

Calculation of $\alpha_{\mu}^{(\pi^+\pi^-, LO)}$ with the use of a phenomenological dispersive method

Master's Internship

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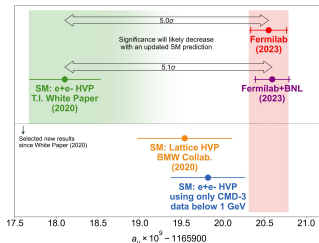
October 31, 2024

- ➊ Motivation
- ➋ Dispersive method
- ➌ Phenomenological model
- ➍ Fits & Results
- ➎ Branching ratios
- ➏ Summary & Conclusions
- ➐ References

Motivation

1: Motivation

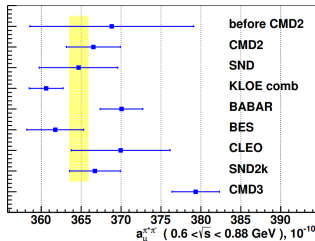
- Tension between experiment - SM theory
- Improve errors for α_μ^{had} -result
 \hookrightarrow HVP-term: $\alpha_\mu^{\pi\pi, LO}$ (~ 60%)
- In SM theory: higher CMD3 result



[Aguillard D.P. et al., 2023]

Primary topic:

- Use standard dispersion method for $\alpha_\mu^{\pi\pi, LO}$ calculation
- Use of phenomenological $F_\pi^V(s)$ functions to test/reproduce this deviation
- Comparison of BaBar - CMD3 data results
- Use fit parameters for $\mathcal{B}(\omega \rightarrow \pi\pi)$ and $\mathcal{B}(\phi \rightarrow \pi\pi)$ calculation



[Ignatov F.V. et al., 2023]

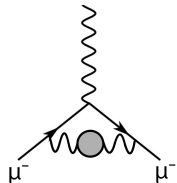
Dispersive method

2.1: Dispersive method for α_μ^{HVP}

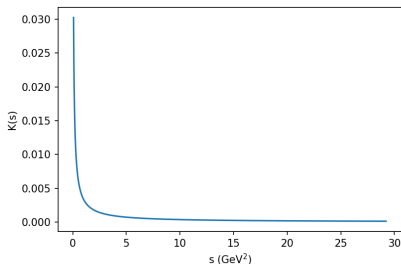
- Use of cross section data for calculation [De Troconiz J.F. & Ynduráin F.J., 2002]:

(LO) HVP Anomalous magnetic moment contribution

$$\alpha_\mu^{\text{HVP,LO}} = \frac{1}{4\pi^3} \int_{s_{\text{th}}}^{\infty} ds \sigma(e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons}) \cdot K(s)$$



→ Analytical kernel function $K(s)$:

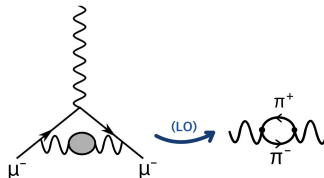


$$K(s) = \frac{(1+x^2)(1+x)^2}{x^2} \left(\log(1+x) - x + \frac{x^2}{2} \right) + \frac{x^2}{2} (2-x^2) + \frac{1+x}{1-x} x^2 \log(x)$$

$$x = \frac{1 - \sigma_\mu(s)}{1 + \sigma_\mu(s)} \quad , \quad \sigma_\mu(s) = \sqrt{1 - \frac{4m_\mu^2}{s}}$$

- With respect to the 2-pion vector form factor (VFF):

$$\alpha_{\mu}^{\pi\pi, LO} = \frac{\alpha^2}{12\pi^2} \int_{4M_{\pi}^2}^{\infty} ds \frac{\beta_{\pi}^3 \cdot K(s) \cdot |F_{\pi}^V(s)|^2}{s}$$



→ Pion velocity : $\beta_{\pi} = \sqrt{1 - 4 \frac{m_{\pi}^2}{s}}$, α : fine-structure constant [\[Review of Particle Physics, 2022\]](#)

- Due to the analytic structure of $F_{\pi}^V(s) \rightarrow$ Dispersion representation of VFF

$$F_{\pi}^V(s) = \frac{1}{\pi} \int_{4M_{\pi}^2}^{\infty} \frac{ds'}{s' - s} \cdot \text{Im} F_{\pi}^V(s')$$

