Package 'quantmod'

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```
coef.quantile_genlasso
```

Coef function for quantile_genlasso object

Description

Retrieve coefficients for estimating the conditional quantiles, using the generalized lasso coefficients at particular tau or lambda values.

Usage

```
## S3 method for class 'quantile_genlasso'
coef(obj, s = NULL)
```

Arguments

obi

The quantile_genlasso object.

s

Vector of integers specifying the tau and lambda values to consider for predictions; for each i in this vector, a prediction is made at quantile level tau[i] and tuning parameter value lambda[i], according to the tau and lambda vectors stored in the given quantile_genlasso object obj. (Said differently, s specifies the columns of obj\$beta to use for the predictions.) Default is NULL, which means that all tau and lambda values will be considered.

cv_quantile_genlasso Cross-validation for quantile generalized lasso

Description

Run cross-validation for the quantile generalized lasso on a tau by lambda grid. For each tau, the lambda value minimizing the cross-validation error is reported.

```
cv_quantile_genlasso(x, y, d, tau, lambda = NULL, nlambda = 30,
  lambda_min_ratio = 0.001, weights = NULL, no_pen_rows = c(),
  nfolds = 5, train_test_inds = NULL, intercept = TRUE,
  standardize = TRUE, lp_solver = c("gurobi", "glpk"),
  time_limit = NULL, warm_starts = TRUE, params = list(),
  transform = NULL, inv_trans = NULL, jitter = NULL,
  verbose = FALSE, sort = FALSE, iso = FALSE, nonneg = FALSE,
  round = FALSE)
```

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Arguments

```
nfolds Number of cross-validation folds. Default is 5. train_test_inds
```

List of length two, with components named train and test. Each of train and test are themselves lists, of the same length; for each i, we will consider train[[i]] the indices (which index the rows of x and elements of y) to use for training, and test[[i]] as the indices to use for testing (validation). The validation error will then be summed up over all i. This allows for fine control of the "cross-validation" process (in quotes, because there need not be any crossing going on here). Default is NULL; if specified, takes priority over nfolds.

Details

All arguments through verbose (except for nfolds and train_test_inds) are as in quantile_genlasso_grid and quantile_genlasso. Past verbose, the arguments are as in predict.quantile_genlasso, and control what happens with the predictions made on the validation sets.

Value

A list with the following components:

- qgl_obj: a quantile_genlasso object obtained by fitting on the full training set, at all quantile levels and their corresponding optimal lambda values
- cv_mat: a matrix of cross-validation errors (as measured by quantile loss), of dimension (number of tuning parameter values) x (number of quantile levels)
- lambda_min: a vector of optimum lambda values, one per quantile level
- tau, lambda: the sequences of tau and lambda values considered

cv_quantile_lasso

Cross-validation for quantile lasso

Description

Run cross-validation for the quantile lasso on a tau by lambda grid. For each tau, the lambda value minimizing the cross-validation error is reported.

```
cv_quantile_lasso(x, y, tau, lambda = NULL, nlambda = 30,
  lambda_min_ratio = 0.001, weights = NULL, no_pen_vars = c(),
  nfolds = 5, train_test_inds = NULL, intercept = TRUE,
  standardize = TRUE, lp_solver = c("gurobi", "glpk"),
  time_limit = NULL, warm_starts = TRUE, params = list(),
  transform = NULL, inv_trans = NULL, jitter = NULL,
  verbose = FALSE, sort = FALSE, iso = FALSE, nonneg = FALSE,
  round = FALSE)
```

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Arguments

nfolds Number of cross-validation folds. Default is 5. train_test_inds

List of length two, with components named train and test. Each of train and test are themselves lists, of the same length; for each i, we will consider train[[i]] the indices (which index the rows of x and elements of y) to use for training, and test[[i]] as the indices to use for testing (validation). The validation error will then be summed up over all i. This allows for fine control of the "cross-validation" process (in quotes, because there need not be any crossing going on here). Default is NULL; if specified, takes priority over nfolds.

Details

All arguments through verbose (except for nfolds and train_test_inds) are as in quantile_lasso_grid and quantile_lasso. Past verbose, the arguments are as in predict.quantile_lasso, and control what happens with the predictions made on the validation sets.

Value

A list with the following components:

- qgl_obj: a quantile_genlasso object obtained by fitting on the full training set, at all quantile levels and their corresponding optimal lambda values
- cv_mat: a matrix of cross-validation errors (as measured by quantile loss), of dimension (number of tuning parameter values) x (number of quantile levels)
- lambda_min: a vector of optimum lambda values, one per quantile level

get_diff_mat

Difference matrix

Description

Construct a difference operator, of a given order, for use in trend filtering penalties.

Usage

