

Automating Algorithm Design through Genetic Programming Hyper-Heuristics

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Morris, MN

What does the title mean?

- Reducing the human component in algorithm design



[https://scratch.mit.edu/
discuss/m/topic/200574/](https://scratch.mit.edu/discuss/m/topic/200574/)

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- Reducing the human component in algorithm design
- More work at the beginning, more possibilities



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What does the title mean?

- Reducing the human component in algorithm design
- More work at the beginning, more possibilities
- Genetic programming hyper-heuristics as a method to the madness



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Outline

- 1 Background
- 2 Hyper-heuristics
- 3 Genetic Programming Variants
- 4 Autoconstruction
- 5 Summary

Outline

1 Background

- Evolutionary Computation
- Genetic Programming

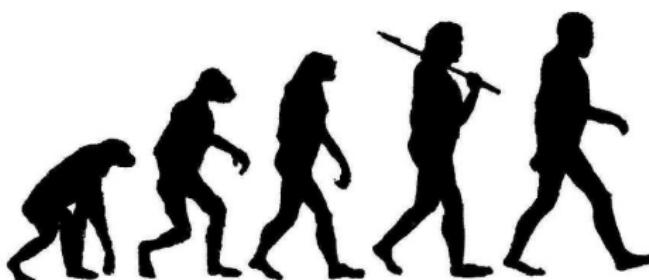
2 Hyper-heuristics

3 Genetic Programming Variants

4 Autoconstruction

5 Summary

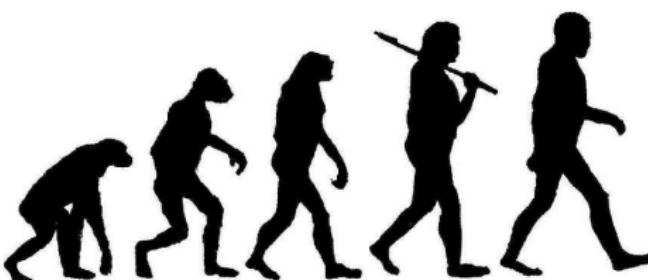
Evolutionary Computation



<https://www.spigotmc.org/attachments/evolution-jpg.137048/>

- Subfield of Artificial Intelligence

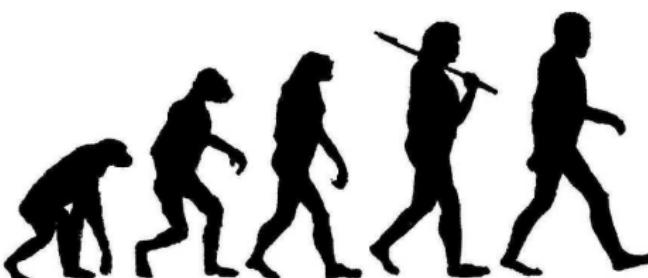
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- Subfield of Artificial Intelligence
- Algorithms based on biological evolution

Evolutionary Computation

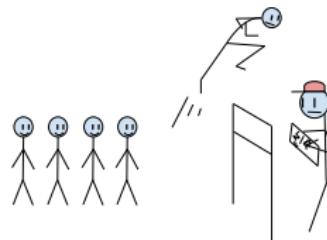
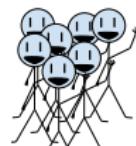
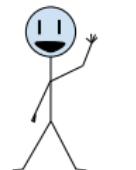


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- Subfield of Artificial Intelligence
- Algorithms based on biological evolution
- Uses lots of terminology from biology, doesn't always mean same thing as term means in biology.

Evolutionary Computation – Terminology

- **Individual** – a potential solution to a problem (or set of problems)
- **Population** – a group of individuals
- **Fit** – how well suited an individual is at solving a problem
- **Fitness Test** – a set of tests to determine how fit an individual is.



Evolutionary Computation – Terminology

- **Mutation** – an insertion, deletion, or small change in the code of an individual, creating a new individual
- **Sexual reproduction** – when two or more individuals are munged together to create a new individual

Evolutionary Computation – Terminology

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If individual A experiences a mutation to create individual B, then:

- **Parent** – Individual A



- **Child** – Individual B



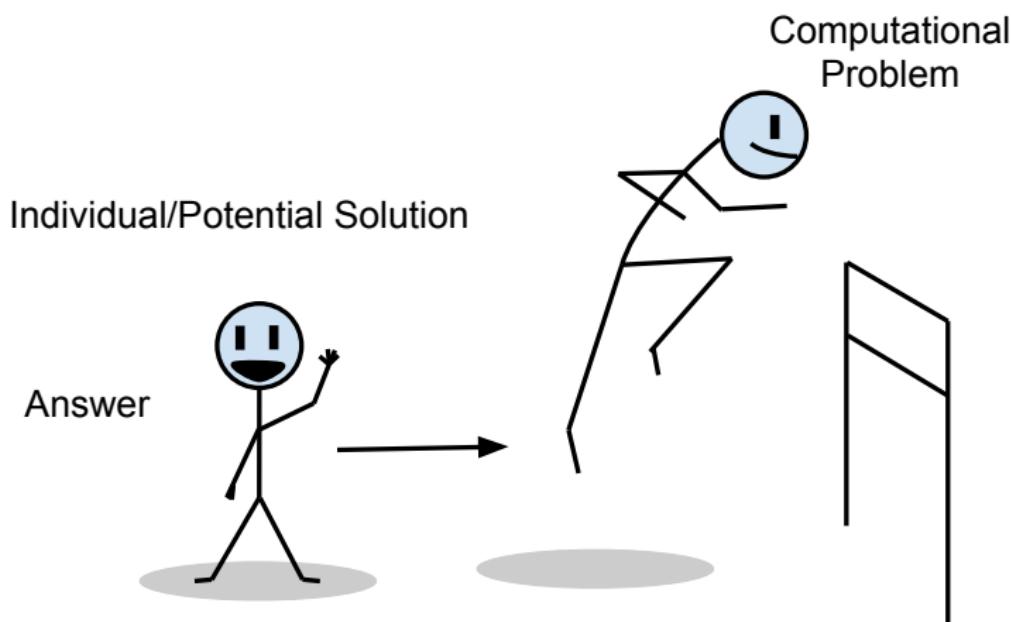
Evolutionary Computation – Terminology

- **Generation** – a population of individuals
- **Global optima** – best solution (or solutions) possible
- **Stopping point** – time limit, or generation limit.

Genetic Programming

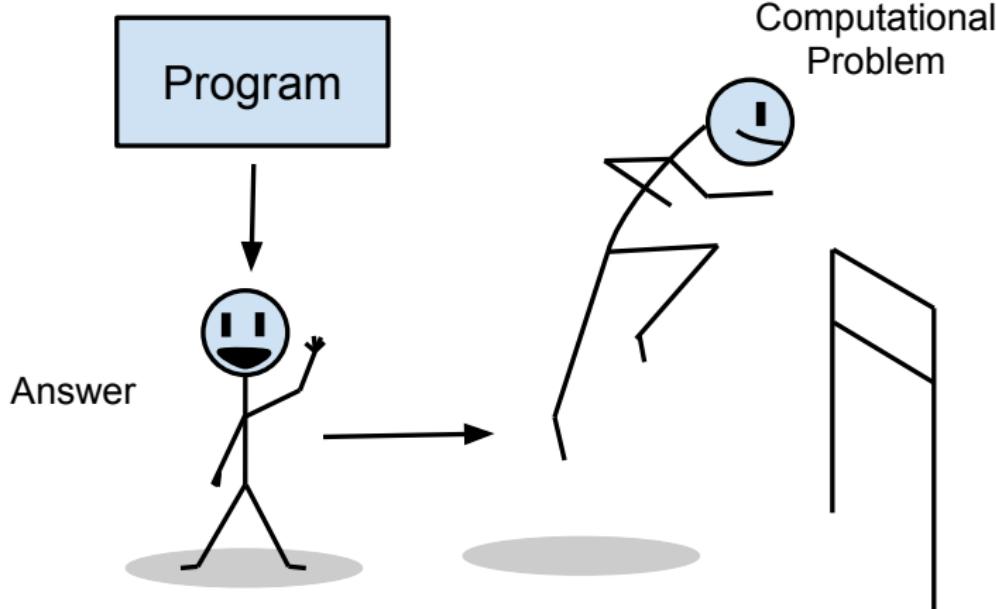
A family of algorithms in Evolutionary Computation that uses biological techniques to create programs to solve computational problems.

Genetic Programming

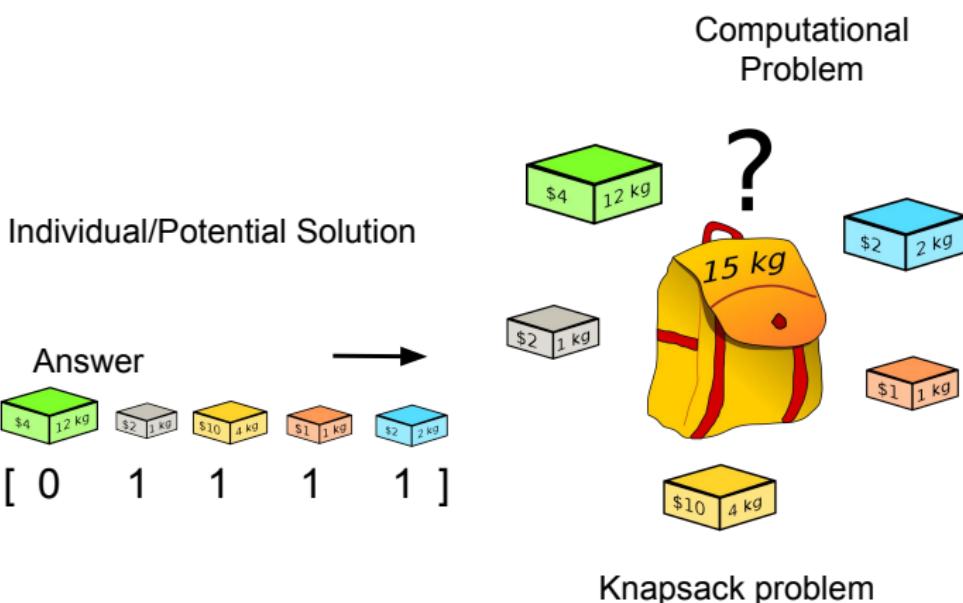


Genetic Programming

Individual/Potential Solution

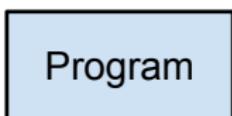


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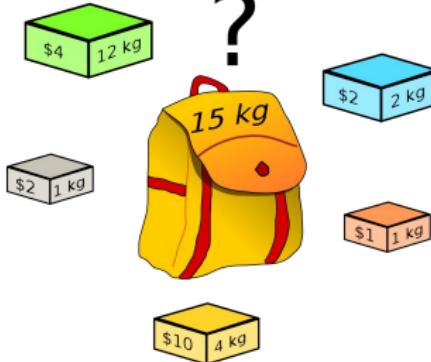


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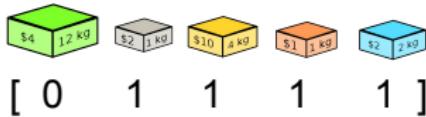
Individual/Potential Solution