2.2: Omnès function

- Solution constructed analytically → Consider special solution: Omnès function $\Omega(s)$

$$F_{\pi}^V(s) = \Omega(s) \quad \text{with} \quad \Omega(0) = 1$$

Then:

$$\Omega(s + i\epsilon) = |\Omega(s)| e^{i\delta(s)}$$

$$\Omega(s - i\epsilon) = |\Omega(s)| e^{-i\delta(s)}$$

$$\Rightarrow \text{disc log } \Omega(s) = \log \Omega(s + i\epsilon) - \log \Omega(s - i\epsilon) = 2i\delta(s)$$

for $\delta(s \rightarrow \infty) \rightarrow \text{constant}$, the [once-subtracted dispersion relation](#) for $\log \Omega(s)$:

$$\log \Omega(s) = \log \Omega(0) + \frac{s}{\pi} \int_{4M_{\pi}^2}^{\infty} ds' \frac{\delta(s')}{s'(s' - s)} \Rightarrow \Omega(s) = \exp \left\{ \frac{s}{\pi} \int_{4M_{\pi}^2}^{\infty} ds' \frac{\delta(s')}{s'(s' - s)} \right\}$$

$$\Omega(s) = \exp \left\{ \frac{s}{\pi} \int_{4M_{\pi}^2}^{\infty} dx \frac{\delta(x)}{x(x - s)} \right\} = \exp \left\{ \frac{s}{\pi} \int_{4M_{\pi}^2}^{\infty} dx \frac{\delta(x) - \delta(s)}{x(x - s)} + i\delta(s) - \frac{\delta(s)}{\pi} \log \left(\frac{4M_{\pi}^2 - s}{4M_{\pi}^2} \right) \right\}$$

where $\delta(s)$: the (elastic) phase shift

Phenomenological model

3.1: The 2-pion vector form factor

- In this project:

$$F_{\pi}^V(s) = P(s) \cdot \Omega(s)$$

for the “polynomial” $P(s)$:¹

- **FF1-type:** $F_{\pi}^V(s) = \left(1 + \alpha \cdot s + \frac{\epsilon_{\rho\omega} \cdot s}{M_{\omega}^2 - s - iM_{\omega}\Gamma_{\omega}^{tot}} \right) \cdot \Omega(s)$

¹ **marked** are the fit parameters in each case

3.1: The 2-pion vector form factor

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- **FF3-type:** $F_{\pi}^V(s) = \left(1 + \alpha \cdot s + \frac{\epsilon_{\rho\omega} \cdot s}{M_{\omega}^2 - s - iM_{\omega}\Gamma_{\omega}^{tot}} + \frac{\epsilon_{\phi} \cdot s}{M_{\phi}^2 - s - iM_{\phi}\Gamma_{\phi}^{tot}} \right) \cdot \Omega(s)$

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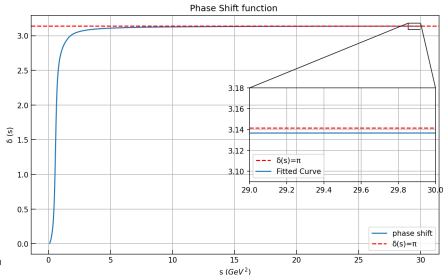
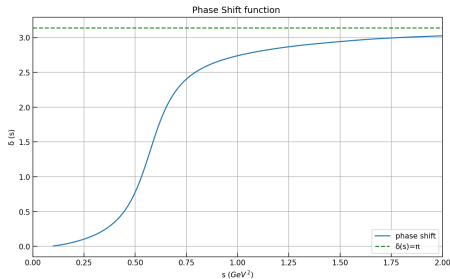
- **FF4-type:**
$$F_{\pi}^V(s) = \left(1 + \alpha \cdot s + \frac{\epsilon_{\rho\omega} \cdot s}{M_{\omega}^2 - s - iM_{\omega}\Gamma_{\omega}^{tot}} + \frac{\epsilon_{\phi} \cdot s}{M_{\phi}^2 - s - iM_{\phi}\Gamma_{\phi}^{tot}} \right) \cdot \Omega(s)$$

¹ **marked** are the fit parameters in each case

3.2: Phase shift function $\delta(s)$

$$\delta(s) = \begin{cases} \text{Interpolated function from isospin 1 P-wave} \\ \text{phase shift values (Bern)} & , \text{ for } 4M_\pi^2 \leq s \leq s_0 \\ \pi + (\delta(s_0) - \pi) \left(\frac{\lambda_0^2 + s_0}{\lambda_0^2 + s} \right) & , \text{ for } s \geq s_0 \end{cases}$$