```
get_diff_mat(p, k)
```

Arguments

p Dimension (number of columns) of the difference matrix.

k Order of the difference matrix.

Value

A sparse matrix of dimension (p - k) x p.

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get_lambda_max

Lambda max for quantile generalized lasso

Description

Compute lambda max for a quantile generalized lasso problem.

Usage

```
get_lambda_max(x, y, d = NULL)
```

Details

This is a rough heuristic derived from fiddling with the KKT conditions when tau = 1/2. It should be possible to improve this. If d is not specified, we will set it equal to the identity (hence interpret the problem as a quantile lasso problem).

get_lambda_seq

Lambda sequence for quantile generalized lasso

Description

Compute a lambda sequence for a quantile generalized lasso problem.

Usage

```
get_lambda_seq(x, y, d = NULL, nlambda, lambda_min_ratio)
```

Details

This function returns nlambda values log-spaced in between lambda_max, as computed by get_lambda_max, and lamdba_max * lambda_min_ratio. If d is not specified, we will set it equal to the identity (hence interpret the problem as a quantile lasso problem).

log_pad

Convenience functions for log padding

Description

```
Functions to map y \mapsto \log(a+y) and x \mapsto \exp(x) - a.
```

```
log_pad(a = 1)
inv_log_pad(a = 1)
```

```
plot.cv_quantile_genlasso
```

Plot function for quantile_genlasso object

Description

Plot the cross-validation error curves, for each quantile level, as functions of the tuning parameter value

Usage

```
## S3 method for class 'cv_quantile_genlasso'
plot(obj, legend_pos = "topleft")
```

Arguments

obj The cv_quantile_genlasso object.

legend_pos Position for the legend; default is "topleft"; use NULL to suppress the legend.

```
predict.cv_quantile_genlasso
```

Predict function for cv_quantile_genlasso object

Description

Predict the conditional quantiles at a new set of predictor variables, using the generalized lasso coefficients stored in a cv_quantile_genlasso object.

Usage

```
## S3 method for class 'cv_quantile_genlasso'
predict(obj, newx, s = NULL,
    sort = FALSE, iso = FALSE, nonneg = FALSE, round = FALSE)
```

Details

This just calls the predict function on the quantile_genlasso that is stored within the given cv_quantile_genlasso object.

```
predict.quantile_genlasso
```

Predict function for quantile_genlasso object

Description

Predict the conditional quantiles at a new set of predictor variables, using the generalized lasso coefficients at particular tau or lambda values.

Usage

```
## S3 method for class 'quantile_genlasso'
predict(obj, newx, s = NULL, sort = FALSE,
  iso = FALSE, nonneg = FALSE, round = FALSE)
```

Arguments

obj	The quantile_genlasso object.
newx	Matrix of new predictor variables at which predictions should be made; if missing, the original (training) predictors are used.
S	Vector of integers specifying the tau and lambda values to consider for predictions; for each i in this vector, a prediction is made at quantile level tau[i] and tuning parameter value lambda[i], according to the tau and lambda vectors stored in the given quantile_genlasso object obj. (Said differently, s specifies the columns of object\$beta to use for the predictions.) Default is NULL, which means that all tau and lambda values will be considered.
sort	Should the quantile estimates be sorted? Default is FALSE. Note: this option only makes sense if the values in the stored tau vector are distinct, and sorted in increasing order.
iso	Should the quantile estimates be passed through isotonic regression? Default is FALSE; if TRUE, takes priority over sort. Note: this option only makes sense if the values in the stored tau vector are distinct, and sorted in increasing order.
nonneg:	should the quantile estimates be truncated at 0? Natural for count data. Default is FALSE.
round:	should the quantile estimates be rounded? Natural for count data. Default is FALSE.