Computational
Problem



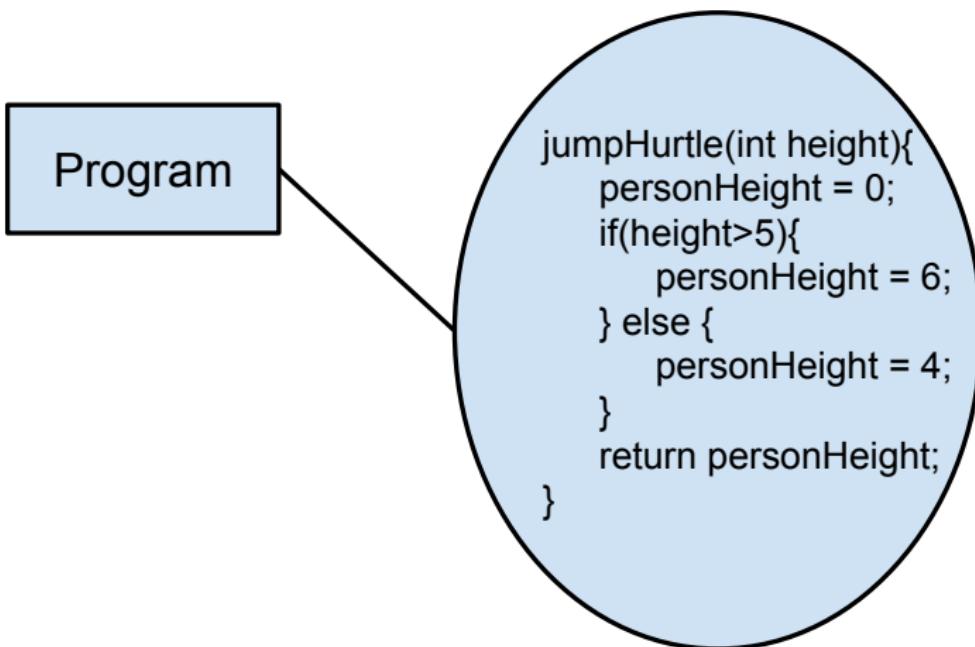
Answer



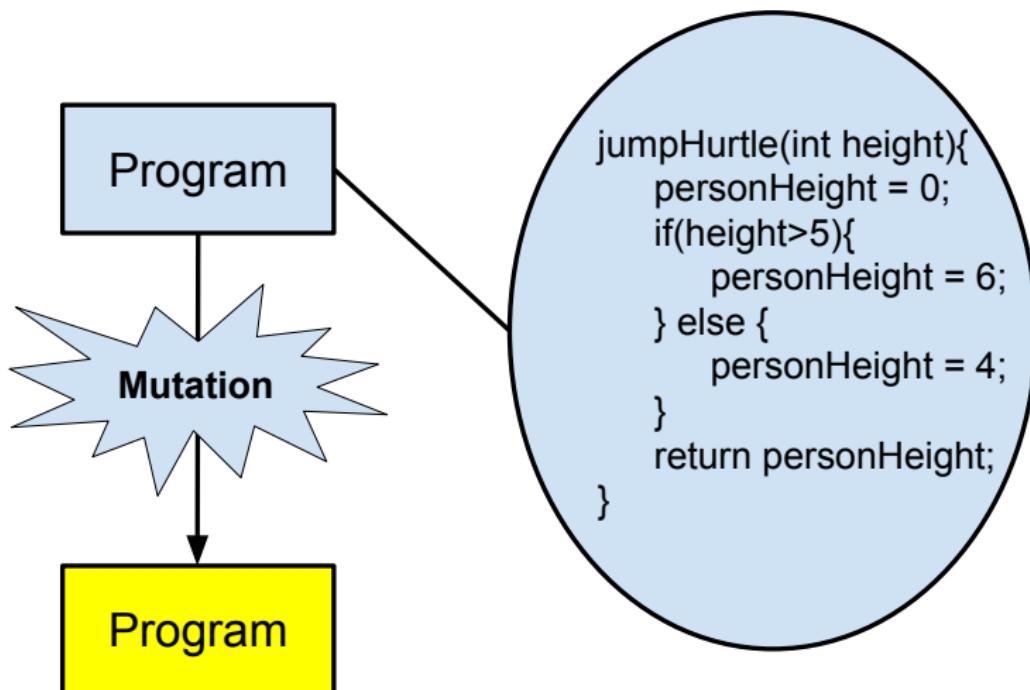
Knapsack problem

Based on <https://upload.wikimedia.org/wikipedia/commons/thumb/f/fd/Knapsack.svg/1200px-Knapsack.svg.png>

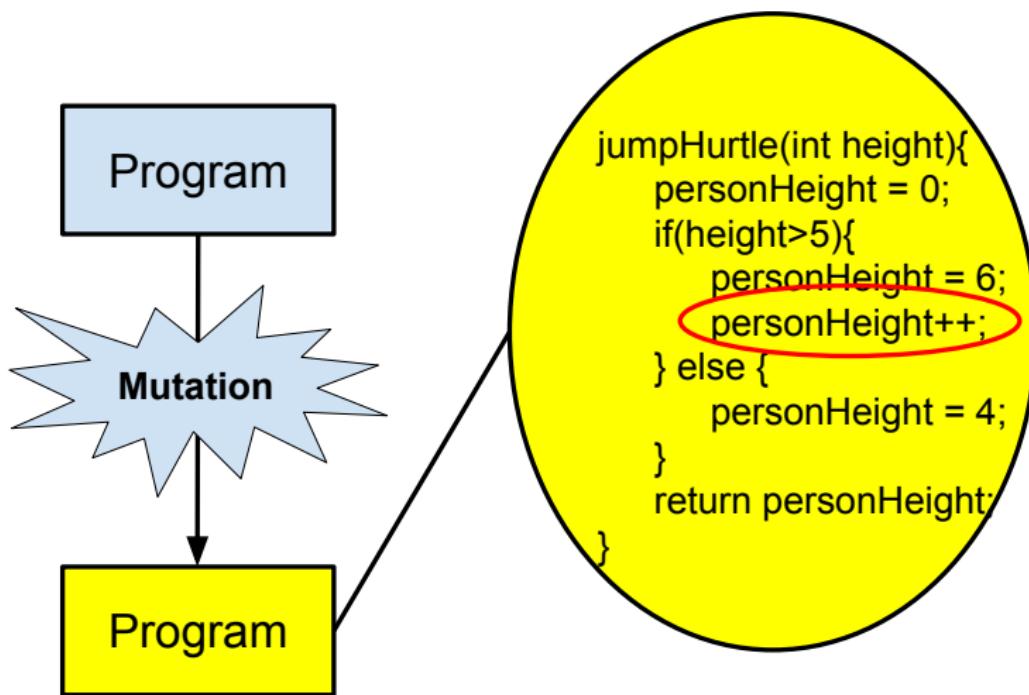
Genetic Programming



Genetic Programming



Genetic Programming



Outline

1 Background

2 Hyper-heuristics

- Heuristics
- Hyper-heuristics

3 Genetic Programming Variants

4 Autoconstruction

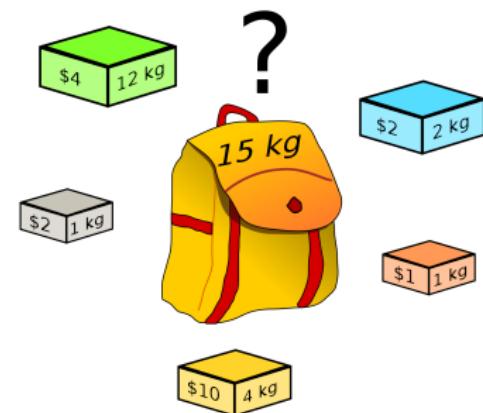
5 Summary

Heuristics

Heuristics – a function that ranks alternatives in a search algorithm at each branching step and uses that information to choose which branch to follow.

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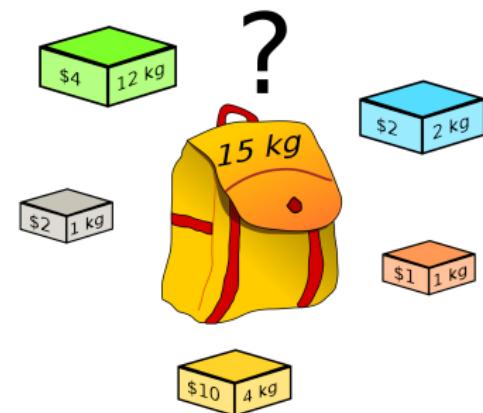


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Heuristics

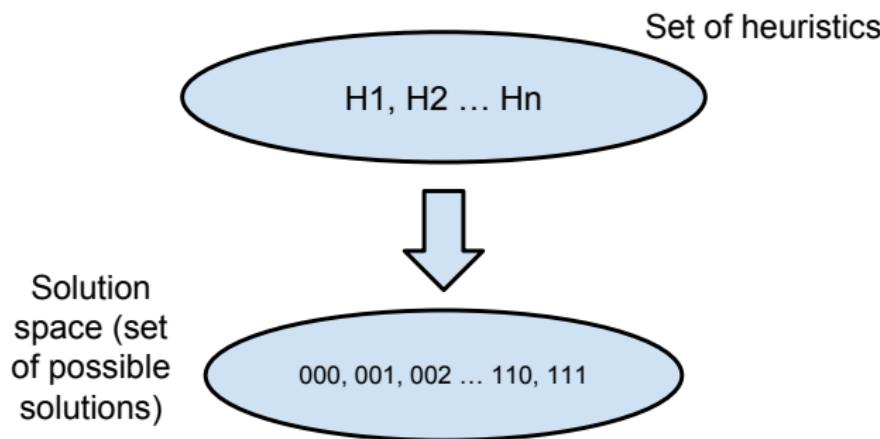
Heuristics – a function that ranks alternatives in a search algorithm at each branching step and uses that information to choose which branch to follow.

Example: “Select highest valued item and put into knapsack. If item puts knapsack overweight, select next highest value instead. Repeat until all items are gone or until the knapsack is full”



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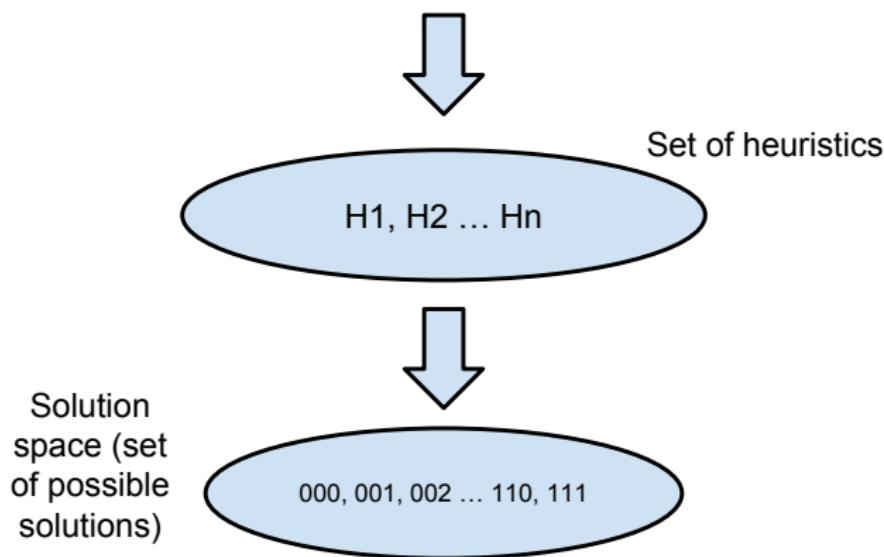
Heuristics



Based on figures from Tauritz et al. (see paper for reference)

Hyper-heuristics

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Hyper-heuristics

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Genetic programming hyper-heuristics – hyper-heuristics that use genetic programming for the process of selecting, generating, or adapting several simpler heuristics.

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2 Hyper-heuristics

3 Genetic Programming Variants

- What are they?
- Why should we care?
- Stack-based genetic programming

4 Autoconstruction

5 Summary

Genetic programming variants

GP variants – variations on the structure and setup of a genetic programming system.