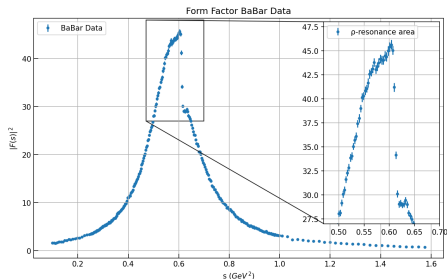
with $s_0 = 25 \text{ (GeV)}^2$ and $\lambda_0 = \text{const.}$



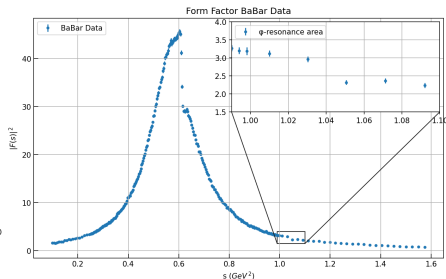
Fits & Results

4.1: BaBar data

- BaBar data from measurements of $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ cross section with the Initial-State Radiation (IRS) method [Lees J.P. et al., 2012]



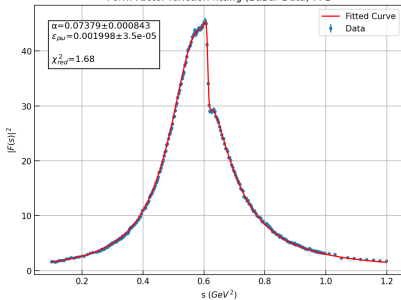
BaBar data with zoom in the behaviour exhibited due to the ω, ρ -mixing.



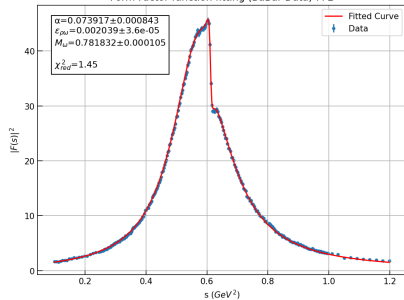
BaBar data with zoom in the behaviour exhibited due to the ϕ -resonance.

4.2: BaBar fits

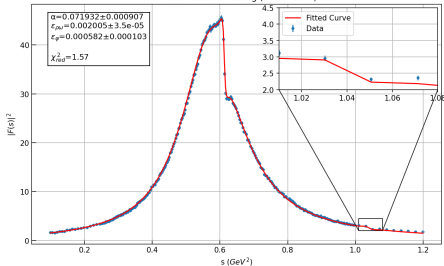
Form Factor function fitting (BaBar Data)-FF1



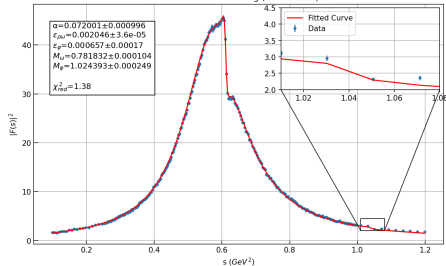
Form Factor function fitting (BaBar Data)-FF2



Form Factor function fitting (BaBar Data)-FF3

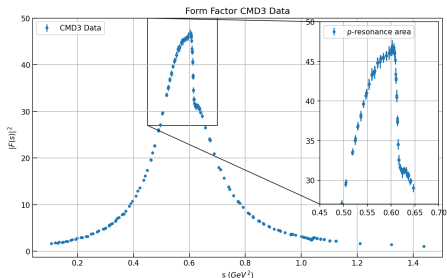


Form Factor function fitting (BaBar Data)-FF4

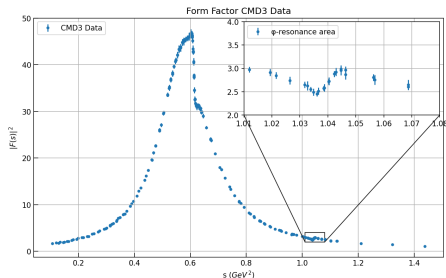


4.3: CMD3 data

- CMD3 data from measurements of $e^+e^- \rightarrow \pi^+\pi^-$ cross section with energy-scan measurement method [Ignatov F.V. et al., 2023]



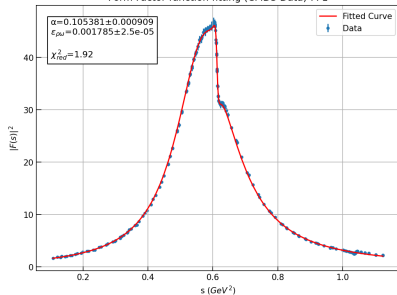
CMD3 data with zoom in the behaviour exhibited due to the ω , ρ -mixing.