```
{\tt predict.quantile\_genlasso\_grid}
```

Predict function for quantile_genlasso_grid object

Description

Predict the conditional quantiles at a new set of predictor variables, using the generalized lasso coefficients at particular tau or lambda values.

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Usage

```
## S3 method for class 'quantile_genlasso_grid'
predict(obj, newx, sort = FALSE,
  iso = FALSE, nonneg = FALSE, round = FALSE)
```

Details

This function operates as in the predict.quantile_genlasso function for a quantile_genlasso object, but with a few key differences. First, the output is reformatted so that it is an array of dimension (number of prediction points) x (number of tuning parameter values) x (number of quantile levels). This output is generated from the full set of tau and lambda pairs stored in the given quantile_genlasso_grid object obj (selecting a subset is disallowed). Second, the arguments sort and iso operate on the appropriate slices of this array: for a fixed lambda value, we sort or run isotonic regression across all tau values.

quantile_ensemble

Quantile ensemble

Description

Fit ensemble weights, given a set of quantile predictions.

Usage

```
quantile_ensemble(qarr, y, tau, weights = NULL, tau_groups = rep(1,
  length(tau)), intercept = FALSE, nonneg = TRUE, unit_sum = TRUE,
  noncross = TRUE, q0 = NULL, lp_solver = "gurobi",
  time_limit = NULL, params = list(), verbose = FALSE)
```

Arguments

qarr	Array of predicted quantiles, of dimension (number of prediction points) x (number or ensemble components) x (number of quantile levels).
У	Vector of responses (whose quantiles are being predicted by qarr).
tau	Vector of quantile levels at which predictions are made.
weights	Vector of observation weights (to be used in the loss function). Default is NULL, which is interpreted as a weight of 1 for each observation.
tau_groups	Vector of group labels, having the same length as tau. Common labels indicate that the ensemble weights for the corresponding quantile levels should be tied together. Default is rep(1,length(tau)), which means that a common set of ensemble weights should be used across all levels. See details.
intercept	Should an intercept be included in the ensemble model? Default is FALSE.
nonneg	Should the ensemble weights be constrained to be nonnegative? Default is TRUE.
unit_sum	Should the ensemble weights be constrained to sum to 1? Default is TRUE.
noncross	Should noncrossing constraints be enforced? Default is TRUE. Note: this option only matters when there is more than group of ensemble weights, as determined by tau_groups. See details.

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q0 Array of points used to define the noncrossing constraints. Must have dimension (number of points) x (number of ensemble components) x (number of quantile levels). Default is NULL, which means that we consider noncrossing constraints at the training points qarr.

lp_solver One of "gurobi" or "glpk", indicating which LP solver to use. Default is "gurobi".

time_limit This sets the maximum amount of time (in seconds) to allow Gurobi or GLPK to solve any single quantile generalized lasso problem (for a single tau and lambda

value). Default is NULL, which means unlimited time.

params A list of control parameters to pass to Gurobi or GLPK. Default is list() which means no additional parameters are passed. For example: with Gurobi, we can use list(Threads=4) to specify that Gurobi should use 4 threads when available. (Note that if a time limit is specified through this params list, then its value will be overriden by the last argument time_limit, assuming the latter is not

NULL.)

verbose Should progress be printed out to the console? Default is FALSE.

Details

This function solves the following quantile ensemble optimization problem, over quantile levels $\tau_k, k = 1, \dots, r$:

$$\underset{\alpha_j, j=1, \dots, p}{\text{minimize}} \sum_{k=1}^r \sum_{i=1}^n w_i \psi_{\tau_k} \left(y_i - \sum_{j=1}^p \alpha_j q_{ijk} \right)$$

subject to
$$\sum_{j=1}^{p} \alpha_j = 1, \ \alpha_j \ge 0, \ j = 1, \dots, p$$

for a response vector y and quantile array q, where q_{ijk} is an estimate of the quantile of y_i at the level τ_k , from ensemble component member j. Here $\psi_{\tau}(v) = \max\{\tau v, (\tau-1)v\}$ is the "pinball" or "tilted ℓ_1 " loss. A more advanced version allows us to estimate a separate ensemble weight α_{jk} per component method j, per quantile level k:

minimize
$$\alpha_{jk}, j = 1, ..., p, k = 1, ..., r \sum_{k=1}^{r} \sum_{i=1}^{n} w_i \psi_{\tau_k} \left(y_i - \sum_{j=1}^{p} \alpha_{jk} q_{ijk} \right)$$

subject to
$$\sum_{j=1}^{p} \alpha_{jk} = 1, \ k = 1, \dots, r, \ \alpha_{jk} \ge 0, \ j = 1, \dots, p, \ k = 1, \dots, r$$

As a form of regularization, we can additionally incorporate noncrossing constraints into the above optimization, which take the form:

$$\alpha_{\bullet,k}^T q \leq \alpha_{\bullet,k+1}^T q, \ k=1,\ldots,r-1, \ q \in \mathcal{Q}$$

where the quantile levels $\tau_k, k=1,\ldots,r$ are assumed to be in increasing order, and $\mathcal Q$ is a collection of points over which to enforce the noncrossing constraints. Finally, somewhere in between these two extremes is to allow one ensemble weight per component member j, per quantile group g. This can be interpreted as a set of further constraints which enforce equality between α_{jk} and $\alpha_{j\ell}$, for all k,ℓ that are in the same group g.

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Value

A list with the following components:

• alpha: vector or matrix of ensemble weights. If tau_groups has only one unique label, then this is a vector of length = (number of ensemble components); otherwise, it is a matrix, of dimension (number of ensemble components) x (number of quantile levels)

- · tau: vector of quantile levels used
- weights, tau_groups, ..., params: values of these other arguments used in the function call