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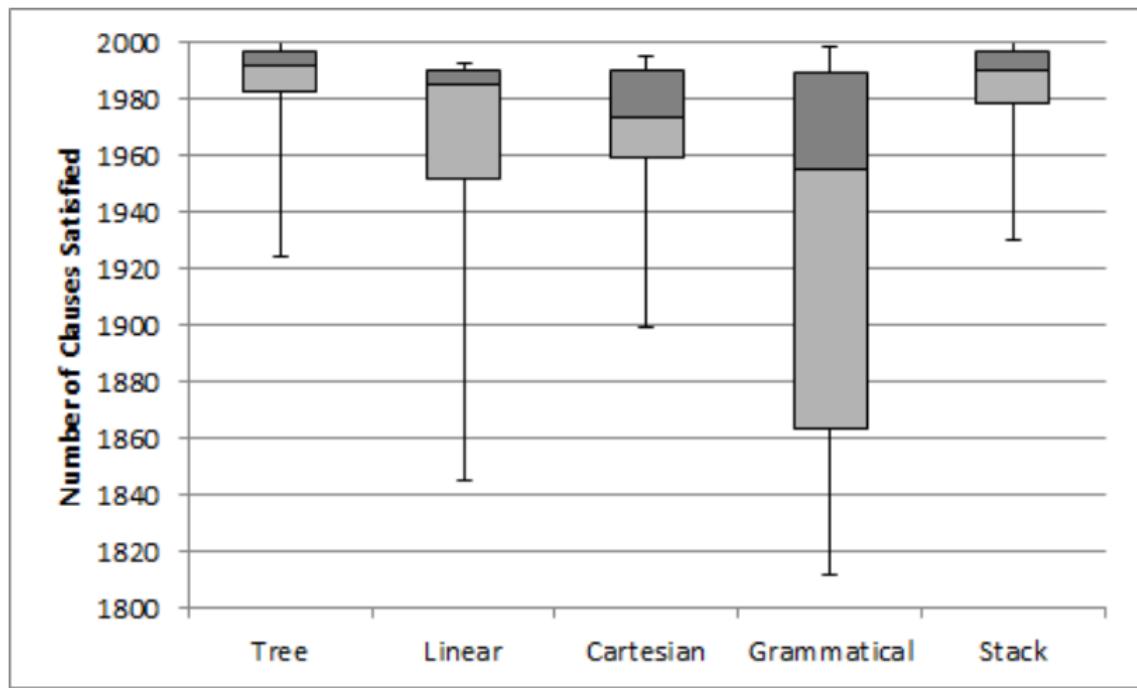
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GP variants tested:

- Cartesian GP
- Linear GP
- Stack-based GP
- Tree-based GP
- Grammatical Evolution

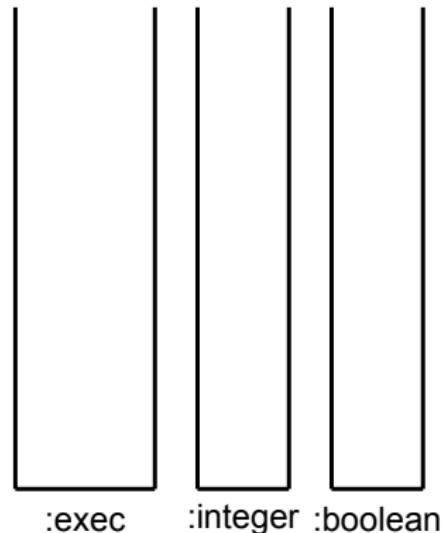
Why should we care?



Graph taken from Harris et al. [1]

Stack-based genetic programming

Data-stacks are used for managing input and output of operations.

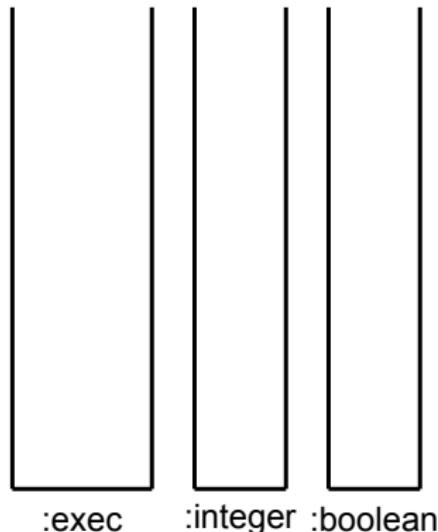


Stack-based genetic programming

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Programs are represented as linear sequences of literals and instructions.
Below is an example of a simple Push program:

(1 integer_add 2 integer_equal)

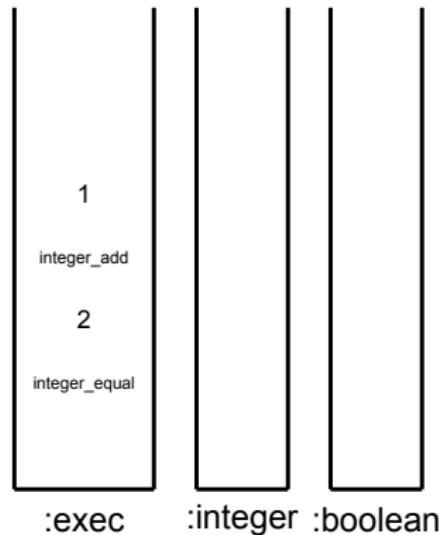


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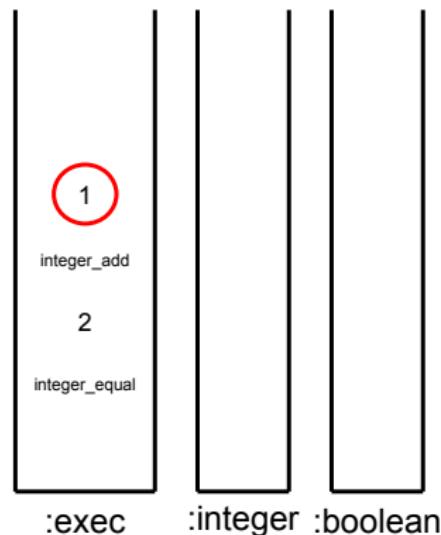


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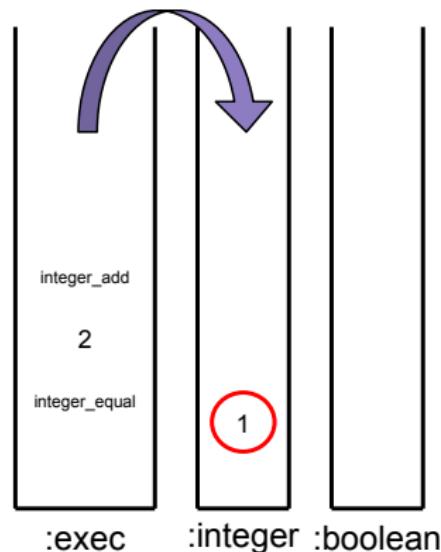


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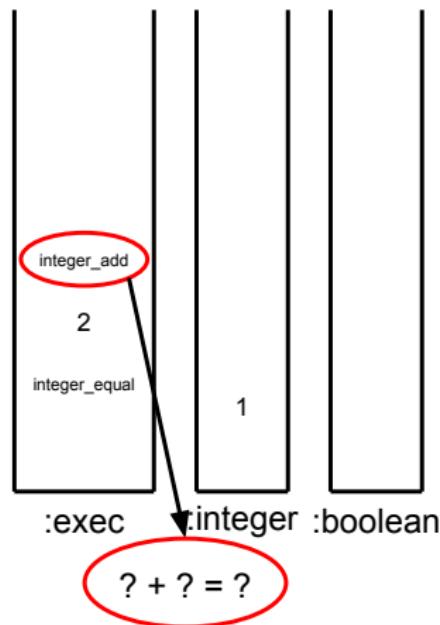


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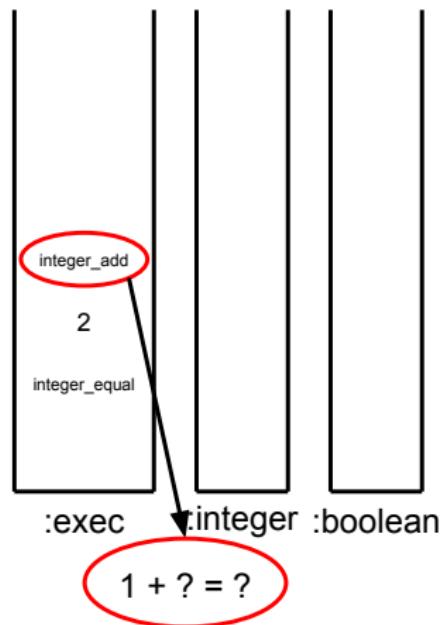


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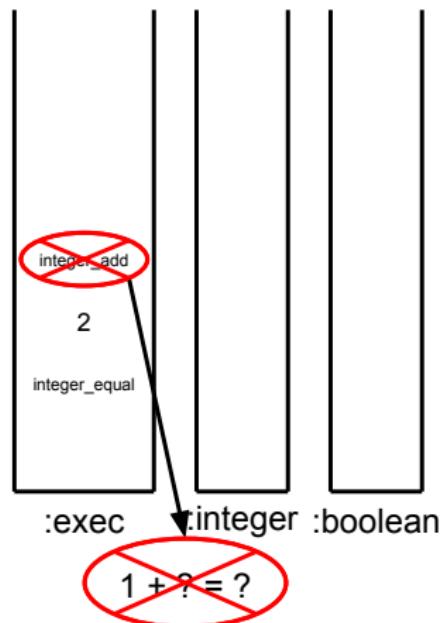


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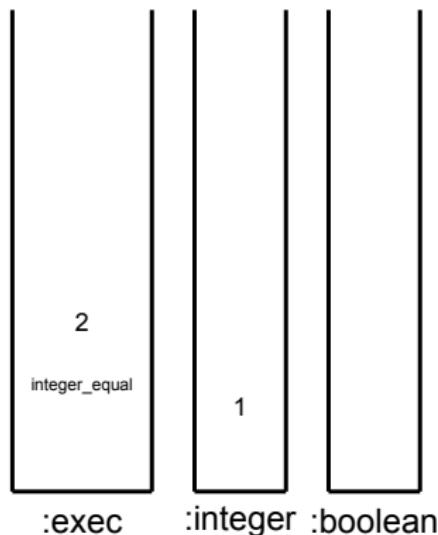


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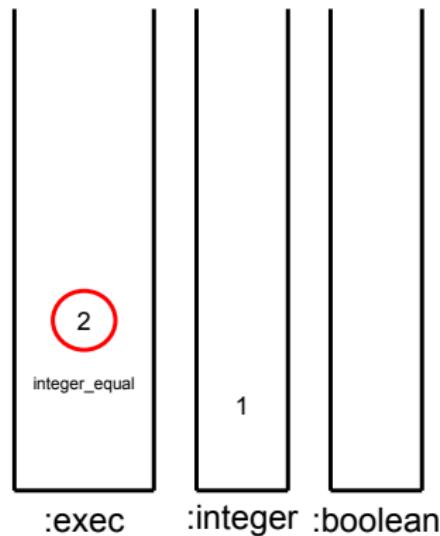


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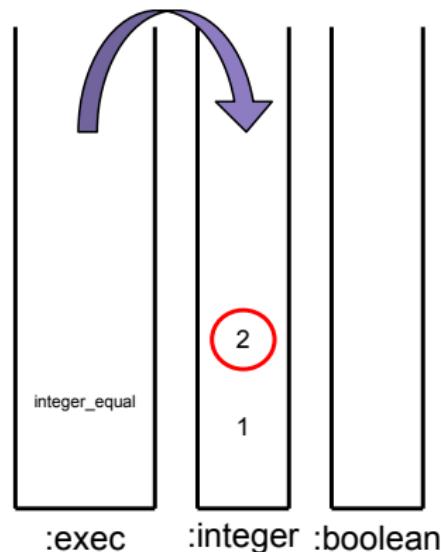


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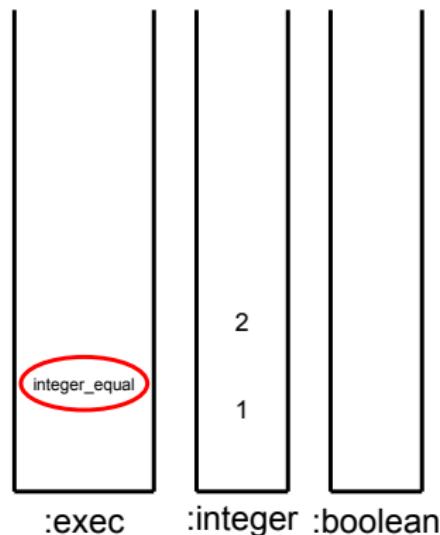


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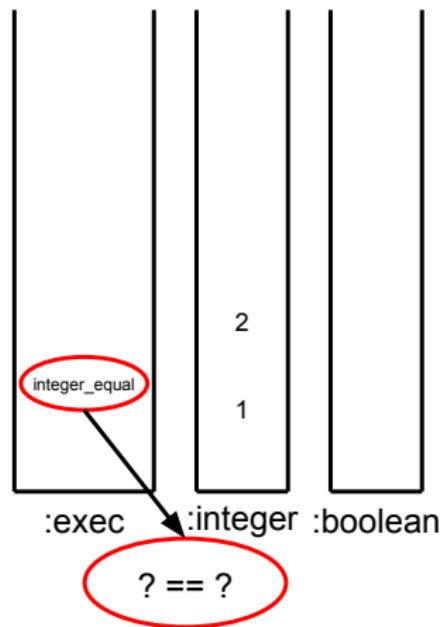


