# Running a Discussion Section

Eric Lybrand, Jeff Rabin, Jacqueline Warren



### Announcements

- ► Teaching statement due on Gradescope tonight by 11pm.
- Reserve a homework box for your course if you have not already. Have at least two discussion sections to a box when possible.
- ► Have you contacted your course's instructor? What about the grader?
- Eric and Jacqueline will start observations next week.

### Overview

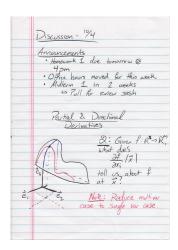
Structuring a Discussion Section: Eric's & Jacqueline's Advice Before Discussion Begins During Discussion Section How to End Discussion Section

Prof. Rabin's Tips of the Trade

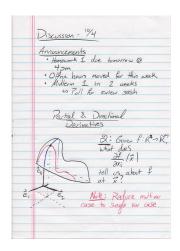
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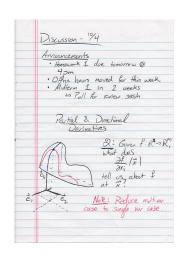
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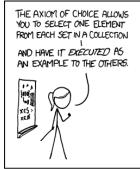


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  - Day of: Ask students where they want practice.



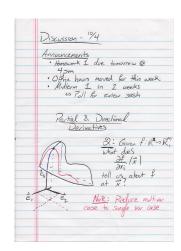
### What to do 10 Minutes Before

- Show up 10 minutes early.
- Break the ice.
  - "How was your weekend?"
  - Appropriate joke/pun/story.
  - What problems do you want to work on?
- Write up announcements, office hours, email.
- ► Relax, smile, take a deep breath.

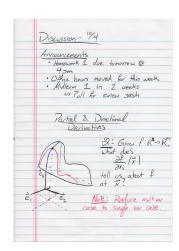


MY MATH TEACHER WAS A BIG BELIEVER IN PROOF BY INTIMIDATION.

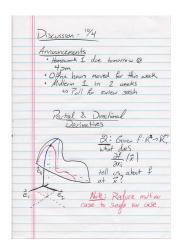
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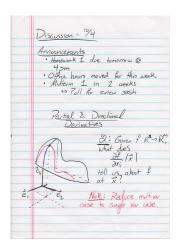
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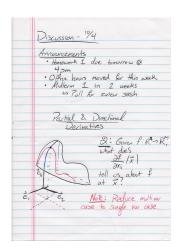
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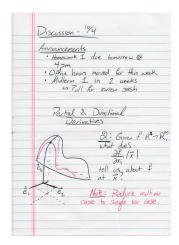
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  - "What are we actually doing?"
  - Form a narrative. Add to it every week.
  - Draw (good) pictures.
- Ask questions that test understanding.
- Definitions vs intuition.



Having a basic roadmap to refer to helps contextualize material for students.

$$\begin{bmatrix} \cos 90^{\circ} & \sin 90^{\circ} \\ -\sin 90^{\circ} & \cos 90^{\circ} \end{bmatrix} \begin{bmatrix} \alpha_{1} \\ \alpha_{2} \end{bmatrix} = \underbrace{500}$$

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Figure: xkcd.com

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- ▶ **Geometry:** What do solutions to Ax = b look like? How do we find them? How many? What is their structure?
- ▶ **Algebra:** What properties of matrix A as a function inform us about solutions to Ax = b?

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- ▶ Let students guide the discussion after the recap.
- Do not be frustrated if you feel students are moving slowly.
  - ► Eric's Opinion: Better that students understand the basics well than rush through all the material.
- Carefully walk through how to interpret a problem (see Dr. Rabin's upcoming slides).
- Some problems only need to be set up. Do not be afraid to delegate the details to the students if you are very sure they can understand them. This saves a lot of time.
- ▶ Mind your board work. Keep your eye on the clock.

### Boardwork

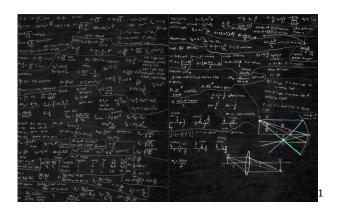


Figure: An example of poor boardwork.

<sup>&</sup>lt;sup>1</sup>https://taxfoundation.org/tax-foundation-s-model-results-context/

### Boardwork

#### Good Boardwork

- ► Neat writing.
- Board is properly partitioned.
- Whole board is being used.
- Not too much, not too little writing.

#### **Bad Boardwork**

- Erasing too soon.
- ► Not labelling problems.
- Standing in front of what was most recently written.
- ► Poorly spaced work.

# Finishing on Time

- ► Do not keep students long past the when discussion is over. Students do not appreciate this.
- ▶ Not every question will be answered during discussion.
- ▶ If a discussion is threatening to run long, end with a carefully given hint or a well-posed question.
- ▶ Encourage students to come to office hours.

# Prof. Rabin's Three Rules of Teaching

- 1. Everything should be made as simple as possible, but not simpler than that. (–Einstein?)
- 2. Be enthusiastic about what you are teaching. If you aren't, why would your students be?
- 3. Hear what you say, see what you write, from students' viewpoint. Would I understand it without the background I have now? What am I assuming without explaining it? Terminology, strategies, context. Use your own undergraduate experience to help you.

# Problem Solving, Phase 1: Understanding the Problem

- ▶ What do the words in the problem mean?
- ▶ What is the situation described? Can I draw a picture?
- What is given and what must be found/proved/done?
- ▶ How will I tell when I have found it?
- Do I know an example?
- Do I know a relevant theorem?
- What is my conjecture/prediction of the answer?

# Problem-free Activity

- Students may not be engaged with a mathematical problem at all, but rather a social one.
- "What do they want me to do?", instead of "what does this mean?"
- They may perform rote procedures in response to perceived triggers.
- ► "The problem" becomes guessing what is expected, or forcing the situation to fit a known template.

# Problem Solving, Phase N+1: Reflection

- ▶ How would I recognize such a problem on an exam?
- Why was this problem assigned?
- ► Can the answer be checked? What does it mean? Does it make sense? Could I have anticipated it?
- How does the answer change if parameters or assumptions vary?
- Are there alternate solution methods?
- What patterns or new questions does the solution suggest?

### TA Questions

- "What's the next step?" may not be ideal.
- What does this mean?
- ▶ How do we know this?
- What does this computation prove? (Necessary or sufficient condition? For all, or there exists?)
- ▶ Is there another way? What would happen if we did this?
- What is the role of this concept (e.g. continuity) in the solution?
- How can we check the answer?
- ▶ What if we modify the problem by...?
- What was confusing, and how can we avoid this confusion next time?