

# Formula sheet for testing materials

Izaak van Dongen

October 17, 2017

## Contents

<b>1</b>	<b>Material properties</b>	<b>1</b>
1.1	Strength . . . . .	1
1.2	Young's Modulus . . . . .	1
<b>2</b>	<b>Formulas</b>	<b>2</b>
2.1	Stress . . . . .	2
2.2	Strain . . . . .	2
2.3	Area of a circle . . . . .	2

## 1 Material properties

### 1.1 Strength

Strength is actually a stress value. Strength is the stress at which a material "fails".

- The "yield strength" of a material is when it starts to plastically deform.
- The "breaking strength" of a material is when it actually breaks.

### 1.2 Young's Modulus

Young's modulus is an indication of the stiffness of a material (how much strain is produced by a stress while deforming elastically). It is given by stress over strain, and denoted as  $E$ :

$$E = \frac{\sigma}{\epsilon} \quad (1)$$

As the units of  $\sigma$  are  $Pa$  and  $\epsilon$  is dimensionless, we can conclude that  $E$  has units  $Pa$ .

Also, as we know formulas for both  $\sigma$  and  $\epsilon$ , we can substitute in:

$$\begin{aligned} E &= \frac{\sigma}{\epsilon} \\ &= \frac{\frac{F}{A}}{\frac{x}{l}} \\ &= \frac{Fl}{Ax} \end{aligned}$$

## 2 Formulas

### 2.1 Stress

The stress is defined as force applied divided by cross-sectional area and denoted as  $\sigma$ :

$$\sigma = \frac{F}{A} \quad (2)$$

Hence, stress is measured in  $Nm^{-2}$ , which is called *Pa* (scals).

### 2.2 Strain

Strain is a measure of the deformation of a material. It denoted as  $\epsilon$  and given by extension over original length:

$$\epsilon = \frac{x}{l_0} \quad (3)$$

As the units of both  $x$  and  $l_0$  are  $m$ ,

$$\begin{aligned} \text{units} &= \frac{m}{m} \\ &= \text{dimensionless} \end{aligned}$$

### 2.3 Area of a circle

This is given by

$$A_{circle} = \pi r^2 \quad (4)$$

We can also make some substitutions, as we know

$$\begin{aligned} r &= \frac{d}{2} \\ \Rightarrow A_{circle} &= \frac{\pi d^2}{4} \end{aligned}$$