```
quantile_extrapolate Quantile extrapolater
```

Description

Extrapolate a set of quantiles at new quantile levels: parametric in the tails, nonparametric in the middle.

Usage

```
quantile_extrapolate(tau, qvals, tau_out = c(0.01, 0.025, seq(0.05, 0.95, by = 0.05), 0.975, 0.99), sort = TRUE, iso = FALSE, nonneg = FALSE, round = FALSE, qfun_left = qnorm, qfun_right = qnorm, n_tau_left = 1, n_tau_right = 1, middle = c("cubic", "linear"), param0 = NULL, param1 = NULL, grid_size = 1000, tol = 0.01, max_iter = 10)
```

Arguments

tau	Vector of quantile levels. Assumed to be distinct, and sorted in increasing order.	
qvals	Vector or matrix quantiles; if a matrix, each row is a separate set of quantiles, at the same (common) quantile levels, given by tau.	
tau_out	Vector of quantile levels at which to perform extrapolation. Default is a sequence of 23 quantile levels from 0.01 to 0.99.	
sort	Should the quantile estimates be sorted? Default is FALSE. Note: this option only makes sense if the values in the stored tau vector are distinct, and sorted in increasing order.	
iso	Should the quantile estimates be passed through isotonic regression? Default is FALSE; if TRUE, takes priority over sort. Note: this option only makes sense if the values in the stored tau vector are distinct, and sorted in increasing order.	
qfun_left, qfun_right		

Quantile functions on which to base extrapolation in the left and right tails, respectively; each must be a function whose first two arguments are a quantile level and a distribution parameter (such as a mean parameter); these are assumed to be vectorized in the first argument when the second argument is fixed, and also vectorized in the second argument when the first argument is fixed. Default is qnorm. See details for further explanation.

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```
n_tau_left, n_tau_right
```

Integers between 1 and the length of tau, indicating how many elements quantile levels from the left and right ends, respectively, to use in defining the tails. For example, if n_tau_left=1, the default, then only the leftmost quantile is used for the left tail extrapolation; if n_tau_left=2, then the two leftmost quantiles are used, etc; and similarly for n_tau_right. See details for further explanation.

middle

One of "cubic" or "linear", indicating the interpolation method to use in the middle (outside of the tails, as determined by n_tau_left and n_tau_right). If "cubic", the default, then a monotone cubic spline interpolant is fit to the given quantiles, and used to estimate quantiles in the middle. If "linear", then linear interpolation is used to estimate quantiles in the middle.

nonneg:

should the quantile estimates be truncated at 0? Natural for count data. Default is FALSE.