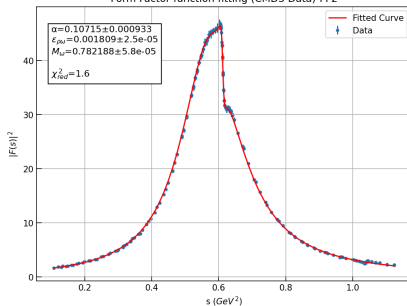
CMD3 data with zoom in the behaviour exhibited due to the ϕ -resonance.

4.4: CMD3 fits

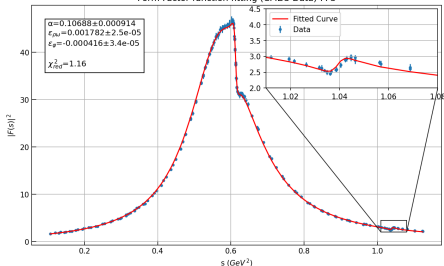
Form Factor function fitting (CMD3 Data)-FF1



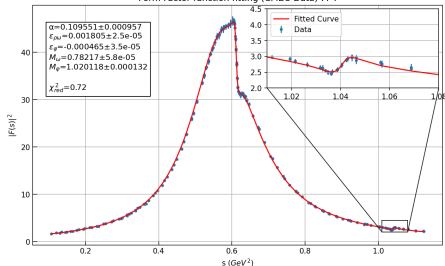
Form Factor function fitting (CMD3 Data)-FF2



Form Factor function fitting (CMD3 Data)-FF3



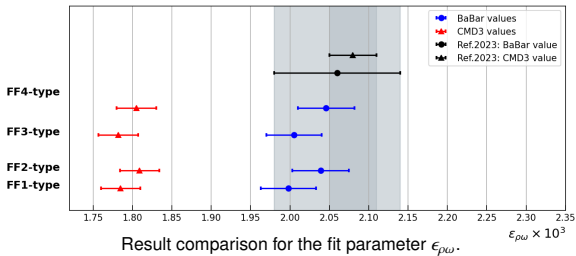
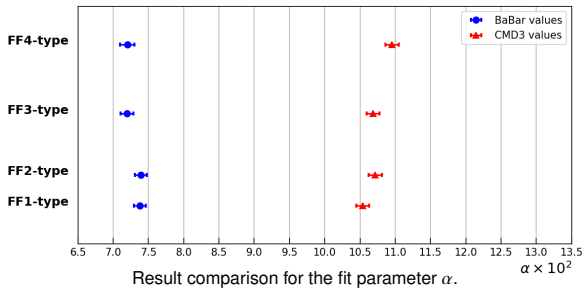
Form Factor function fitting (CMD3 Data)-FF4