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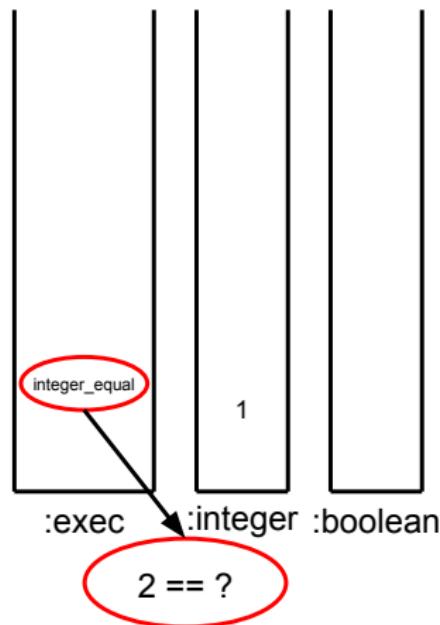


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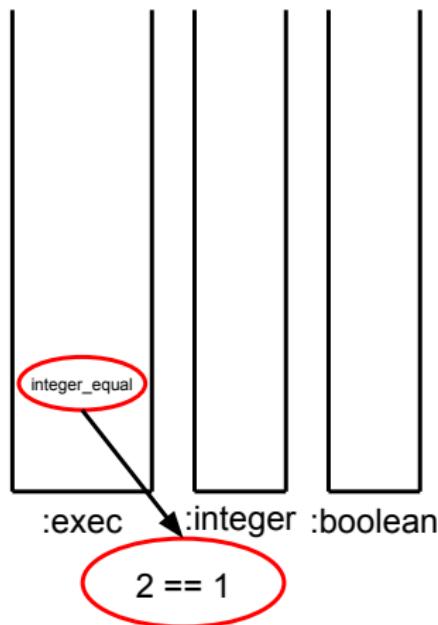


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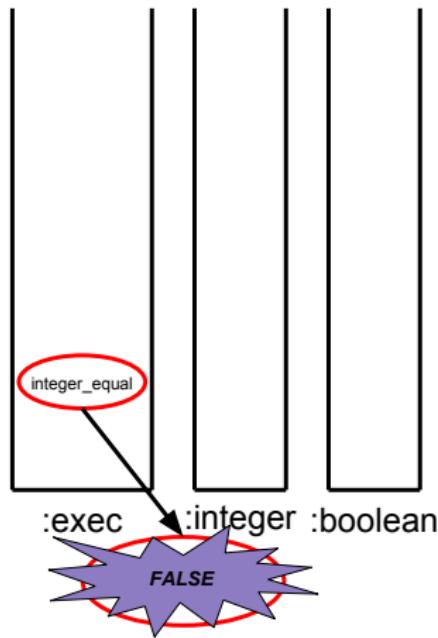


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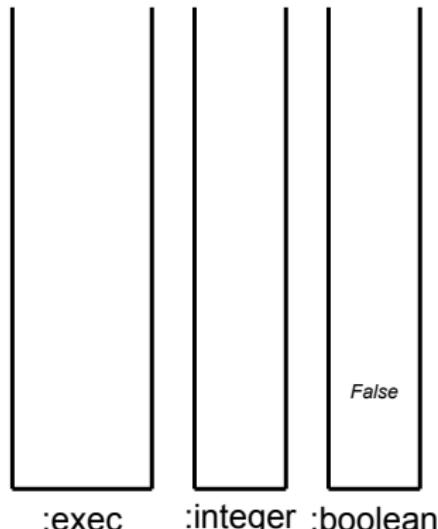


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4 Autoconstruction

- What is it?
- AutoDoG
- Results of AutoDoG

5 Summary

What is Autoconstruction?

- Autoconstruction is a type of genetic programming hyper-heuristic (GPHH)

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- Autoconstruction is a type of genetic programming hyper-heuristic (GPHH)
- In most GPHH, the individual programs are evolving, but everything else is specified by the engineer; in autoconstruction, evolution is evolving as well.
- Programs are responsible for evolving solutions *and* responsible for constructing their offspring.

AutoDoG

- A system designed by Spector et al. [2] that uses autoconstruction to evolve programs.

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- Uses the Push programming language
- Uses Plush, a linear genome format for Push

AutoDoG – reproduction

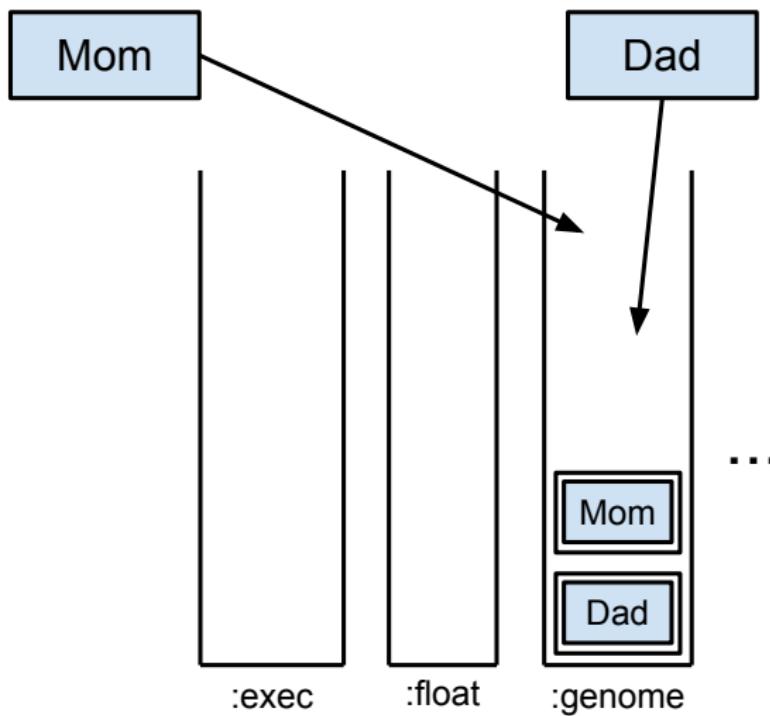
Mom

AutoDoG – reproduction

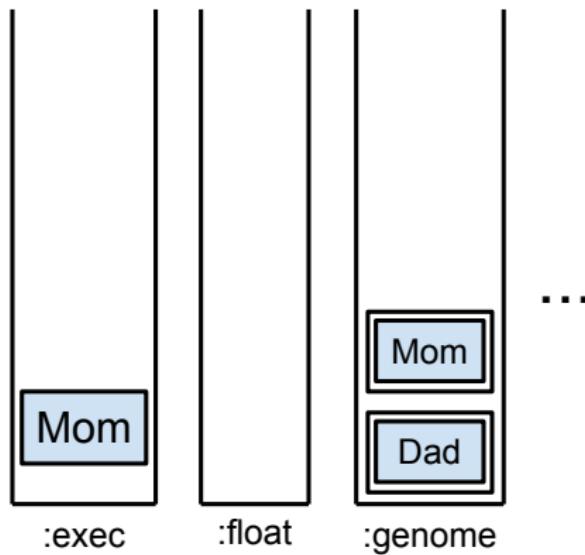
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Dad