Details

TODO

Value

A matrix of dimension (number of rows in qvals) x (length of tau_out), where each row is the extrapolation of the set of quantiles in the corresponding row of qvals, at the quantile levels specified in tau_out.

quantile_genlasso

Quantile generalized lasso

Description

Compute quantile generalized lasso solutions.

Usage

```
quantile_genlasso(x, y, d, tau, lambda, weights = NULL,
  no_pen_rows = c(), intercept = TRUE, standardize = TRUE,
  noncross = FALSE, x0 = NULL, lp_solver = c("gurobi", "glpk"),
  time_limit = NULL, warm_starts = TRUE, params = list(),
  transform = NULL, inv_trans = NULL, jitter = NULL,
  verbose = FALSE)
```

Arguments

x Matrix of predictors. If sparse, then passing it an appropriate sparse Matrix class can greatly help optimization.

y Vector of responses.

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d Matrix defining the generalized lasso penalty; see details. If sparse, then passing it an appropriate sparse Matrix class can greatly help optimization. A convenience function get_diff_mat for constructing trend filtering penalties is pro-

vided.

tau, lambda Vectors of quantile levels and tuning parameter values. If these are not of the

same length, the shorter of the two is recycled so that they become the same length. Then, for each i, we solve a separate quantile generalized lasso problem at quantile level tau[i] and tuning parameter value lambda[i]. The most common use cases are: specifying one tau value and a sequence of lambda values;

or specifying a sequence of tau values and one lambda value.

weights Vector of observation weights (to be used in the loss function). Default is NULL,

which is interpreted as a weight of 1 for each observation.

no_pen_rows Indices of the rows of d that should be excluded from the generalized lasso

penalty. Default is c(), which means that no rows are to be excluded.

intercept Should an intercept be included in the regression model? Default is TRUE.

standardize Should the predictors be standardized (to have zero mean and unit variance)

before fitting? Default is TRUE.

noncross Should noncrossing constraints be applied? These force the estimated quantiles

to be properly ordered across all quantile levels being considered. The default is FALSE. If TRUE, then noncrossing constraints are applied to the estimated quantiles at all points specified by the next argument x0. Note: this option only makes sense if the values in the tau vector are distinct, and sorted in increasing

order.

Matrix of points used to define the noncrossing constraints. Default is NULL,

which means that we consider noncrossing constraints at the training points x.

lp_solver One of "gurobi" or "glpk", indicating which LP solver to use. Default is "gurobi".

This sets the maximum amount of time (in seconds) to allow Gurobi or GLPK to solve any single quantile generalized lasso problem (for a single tau and lambda

value). Default is NULL, which means unlimited time.

warm_starts Should warm starts be used in the LP solver (from one LP solve to the next)?

Only supported for Gurobi.

params A list of control parameters to pass to Gurobi or GLPK. Default is list() which means no additional parameters are passed. For example: with Gurobi, we can

use list(Threads=4) to specify that Gurobi should use 4 threads when available. (Note that if a time limit is specified through this params list, then its value will be overriden by the last argument time_limit, assuming the latter is not

NULL.)

transform, inv_trans

jitter

time_limit

The first is a function to transform y before solving the quantile generalized lasso; the second is the corresponding inverse transform. For example: for count data, we might want to model log(1+y) (which would be the transform, and the inverse transform would be exp(x)-1). Both transform and inv_trans should

be vectorized. Convenience functions log_pad and inv_log_pad are provided.

Function for applying random jitter to y, which might help optimization. For example: for count data, there can be lots of ties (with or without transformation of y), which can make optimization more difficult. The function jitter

should take an integer n and return n random draws. A convenience function

 $unif_jitter$ is provided.

verbose Should progress be printed out to the console? Default is FALSE.