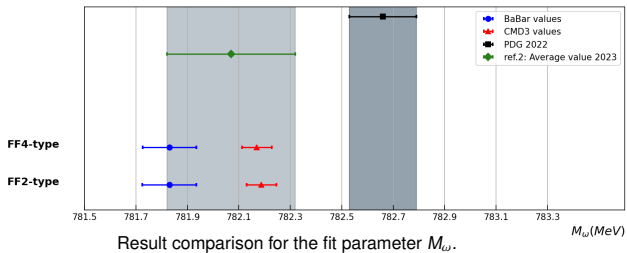
4.5: Results for fit parameters

$F_{\pi}^V(s)$ type	Data set ($\leq 1.2\text{GeV}^2$)	$\alpha \times 10^{-2}$	$\epsilon_{\rho\omega} \times 10^{-4}$	$M_{\omega}(\text{MeV})$	$\epsilon_{\phi} \times 10^{-4}$	$M_{\phi}(\text{MeV})$	χ_{red}^2
FF1-type	BaBar	7.38 (± 0.08)	19.98 (± 0.35)	-	-	-	1.68
	CMD3	10.54 (± 0.09)	17.85 (± 0.25)	-	-	-	1.92
FF2-type	BaBar	7.39 (± 0.08)	20.39 (± 0.36)	781.833 (± 0.105)	-	-	1.45
	CMD3	10.72 (± 0.09)	18.09 (± 0.25)	782.188 (± 0.058)	-	-	1.60
FF3-type	BaBar	7.19 (± 0.09)	20.05 (± 0.35)	-	5.82 (± 1.03)	-	1.57
	CMD3	10.69 (± 0.09)	17.82 (± 0.25)	-	-4.16 (± 0.34)	-	1.16
FF4-type	BaBar	7.2 (± 0.10)	20.46 (± 0.36)	781.832 (± 0.104)	6.57 (± 1.70)	1024.393 (± 0.249)	1.38
	CMD3	10.97 (± 0.10)	18.05 (± 0.25)	782.168 (± 0.058)	4.68 (± 0.35)	1020.118 (± 0.131)	0.76

Results for the fit parameters for each form factor function and data set

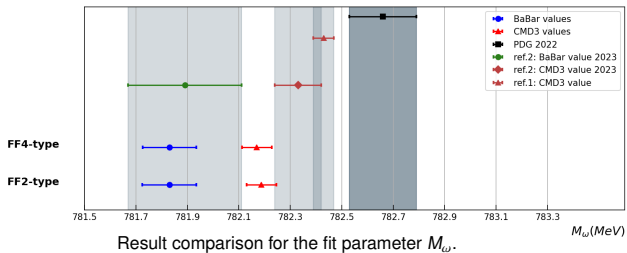


Ref.2023 BaBar, CMD3
values: [Colangelo G.,
Hoferichter M. & Stofer
P., 2023]



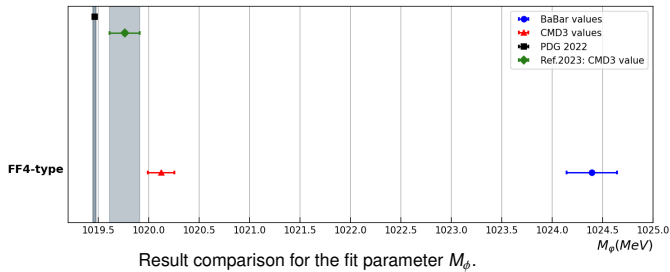
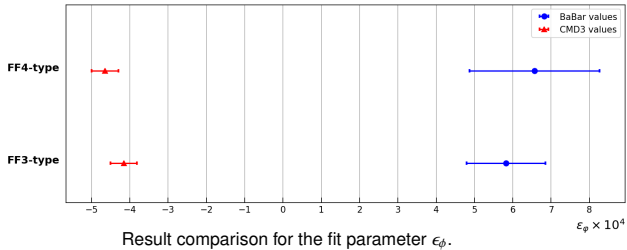
ref.2, Average value 2023:
[Colangelo G., Hoferichter M. & Stoffer P., 2023]

Review of Particle Physics,
Average value (2022):
[Review of Particle Physics,
2022]



ref.1, CMD3 value: [Ignatov
F.V. et al., 2023]

ref.2 BaBar, CMD3 values
2023: [Colangelo G.,
Hoferichter M. & Stoffer P.,
2023]



PDG Average value
(2022): [\[Review of Particle Physics, 2022\]](#)

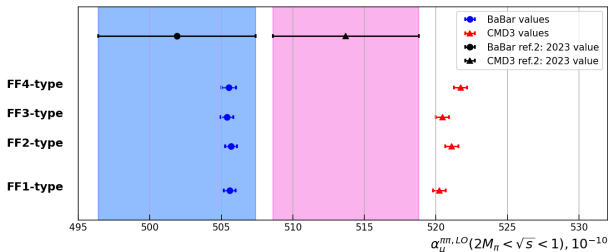
Ref.2023 CMD3 value:
[\[Ignatov F.V. et al., 2023\]](#)