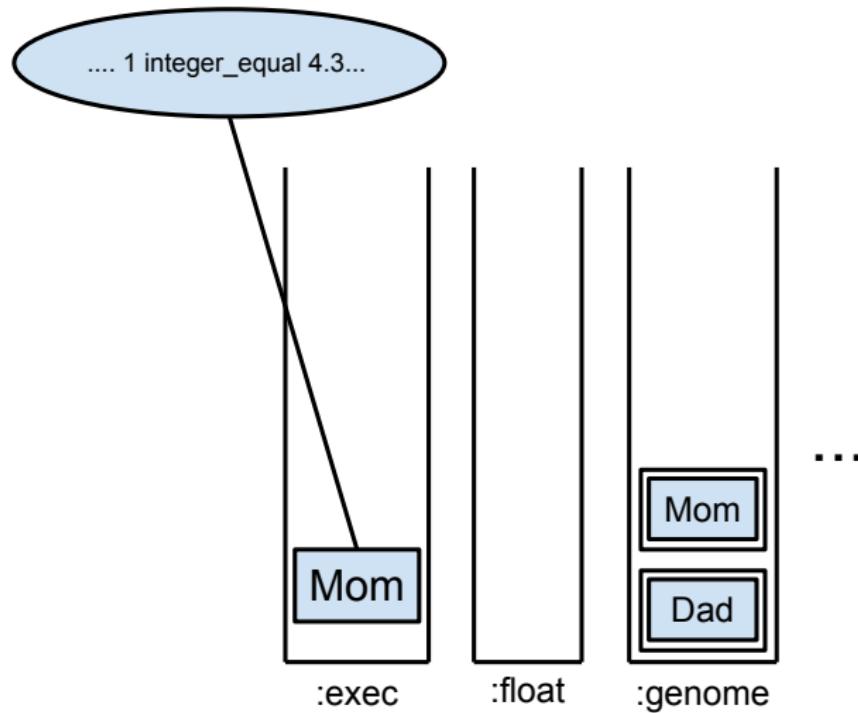
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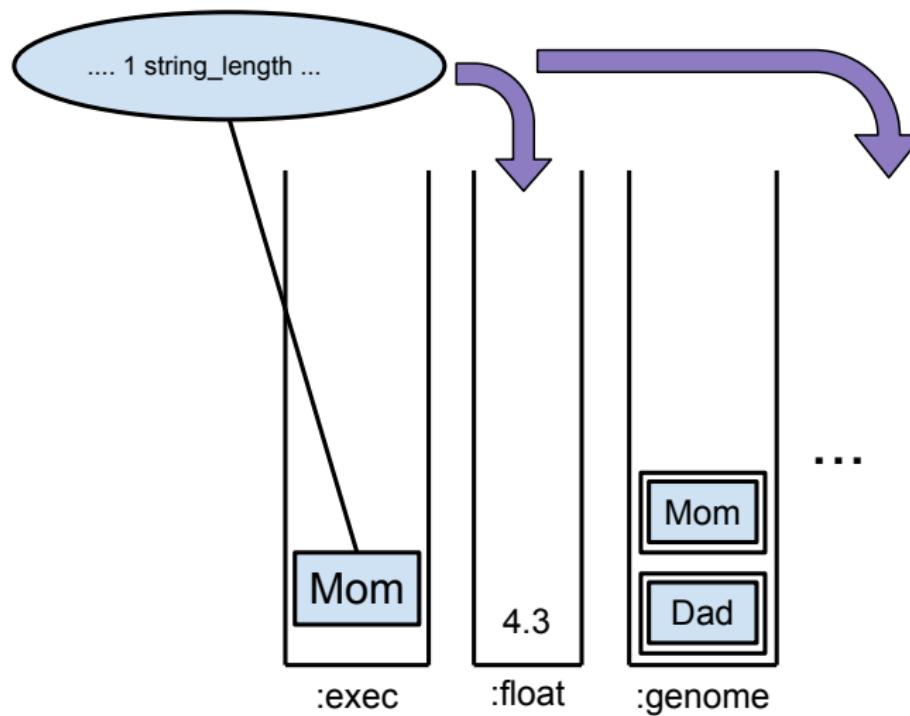
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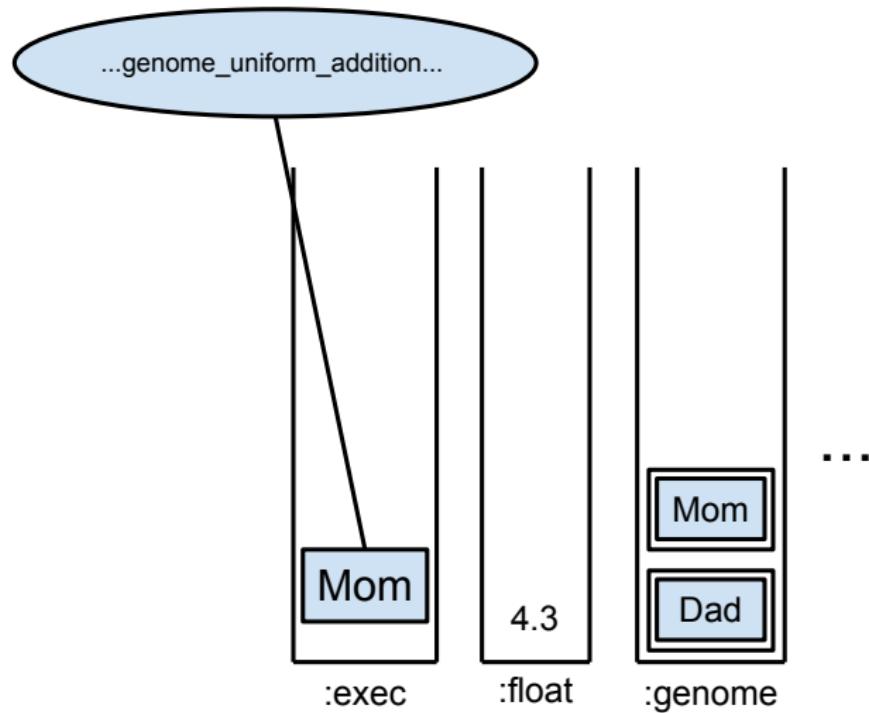
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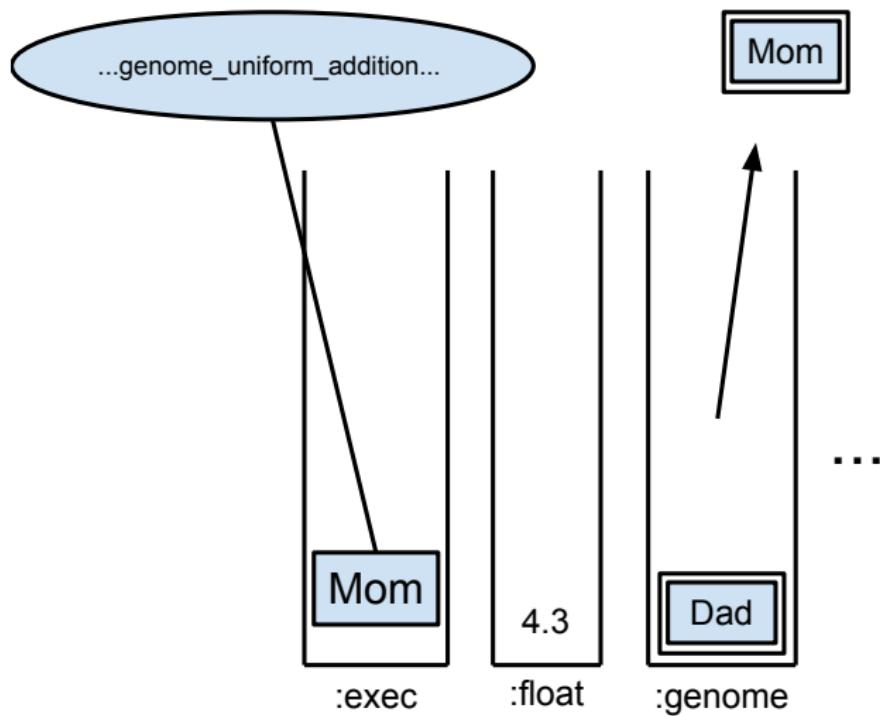
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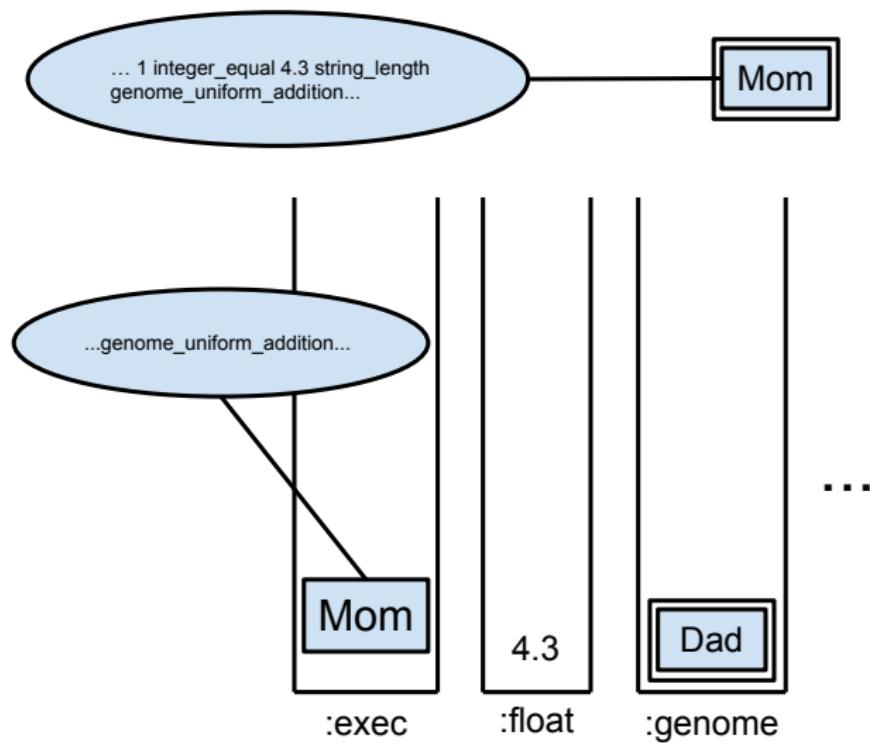
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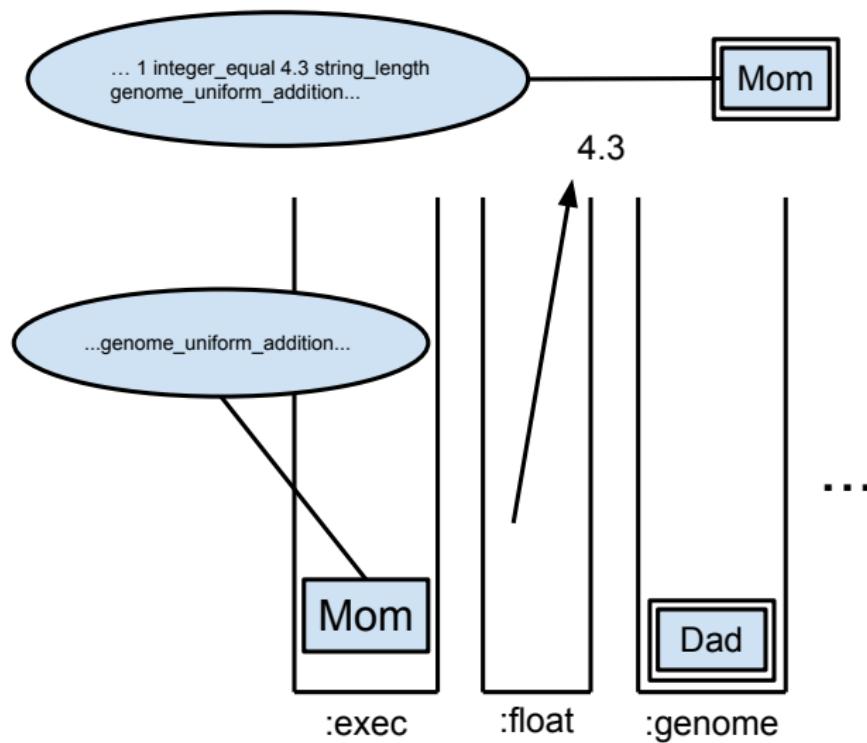
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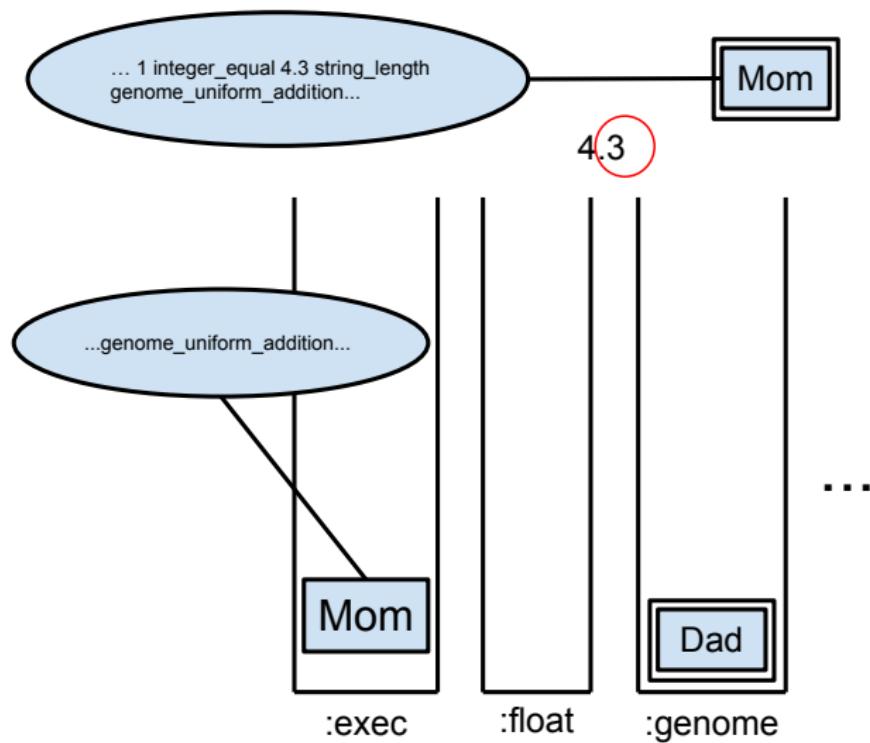
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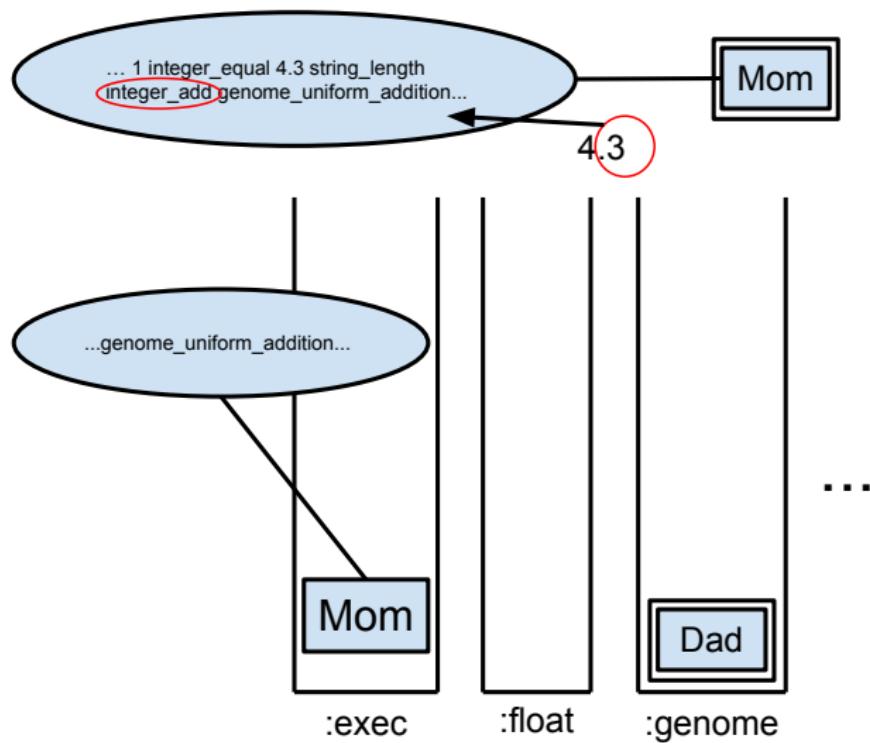
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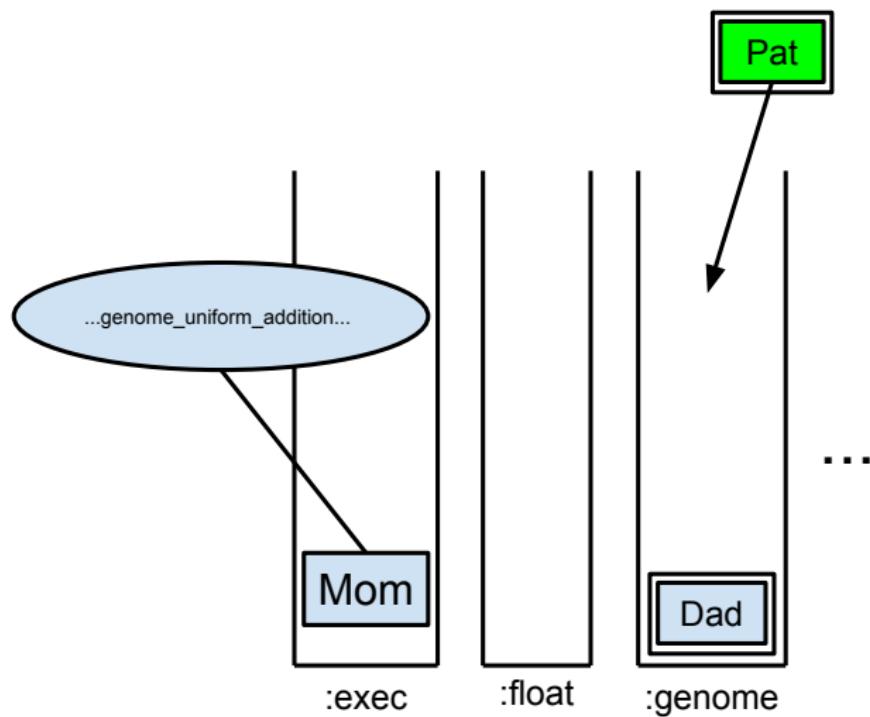
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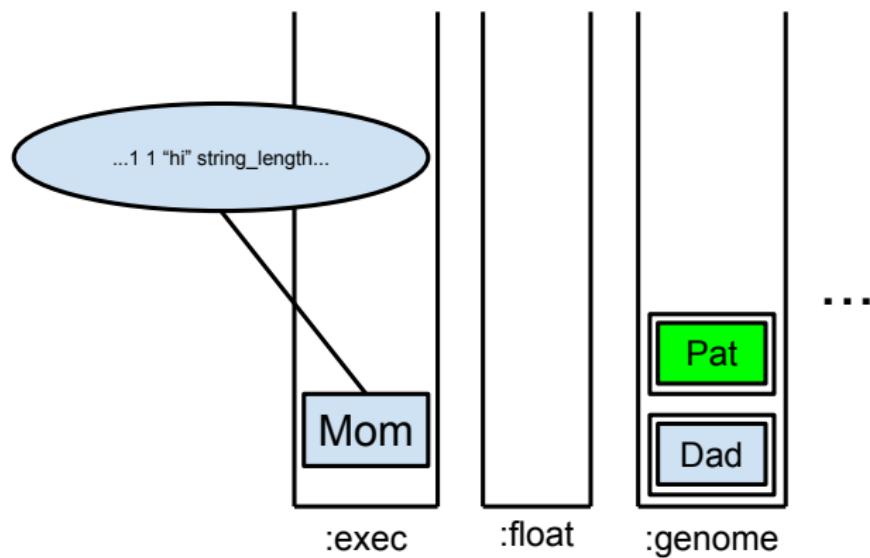
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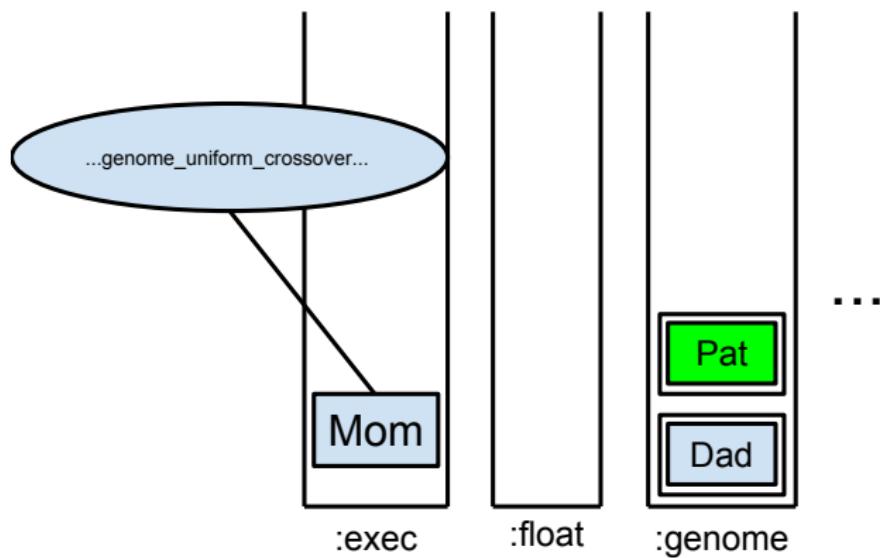
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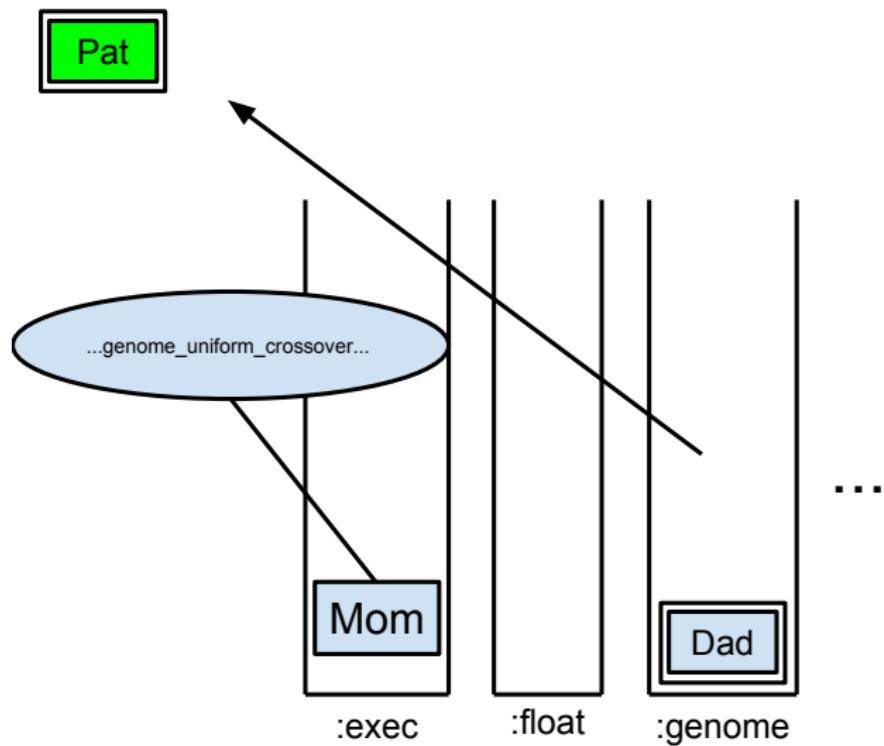
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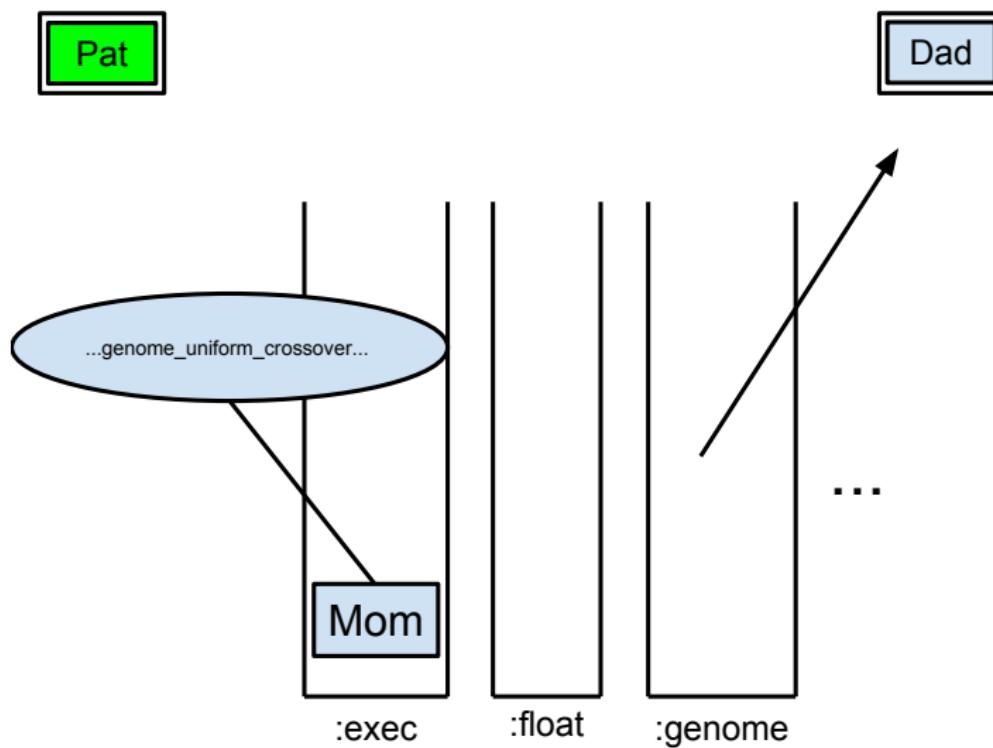
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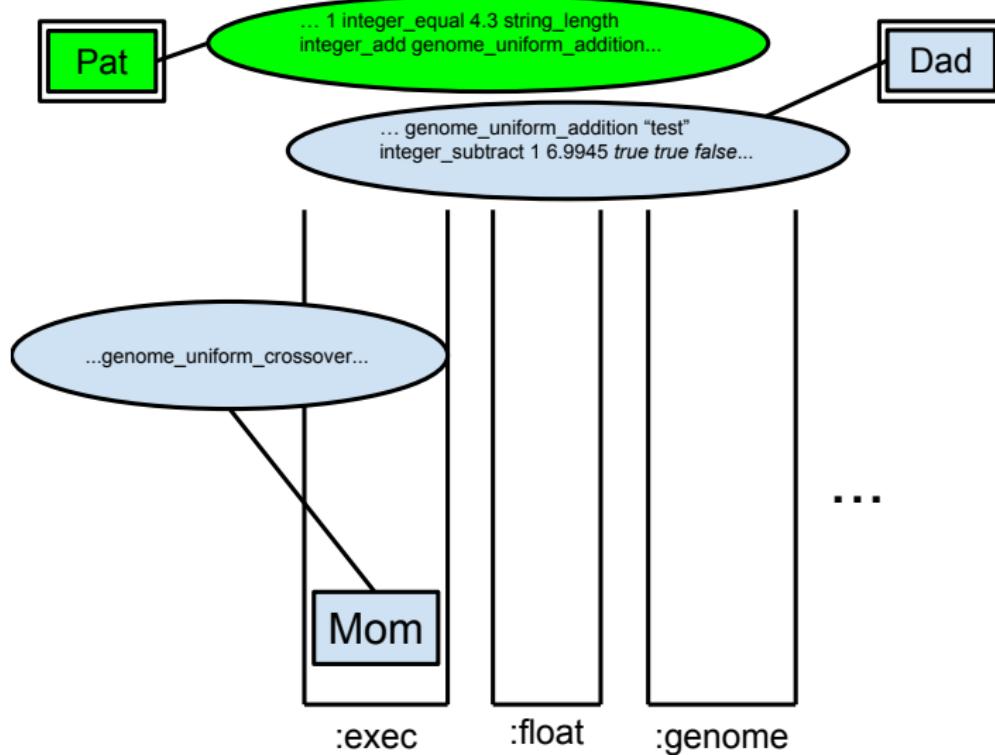
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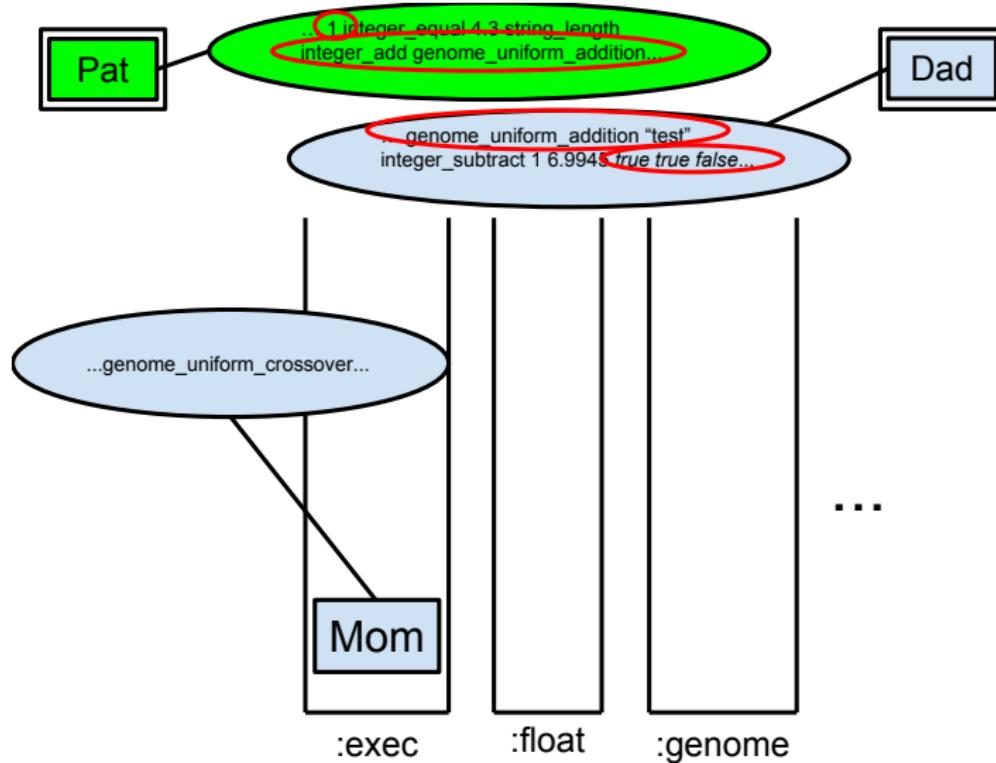
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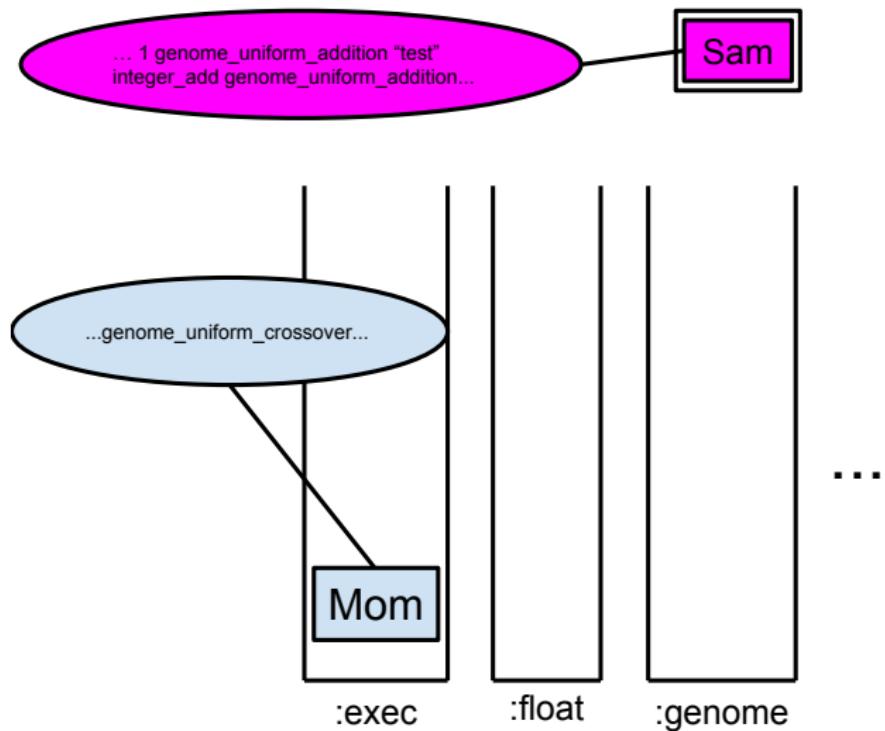
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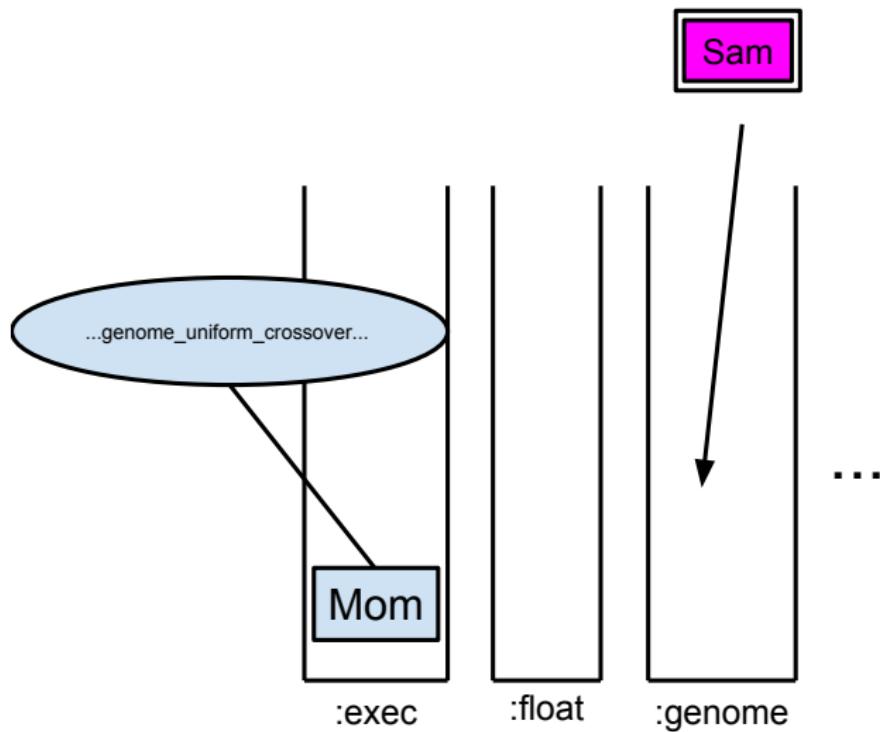
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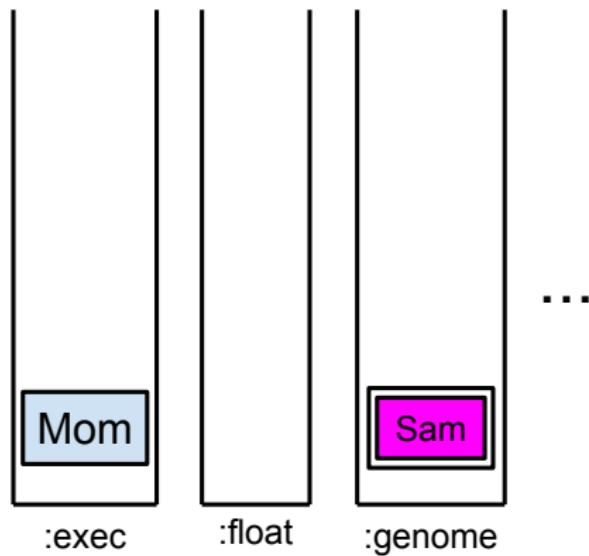
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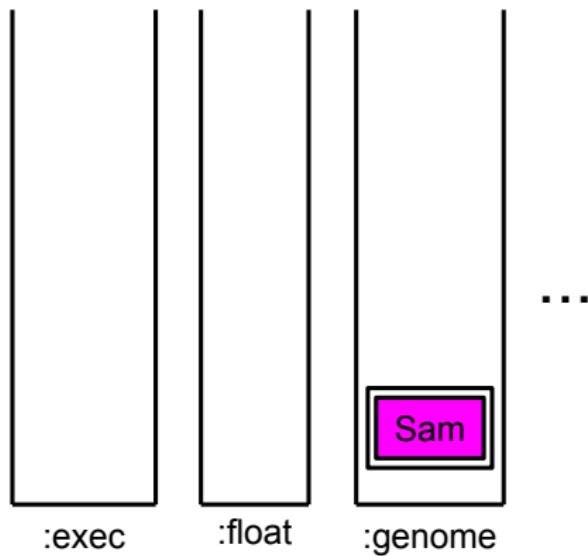
AutoDoG – reproduction