Details

This function solves the quantile generalized lasso problem, for each pair of quantile level τ and tuning parameter λ :

minimize
$$\sum_{i=1}^{n} w_i \psi_{\tau}(y_i - \beta_0 - x_i^T \beta) + \lambda ||D\beta||_1$$

for a response vector y with components y_i , predictor matrix X with rows x_i , and penalty matrix D. Here $\psi_{\tau}(v) = \max\{\tau v, (\tau - 1)v\}$ is the "pinball" or "tilted ℓ_1 " loss. When noncrossing constraints are applied, we instead solve one big joint optimization, over all quantile levels and tuning parameter values:

$$\underset{\beta_{0k}, \beta_k, k=1, ..., r}{\text{minimize}} \sum_{k=1}^{r} \left(\sum_{i=1}^{n} w_i \psi_{\tau_k} (y_i - \beta_{0k} - x_i^T \beta_k) + \lambda_k \|D\beta_k\|_1 \right)$$

subject to
$$\beta_{0k} + x^T \beta_k \le \beta_{0,k+1} + x^T \beta_{k+1} \ k = 1, ..., r-1, \ x \in \mathcal{X}$$

where the quantile levels τ_k , $k=1,\ldots,r$ are assumed to be in increasing order, and \mathcal{X} is a collection of points over which to enforce the noncrossing constraints.

Either problem is readily converted into a linear program (LP), and solved using either Gurobi (which is free for academic use, and generally fast) or GLPK (which free for everyone, but slower).

Value

A list with the following components:

- beta: a matrix of generalized lasso coefficients, of dimension = (number of features + 1) x (number of quantile levels) assuming intercept=TRUE, else (number of features) x (number of quantile levels). Note: these coefficients will always be on the appropriate scale; they are always on the scale of original features, even if standardize=TRUE
- status: vector of status flags returned by Gurobi's or GLPK's LP solver, of length = (number of quantile levels)
- tau, lambda: vectors of tau and lambda values used
- weights, no_pen_rows, ..., jitter: values of these other arguments used in the function call

Author(s)

Ryan Tibshirani

quantile_genlasso_grid

Quantile generalized lasso on a tau by lambda grid

Description

Convenience function for computing quantile generalized lasso solutions on a tau by lambda grid.

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Usage

```
quantile_genlasso_grid(x, y, d, tau, lambda = NULL, nlambda = 30,
  lambda_min_ratio = 0.001, weights = NULL, no_pen_rows = c(),
  intercept = TRUE, standardize = TRUE, lp_solver = c("gurobi",
  "glpk"), time_limit = NULL, warm_starts = TRUE, params = list(),
  transform = NULL, inv_trans = NULL, jitter = NULL,
  verbose = FALSE)
```

Arguments

nlambda Number of lambda values to consider, for each quantile level. Default is 30. lambda_min_ratio

Ratio of the minimum to maximum lambda value, for each quantile levels. Default is 1e-3.

Details

This function forms a lambda vector either determined by the nlambda and lambda_min_ratio arguments, or the lambda argument; if the latter is specified, then it takes priority. Then, for each i and j, we solve a separate quantile generalized lasso problem at quantile level tau[i] and tuning parameter value lambda[j], using the quantile_genlasso function. All arguments (aside from nlambda and lambda_min_ratio) are as in the latter function; noncrossing constraints are disallowed.

```
quantile_genlasso_objective
```

Quantile generalized lasso objective

Description

Compute generalized lasso objective for a single tau and lambda value.

Usage

```
quantile_genlasso_objective(x, y, d, beta, tau, lambda)
```

quantile_lasso

Quantile lasso.

Description

Compute quantile lasso solutions.

```
quantile_lasso(x, y, tau, lambda, weights = NULL, no_pen_vars = c(),
  intercept = TRUE, standardize = TRUE, noncross = FALSE,
  x0 = NULL, lp_solver = c("gurobi", "glpk"), time_limit = NULL,
  warm_starts = TRUE, params = list(), transform = NULL,
  inv_trans = NULL, jitter = NULL, verbose = FALSE)
```

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Arguments

x Matrix of predictors. If sparse, then passing it an appropriate sparse Matrix class can greatly help optimization.

y Vector of responses.

tau, lambda Vectors of quantile levels and tuning parameter values. If these are not of the

same length, the shorter of the two is recycled so that they become the same length. Then, for each i, we solve a separate quantile lasso problem at quantile level tau[i] and tuning parameter value lambda[i]. The most common use cases are: specifying one tau value and a sequence of lambda values; or

specifying a sequence of tau values and one lambda value.

weights Vector of observation weights (to be used in the loss function). Default is NULL,

which is interpreted as a weight of 1 for each observation.

no_pen_vars Indices of the variables that should be excluded from the lasso penalty. Default

is c(), which means that no variables are to be excluded.

Details

This function solves the quantile lasso problem, for each pair of quantile level τ and tuning parameter λ :

minimize
$$\sum_{i=1}^{n} w_i \psi_{\tau} (y_i - \beta_0 - x_i^T \beta) + \lambda \|\beta\|_1$$

for a response vector y with components y_i , and predictor matrix X with rows x_i . Here $\psi_{\tau}(v) = \max\{\tau v, (\tau - 1)v\}$ is the "pinball" or "tilted ℓ_1 " loss. When noncrossing constraints are applied, we instead solve one big joint optimization, over all quantile levels and tuning parameter values:

$$\underset{\beta_{0k}, \beta_k, k=1, ..., r}{\text{minimize}} \sum_{k=1}^{r} \left(\sum_{i=1}^{n} w_i \psi_{\tau_k} (y_i - \beta_{0k} - x_i^T \beta_k) + \lambda_k \|\beta_k\|_1 \right)$$

subject to
$$\beta_{0k} + x^T \beta_k \leq \beta_{0,k+1} + x^T \beta_{k+1}$$
 $k = 1, \dots, r-1, x \in \mathcal{X}$

where the quantile levels τ_j , $j=1,\ldots,k$ are assumed to be in increasing order, and \mathcal{X} is a collection of points over which to enforce the noncrossing constraints.

Either problem is readily converted into a linear program (LP), and solved using either Gurobi (which is free for academic use, and generally fast) or GLPK (which free for everyone, but slower).

All arguments not described above are as in the quantile_genlasso function. The associated coef and predict functions are just those for the quantile_genlasso class.

Value

A list with the following components:

- beta: a matrix of lasso coefficients, of dimension = (number of features + 1) x (number of quantile levels) assuming intercept=TRUE, else (number of features) x (number of quantile levels). Note: these coefficients will always be on the appropriate scale; they are always on the scale of original features, even if standardize=TRUE
- status: vector of status flags returned by Gurobi's or GLPK's LP solver, of length = (number of quantile levels)
- tau, lambda: vectors of tau and lambda values used
- weights, no_pen_vars, ..., jitter: values of these other arguments used in the function call

Author(s)

Ryan Tibshirani

```
quantile_lasso_grid Quantile lasso on a tau by lambda grid
```

Description

Convenience function for computing quantile lasso solutions on a tau by lambda grid.

Usage

```
quantile_lasso_grid(x, y, tau, lambda = NULL, nlambda = 30,
  lambda_min_ratio = 0.001, weights = NULL, no_pen_vars = c(),
  intercept = TRUE, standardize = TRUE, lp_solver = c("gurobi",
  "glpk"), time_limit = NULL, warm_starts = TRUE, params = list(),
  transform = NULL, inv_trans = NULL, jitter = NULL,
  verbose = FALSE)
```

Arguments

nlambda Number of lambda values to consider, for each quantile level. Default is 30. lambda_min_ratio

Ratio of the minimum to maximum lambda value, for each quantile levels. Default is 1e-3.

Details

This function forms a lambda vector either determined by the nlambda and lambda_min_ratio arguments, or the lambda argument; if the latter is specified, then it takes priority. Then, for each i and j, we solve a separate quantile lasso problem at quantile level tau[i] and tuning parameter value lambda[j], using the quantile_lasso function. All arguments (aside from nlambda and lambda_min_ratio) are as in the latter function; noncrossing constraints are disallowed. The associated predict function is just that for the quantile_genlasso_grid class.

```
quantile_lasso_objective

Quantile lasso objective
```

Description

Compute lasso objective for a single tau and lambda value.

```
quantile_lasso_objective(x, y, beta, tau, lambda)
```

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Description

Compute the quantile (tilted absolute) loss for a single tau value.