4.6: Results for $\alpha_\mu^{(\pi^+\pi^-,LO)}$

$\alpha_\mu^{\pi\pi,LO} \times 10^{-10}$						
	BaBar			CMD3		
$F_\pi^V(s)$ type	$(2M_\pi - 1)$ GeV	$(0.6 - 0.88)$ GeV	$(0.327 - 1.2)$ GeV	$(2M_\pi - 1)$ GeV	$(0.6 - 0.88)$ GeV	$(0.327 - 1.2)$ GeV
FF1-type	505.58±0.41	372.15±0.34	509.38±0.43	520.23±0.44	383.99±0.36	524.50±0.45
FF2-type	505.67±0.41	372.23±0.34	509.47±0.43	521.11±0.46	384.72±0.37	525.41±0.47
FF3-type	505.39±0.46	371.94±0.37	509.13±0.43	520.45±0.45	384.22±0.37	524.78±0.45
FF4-type	504.06±0.52	371.69±0.42	509.27±0.43	520.32±0.47	384.94±0.38	526.09±0.48

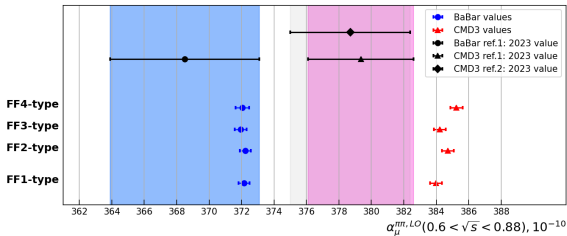
Results for the HVP contribution of the $(2\pi, LO)$ to the anomalous magnetic moment of the muon

- The result comparison ² for $\sqrt{s} \in [2M_\pi, 1]$ GeV :

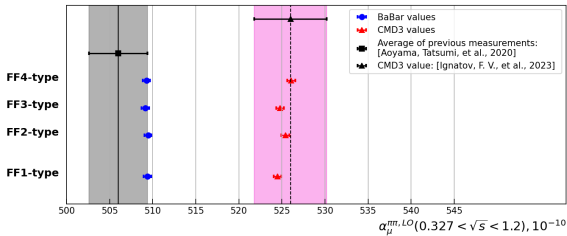


²BaBar ref.2, CMD3 ref.2: 2023 value: [Colangelo G., Hoferichter M. & Stoffer P., 2023]

- The result comparison^{3 4} for $\sqrt{s} \in [0.6, 0.88]$ GeV:



- The result comparison for $\sqrt{s} \in [0.327, 1.2]$ GeV:

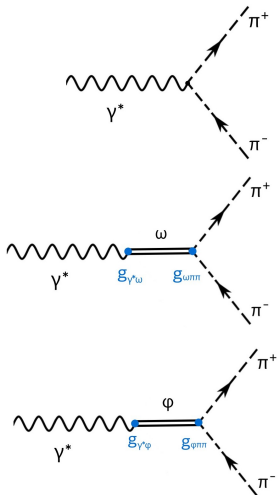


³BaBar ref.1, CMD3 ref.1: 2023 values: [Ignatov F.V. et al., 2023]

⁴CMD3 ref.2: 2023 value [Colangelo G., Hoferichter M., & Stofer P, 2023]

Branching ratios

5: Branching ratio results



$$\kappa_1 = g_{\gamma^*\omega} \cdot g_{\omega\pi\pi} = \epsilon_{\rho\omega}$$

$$\kappa_2 = g_{\gamma^*\phi} \cdot g_{\phi\pi\pi} = \epsilon_{\phi}$$

- Use of known decay widths ^a to calculate $g_{\gamma^*\omega}$ and $g_{\gamma^*\phi}$:

$$\Gamma(\omega \rightarrow e^+e^-) = \frac{4\pi\alpha_{em}^2}{3} g_{\gamma^*\omega}^2 M_{\omega}$$

$$\Gamma(\phi \rightarrow e^+e^-) = \frac{4\pi\alpha_{em}^2}{3} g_{\gamma^*\phi}^2 M_{\phi}$$

^a[Hanhart C. et al., 2018]

- Use of fit parameters $\epsilon_{\rho\omega}/\epsilon_\phi$ to calculate the couplings $g_{\omega\pi\pi}$ and $g_{\phi\pi\pi}$ and then the branching ratios⁵:

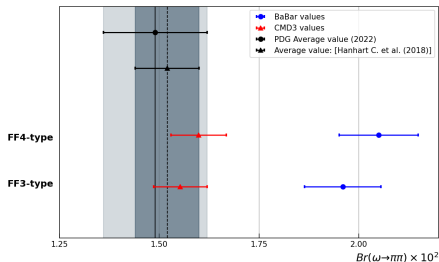
$$\mathcal{B}(\omega \rightarrow \pi^+ \pi^-) = \frac{\Gamma(\omega \rightarrow \pi^+ \pi^-)}{\Gamma_\omega^{\text{tot}}} = \frac{g_{\omega\pi\pi}^2}{48\pi} \frac{(M_\omega^2 - 4M_\pi^2)^{3/2}}{M_\omega^2} \left| \Omega(M_\omega^2) \right|^2 \cdot \frac{1}{\Gamma_\omega^{\text{tot}}}$$

$$\mathcal{B}(\phi \rightarrow \pi^+ \pi^-) = \frac{\Gamma(\phi \rightarrow \pi^+ \pi^-)}{\Gamma_\phi^{\text{tot}}} = \frac{g_{\phi\pi\pi}^2}{48\pi} \frac{(M_\phi^2 - 4M_\pi^2)^{3/2}}{M_\phi^2} \left| \Omega(M_\phi^2) \right|^2 \cdot \frac{1}{\Gamma_\phi^{\text{tot}}}$$

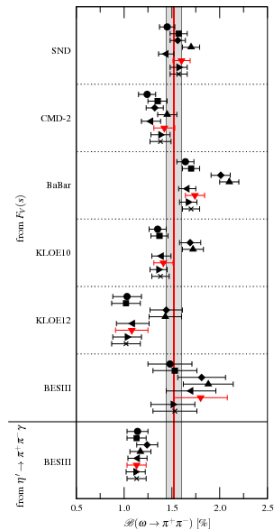
$F_\pi(s)$ type	Data set	$ g_{\omega\pi\pi} \times 10^{-2}$	$ g_{\phi\pi\pi} \times 10^{-2}$	$\mathcal{B}(\omega \rightarrow \pi\pi) \times 10^{-2}$	$\mathcal{B}(\phi \rightarrow \pi\pi) \times 10^{-2}$
FF3-type	BaBar	3.42 (± 0.08)	0.78(± 0.14)	1.96 (± 0.90)	0.029 (± 0.010)
	CMD3	3.04 (± 0.07)	0.56 (± 0.05)	1.55 (± 0.07)	0.015 (± 0.003)
FF4-type	BaBar	3.49 (± 0.08)	0.88 (± 0.23)	2.05 (± 0.10)	0.036 (± 0.019)
	CMD3	3.08 (± 0.07)	0.63 (± 0.05)	1.60 (± 0.07)	0.019 (± 0.003)

⁵[Hanhart C. et al., 2018]

- The branching ratio result comparison for the mode $(\omega \rightarrow \pi\pi)^a$:

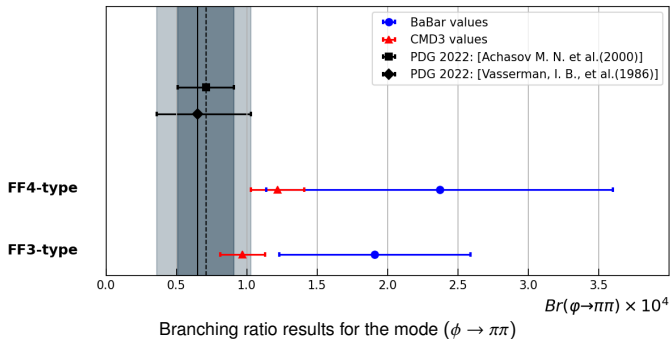


^aPDG Average value (2022): [Review of Particle Physics, 2022]
Average value including corrected BaBar data: [Hanhart C. et al., 2018]



[Hanhart C. et al., 2018]

- The Branching ratio result comparison for the mode $(\phi \rightarrow \pi\pi)$ ⁶:



⁶PDG 2022 values: [\[Review of Particle Physics, 2022\]](#)

Summary & Conclusions

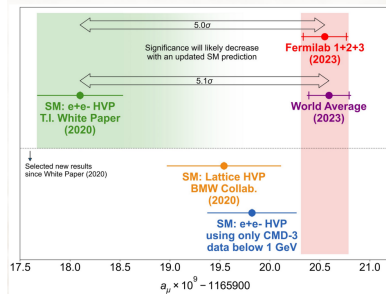
Fit of **four** phenomenological functions of $F_{\pi}^V(s)$ on data from BaBar and CMD-3:

- **Calculated $\alpha_{\mu}^{\pi\pi, LO}$ for $\sqrt{s} \in [2M_{\pi}, 1]$, $[0.6, 0.88]$ and $[0.327, 1.2]\text{GeV}$**
 - ↪ Results within the limits for BaBar and in relative agreement for CMD-3
 - ↪ **Reproduced** and **confirm the deviation** between the values for BaBar and CMD-3
- **Used $\epsilon_{\rho\omega}$ and ϵ_{ϕ} for the isospin-breaking processes**
 - ↪ Calculated branching ratios for ($\omega \rightarrow \pi^+\pi^-$, $\phi \rightarrow \pi^+\pi$)
 - ↪ Values from CMD-3 data analysis closer or in agreement with reference values

Conclusions

Primary concerns:

- CMD-3 produce higher values than all previous experiments
 - ↪ inconsistencies between results
 - ↪ add to the uncertainty for the α_μ^{HVP}
- Using only CMD3 data for $\alpha_\mu^{e^+e^-}$, HVP
 - ↪ eliminate large deviation from experiment
 - ↪ deviation from previous evaluations



[Ignatov F. et al., 2023.]

Future goals:

- Further study of experimental & calculation methods → determine the source of discrepancy
- Results from future experiments → obtain more values for a more accurate picture

Thank you for your attention!
Any questions?

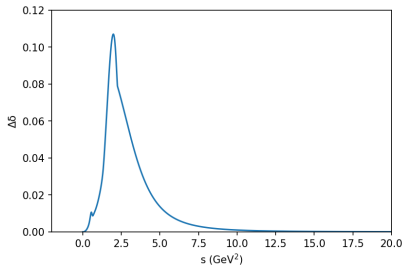
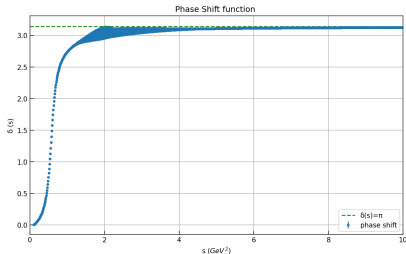
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B.1: Alternative to error analysis

- Include the error-data of phase shift $\delta \pm \Delta\delta(s)$:



- Extrapolate the errors at higher energy so that it goes to 0:

$$\Delta\delta(s) = \begin{cases} \text{Interpolated function from Bern error values} & , \text{ for } 4M_\pi^2 \leq s \leq s_0 \\ \Delta\delta(s_0) \cdot \left(\frac{\lambda_0^2 + s_0^4}{\lambda_0^2 + s^4} \right) & , \text{ for } s \geq s_0 \end{cases}$$

with $s_0 = 2.25 \text{ (GeV)}^2$.

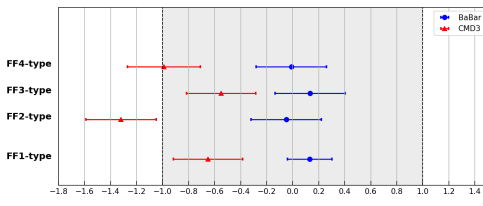
- Use exponential form of $\Omega(s)$ and add another fit parameter:

$$\Omega[\delta \pm \Delta\delta] = \Omega[\delta] \cdot \Omega[\pm\Delta\delta] = \Omega[\delta] \cdot (\Omega[\Delta\delta])^c$$

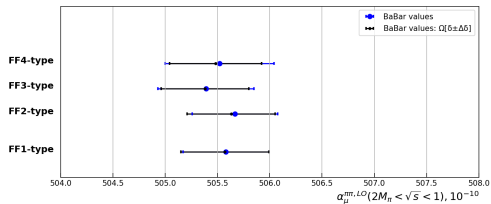
$$F_\pi^V(s) = P(s) \cdot \Omega[\delta(s)] \cdot \Omega[\Delta\delta(s)]^c$$

- Fit result comparison:

χ^2_{red}				
F-type	BaBar		CMD3	
	without $\Delta\delta$	with $\Delta\delta$	without $\Delta\delta$	with $\Delta\delta$
FF1	1.68	1.67	1.92	1.89
FF2	1.45	1.44	1.60	1.49
FF3	1.57	1.57	1.16	1.14
FF4	1.38	1.37	0.72	0.65



- Result comparison for BaBar:



- Result comparison for CMD-3:

