			
	Lab, Wrist	40.3%	32.9%	14.0%	12.9%			
Type		Sedentary/ Standing	Moving Intermittently	Locomotion	Transition			
	Sasaki Lab	17.2%	53.7%	27.4%	1.7%			
	Sasaki Free Living	45.5%	26.4%	18.9%	9.3%			

Table 3: Prevalence of activity intensity and type labels in the data from Mannini et al. [2013] and Sasaki et al. [2016]. In the data from Mannini et al. [2013], prevalence varies slightly across accelerometer locations since different time windows were dropped in the cleaning process they used to handle missing data due to wireless transmission problems with the accelerometers.

Response	Location	Data Set	CRF	HMM	MLR	FMM	RF
Intensity	Ankle	Mannini	0.480	0.574	0.468	0.579	0.555
Intensity	Ankle	Sasaki Free Living	0.538	0.522	0.526	0.505	0.483
Intensity	Ankle	Sasaki Lab	0.789	0.737	0.680	0.654	0.675
Intensity	Wrist	Mannini	0.611	0.690	0.496	0.630	0.608
Intensity	Wrist	Sasaki Free Living	0.419	0.451	0.413	0.421	0.417
Intensity	Wrist	Sasaki Lab	0.696	0.703	0.599	0.577	0.604
Type	Ankle	Mannini	0.978	0.978	0.921	0.916	0.941
Type	Ankle	Sasaki Free Living	0.590	0.547	0.523	0.516	0.541
Type	Ankle	Sasaki Lab	0.938	0.882	0.783	0.762	0.808
Type	Wrist	Mannini	0.872	0.867	0.737	0.786	0.829
Type	Wrist	Sasaki Free Living	0.424	0.459	0.424	0.434	0.485
Type	Wrist	Sasaki Lab	0.949	0.839	0.723	0.674	0.727

Table 4: Estimated mean macro  $F_1$  score for the activity type and intensity classification tasks in data from Mannini et al. [2013] and Sasaki et al. [2016] by response variable, accelerometer location and data set.

Here we present the classification results in the applications, as summarized by the macro  $F_1$  score (Supplemental Figure 3). With the  $F_1$  score, the differences in performance between the dynamic models and the corresponding static models are statistically significant at the  $\alpha=0.05$  level. The differences in mean  $F_1$  score between the generative and discriminative models are not statistically significant or consistent in direction across classification of activity type or intensity. This is different from the measure of proportion correct discussed in the main manuscript, where discriminative models generally outperformed their static counterparts by a statistically significant margin. These results are consistent with Supplemental Table 4, where we present the mean  $F_1$  score separately for each combination of response, location, and data set. Across all of these combinations, the dynamic models tended to achieve higher  $F_1$  scores than the static models, and the **CRF** had the most consistent performance as measured by the  $F_1$  score.

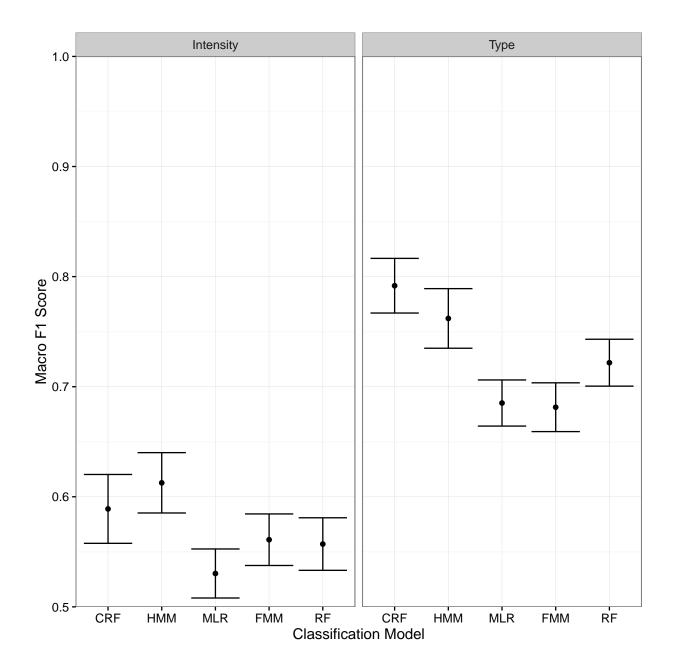
The confidence intervals displayed in Figure 4 of the main manuscript and Supplemental Figure 3, as well as the hypothesis test results discussed throughout the text, were obtained using linear mixed effects models with the following specification:

$$y_{r,l,d,c,s} = \mu_{r,l,d,c} + \alpha_{d|s} + \varepsilon_{r,l,d,c,s}$$

$$\alpha_{d|s} \sim N(0, \sigma_s^2)$$

$$\varepsilon_{r,l,d,c,s} \sim N(0, \xi_{r,l,d,c}^2)$$

In this notation  $y_{r,l,d,c,s}$  is a measure of classifier quality (either proportion correct or macro  $F_1$  score) for one instance, indexed by r denoting the response (activity type or activity



Supplemental Figure 3: Results from activity type and intensity classification tasks in data from Mannini et al. [2013] and Sasaki et al. [2016], averaged across the three data sets and two accelerometer locations. The joint confidence intervals are from a linear mixed effects model and have a familywise confidence level of 95%.

intensity), l denoting the accelerometer location (ankle or wrist), d denoting the data set (Mannini, Sasaki Free Living, or Sasaki Lab), c denoting the classifier (**CRF**, **HMM**, **MLR**, **FMM**, **RF**), and s denoting the subject within each study. The  $\alpha_{d|s}$  term is a random effect for each subject; the notation d|s emphasizes that we treat the subjects in different data sets separately for the purpose of this model, even though the subjects in the Sasaki Free Living data set also participated in the Sasaki Lab data collection. The error term,  $\varepsilon_{r,l,d,c,s}$ , has a separate variance for each combination of response, location, data set, and classifier. We fit a separate model for each measure of classifier quality using the nlme package [Pinheiro et al., 2017] in R [R Core Team, 2016]. For each measure of classifier quality, we conducted all hypothesis tests simultaneously with construction of the confidence intervals in Figure 3 of the manuscript and Supplemental Figure 3 in this document using the multcomp package [Hothorn et al., 2008] for R.

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