Usage

```
quantile_loss(yhat, y, tau)
```

```
refit_quantile_genlasso
```

Refit function for cv_quantile_genlasso object

Description

Refit generalized lasso solutions at a new set of quantile levels, given an existing cv_quantile_genlasso object.

Usage

```
refit_quantile_genlasso(obj, x, y, d, tau_new = c(0.01, 0.025, seq(0.05, 0.95, by = 0.05), 0.975, 0.99), weights = NULL, no_pen_rows = NULL, intercept = TRUE, standardize = TRUE, noncross = FALSE, x0 = NULL, lp_solver = NULL, time_limit = NULL, warm_starts = NULL, params = NULL, transform = NULL, inv_trans = NULL, jitter = NULL, verbose = FALSE)
```

Arguments

obj	The cv_quantile_genlasso object to start from.
x	Matrix of predictors.
У	Vector of responses.
d	Matrix defining the generalized lasso penalty.
tau_new	Vector of new quantile levels at which to fit new solutions. Default is a sequence of 23 quantile levels from 0.01 to 0.99.
noncross	Should noncrossing constraints be applied? These force the estimated quantiles to be properly ordered across all quantile levels being considered. The default is FALSE. If TRUE, then noncrossing constraints are applied to the estimated quantiles at all points specified by the next argument x0.
x0	Matrix of points used to define the noncrossing constraints. Default is NULL, which means that we consider noncrossing constraints at the training points x.
verbose	Should progress be printed out to the console? Default is FALSE.

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Details

This function simply infers, for each quantile level in tau_new, a (very) roughly-CV-optimal tuning parameter value, then calls quantile_genlasso at the new quantile levels and corresponding tuning parameter values. If not specified, the arguments weights, no_pen_rows, intercept, standardize, lp_solver, time_limit, warm_starts, params, transform, inv_transorm, jitter are all inherited from the given cv_quantile_genlasso object.

Value

A quantile_genlasso object, with solutions at quantile levels tau_new.

Description

Refit lasso solutions at a new set of quantile levels, given an existing cv_quantile_lasso object.

Usage

```
refit_quantile_lasso(obj, x, y, tau_new = c(0.01, 0.025, seq(0.05, 0.95, by = 0.05), 0.975, 0.99), weights = NULL, no_pen_rows = NULL, intercept = TRUE, standardize = TRUE, noncross = FALSE, x0 = NULL, lp_solver = NULL, time_limit = NULL, warm_starts = NULL, params = NULL, transform = NULL, inv_trans = NULL, jitter = NULL, verbose = FALSE)
```

Arguments

obj	The cv_quantile_lasso object to start from.
x	Matrix of predictors.
У	Vector of responses.
tau_new	Vector of new quantile levels at which to fit new solutions. Default is a sequence of 23 quantile levels from 0.01 to 0.99.
noncross	Should noncrossing constraints be applied? These force the estimated quantiles to be properly ordered across all quantile levels being considered. The default is FALSE. If TRUE, then noncrossing constraints are applied to the estimated quantiles at all points specified by the next argument $x0$.
x0	Matrix of points used to define the noncrossing constraints. Default is NULL, which means that we consider noncrossing constraints at the training points x.
verbose	Should progress be printed out to the console? Default is FALSE.

Details

This function simply infers, for each quantile level in tau_new, a (very) roughly-CV-optimal tuning parameter value, then calls quantile_lasso at the new quantile levels and corresponding tuning parameter values. If not specified, the arguments weights, no_pen_rows, intercept, standardize, lp_solver, time_limit, warm_start, params, transform, inv_transorm, jitter are all inherited from the given cv_quantile_lasso object.

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Value

A quantile_lasso object, with solutions at quantile levels tau_new.

 $unif_jitter$

Convenience function for uniform jitter

Description

Function to generate random draws from Unif[a, b].

```
unif_jitter(a = 0, b = 0.01)
```

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