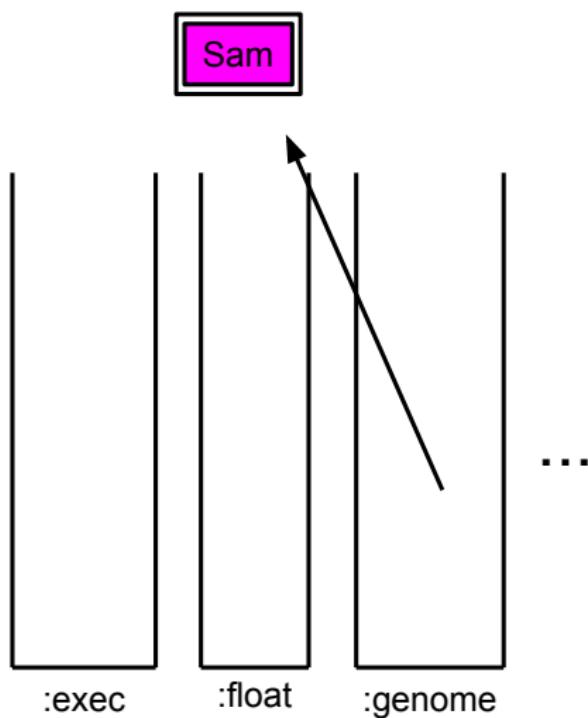
AutoDoG – reproduction



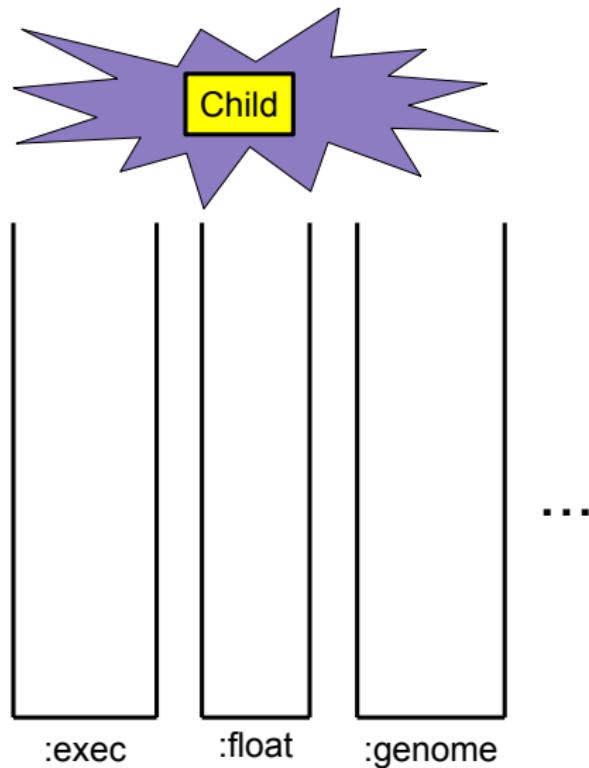
AutoDoG – reproduction



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AutoDoG – reproduction



AutoDoG – reproduction

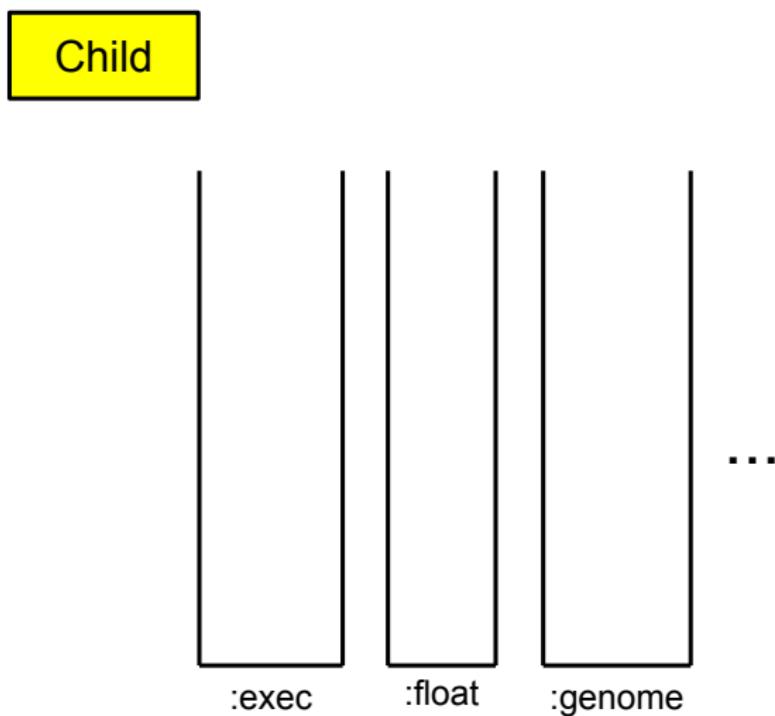
Now Child moves on to the next generation, right?

