

# Summary of Inference

Starting Point:

1. What are the observational units?
2. What are the variables?
3. Is each variable quantitative or categorical?

What Did You Measure?	Conditions for Inference	Population Parameter	Sample Statistic	R function	CI	Hypothesis Test
A Categorical Variable (or a count of how many in sample were in a certain category)	<ul style="list-style-type: none"> <li>• Representative sample</li> <li>• Independent observational units</li> <li>• Count of how many in sample were in a certain category</li> </ul>	$p$ : proportion of population in a certain category	$\hat{p}$ : proportion of sample in a certain category	<code>binom.test</code>	from R	from R
A Quantitative Variable	<ul style="list-style-type: none"> <li>• Representative sample</li> <li>• Independent observational units</li> <li>• Quantitative variable</li> <li>• Mean is a good summary of the center (distribution is approximately unimodal and symmetric, no serious outliers)</li> </ul>	$\mu$ : population mean	$\bar{x}$ : sample mean	<code>t.test</code>	$\bar{x} \pm t_{n-1}^* s / \sqrt{n}$	test statistic: $t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$ If the null hypothesis is true, then $t \sim t_{n-1}$
2 Quantitative Variables (possibly also other variables)	Think of Robert the leprechaun: <b>R. O'LINE</b> <ul style="list-style-type: none"> <li>• <b>R</b>epresentative sample</li> <li>• <b>N</b>o <b>O</b>utliers</li> <li>• <b>L</b>inear relationship</li> <li>• <b>I</b>ndependent observational units</li> <li>• <b>N</b>ormally distributed residuals</li> <li>• <b>E</b>qual variance of residuals</li> </ul>	$\beta_0$ : Intercept of line describing population $\beta_1$ : Slope of line describing population (possibly also other coefficients)	$b_0$ : Intercept of line describing sample $b_1$ : Slope of line describing sample (possibly also other coefficients)	<code>lm</code>	$b_0 \pm t_{n-k-1}^* SE(b_0)$ $b_1 \pm t_{n-k-1}^* SE(b_1)$ $k$ = number of explanatory variables (1 for simple linear regression)	test statistic: $t = \frac{b_0 - \beta_0^{null}}{SE(b_0)}$ or $t = \frac{b_1 - \beta_1^{null}}{SE(b_1)}$ If the null hypothesis is true, then $t \sim t_{n-k-1}$