AutoDoG – reproduction

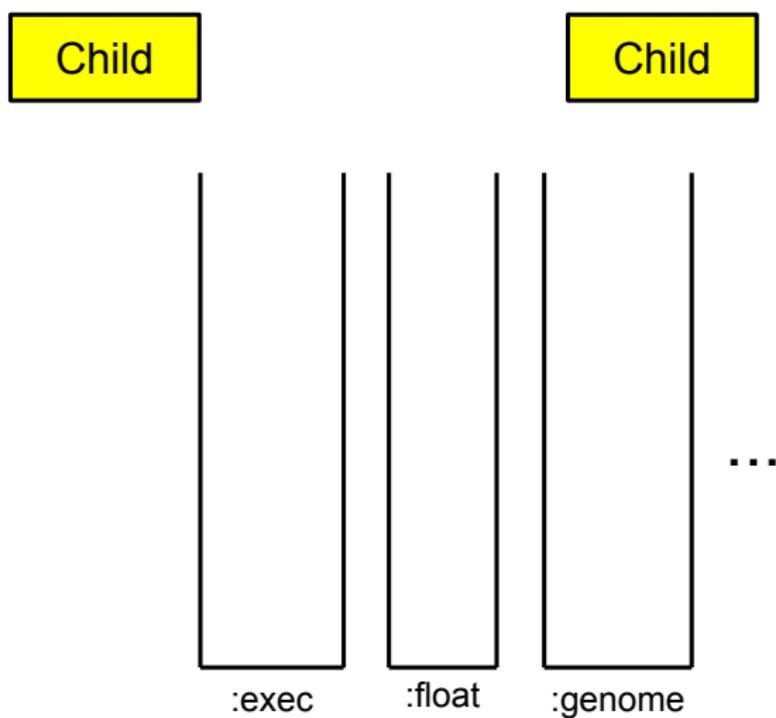
Now Child moves on to the next generation, right?

WRONG!

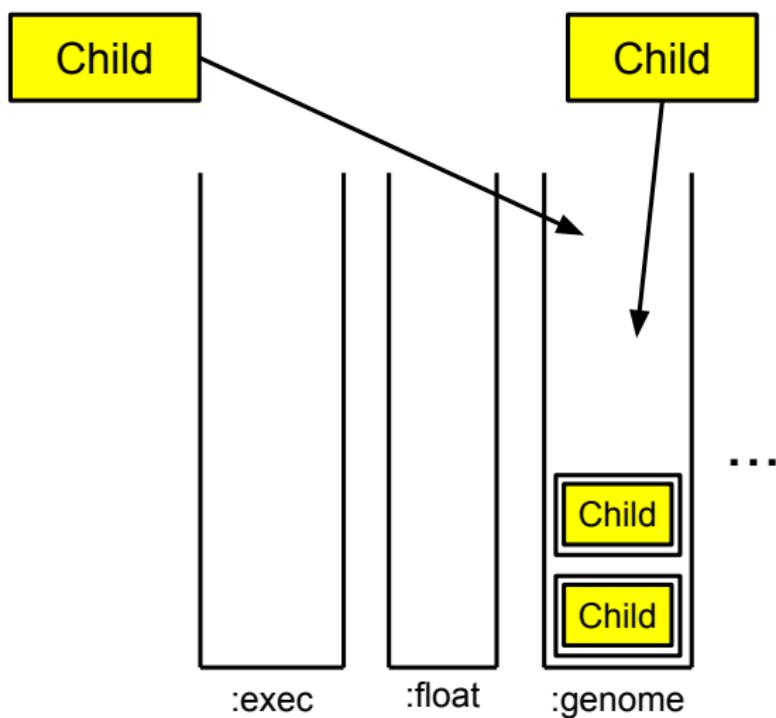
AutoDoG – diversification test



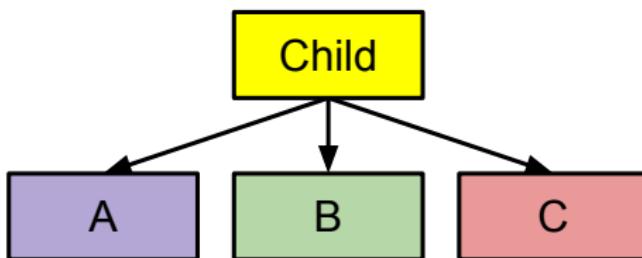
AutoDoG – diversification test



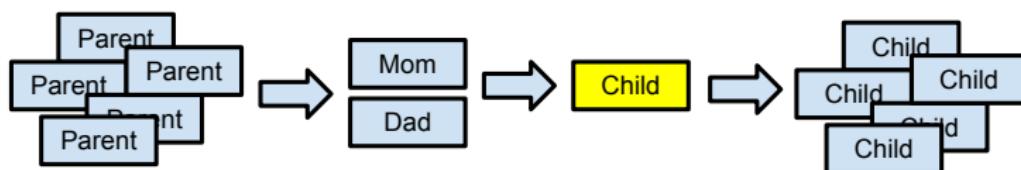
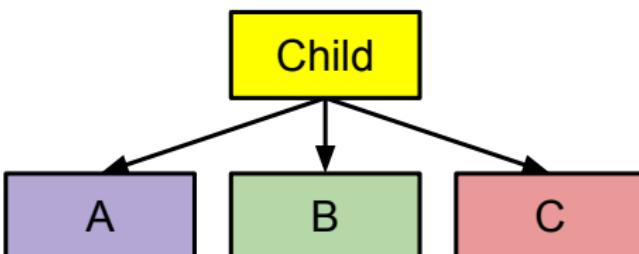
AutoDoG – diversification test



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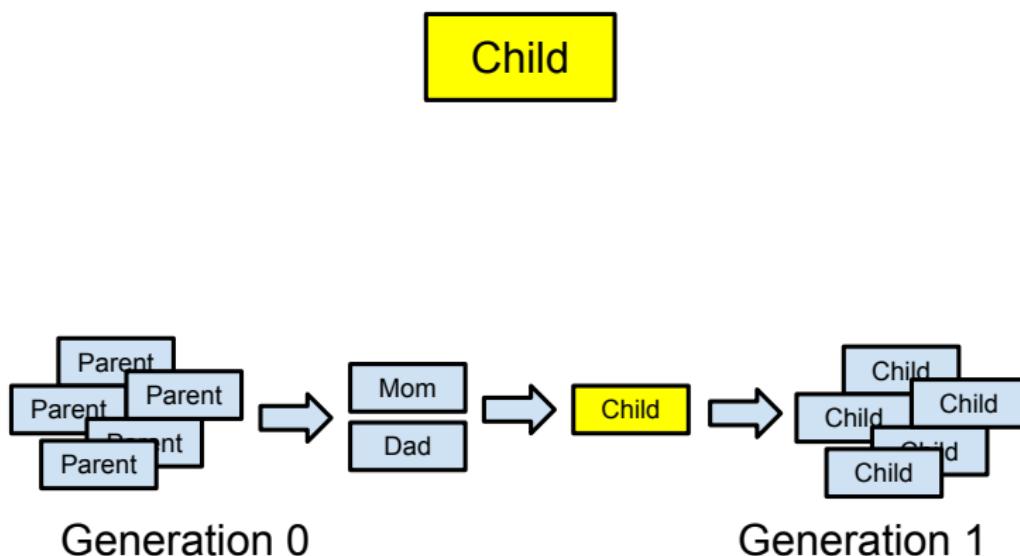
AutoDoG – diversification test



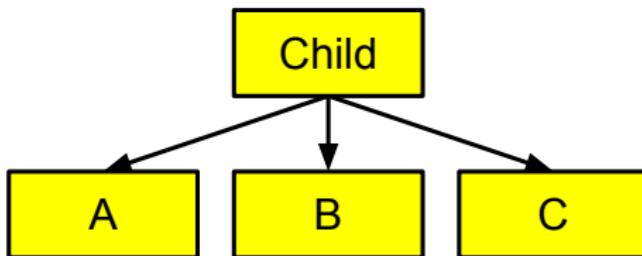
Generation 0

Generation 1

AutoDoG – diversification test



AutoDoG – diversification test



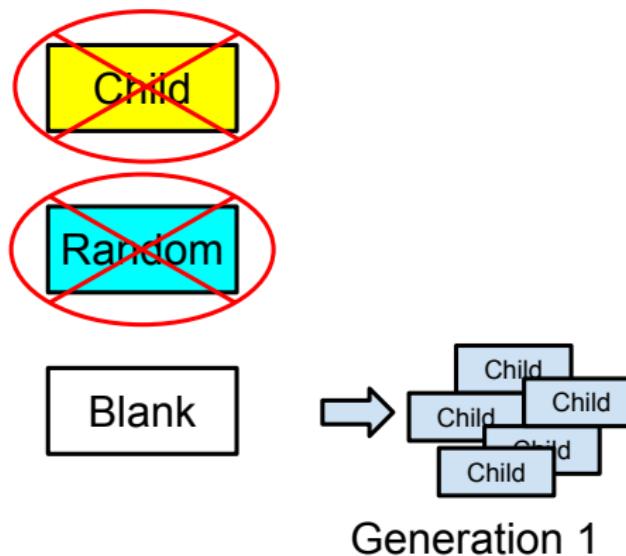
AutoDoG – diversification test



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AutoDoG – diversification test



Results of AutoDoG

AutoDoG has solved Replace Space with New Line (RSWN).

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RSWN: given a string S, print S with all spaces replaced with new lines and return the integer count of all non-whitespace characters.

Results of AutoDoG

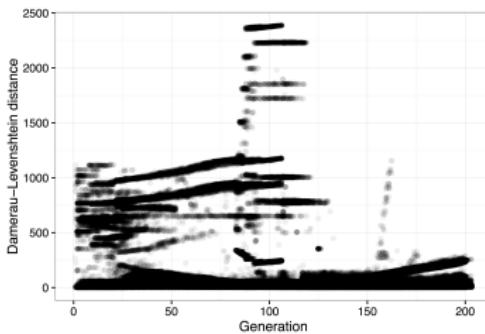
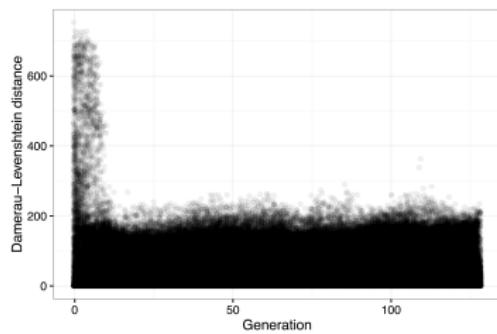
AutoDoG solves RSWN 5–10% of the time, where PushGP solves this problem 50% of the time.

Results of AutoDoG

AutoDoG solves RSWN 5–10% of the time, where PushGP solves this problem 50% of the time.

This is actually really impressive!

Results of AutoDoG



Graphs taken from Spector et al. [2]

Outline

- 1 Background
- 2 Hyper-heuristics
- 3 Genetic Programming Variants
- 4 Autoconstruction
- 5 Summary

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Summary

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- There are many types of GP variants, and the variant chosen may affect the success of the hyper-heuristic
- Autoconstruction is a type of GPHH
- AutoDoG is a newer autoconstructive system that uses stack-based GP and has had recent success in the field of automating algorithm design
- AutoDoG/autoconstruction is special because evolution is evolving

Summary

This may drastically change the way we program in the future!

Acknowledgments

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Thanks for coming!

References

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-  [L. Spector, N. F. McPhee, T. Helmuth, M. M. Casale, and
J. Oks.
Evolution Evolves with Autoconstruction.
In T. Friedrich, *et al*, editors, *GECCO '16*, pages
1349–1356, Denver, Colorado, USA 2016.](#)

See my paper for additional references.

Questions?

If your question was not answered during the presentation today, feel free to contact me: <brow3924@morris.umn.edu>