Diffre- Kellman Protocol. (RH) · Fix a finite cyclic group & of order in (3, &=(Ze)) · Fine a generator q in & leg, &= £1, 2, 9, 9; ..., 8"5) Choose a random bin St, ng choose a random a in It, no B = 9 mode Ba = (g6) = tab = gab = (ga)6 = A and p Comprédational Diffie-Mehman (CDH) · 6: Amile oyelie group of order n. ODH assumption holds if: g, g, g = = g as For all efficient algorithms A: where g = 2 generators of 85 Some Trapadoor Permutations (TRPs) are constaucted directly from CADH

Lecure Trappoor Functions (TDFS)

· (&, F, F) is a secure 7507 which can be evaluated but commot be inverted without six

Challenger		Adversary
(pt, st) = 011	Th. yz F(pe, x)	X,
2 4 X		

Def: (G, F, F) is a secure FAF of for all of A.

Ado [A, F] = P2[n=n:] < negl.

· (6, F, F) - seawy FOF X-> Y.

· (Ez, Dz) - Sym anth ene scheme over (k, M, e)

· h · x -> x - a Lash function.

 $\frac{\mathcal{E}(pk, m)}{x \leftarrow \lambda} \cdot \frac{\mathcal{P}(pk, n)}{y \leftarrow \mathcal{P}(pk, n)} = \frac{\mathcal{P}(sk, (y, c))}{x \leftarrow \lambda} \cdot \frac{1}{(sk, y)} \cdot \frac{1}{$

-

· Come apply F directly to plantest (deterministic)

Arcithmetic mod

· Let N-pq where p, a are prime

· ZN - 80,1,2, N-13 (ZN) = 2 nverlaste elements or ZNJ

· Fact a G ZN is invertable if god (a, N) =1.

· Num of elements in (2) is if (N) - (1-1/9-1) - N-1-9-4

Euler's theorem. Yne (ZN) : ne +(N) = 1

R8A TAP

· G(): choose random pumos p.g a 1024 bits.

generation $8e^2 N = pq$ algorian choose integers e, of such that e d = + (mod + (N))

=> output pk = (N, e) 8k = (N,d)

· F(pk, n): Z" -> Z"; RISA(20) = 20 (1- ZN) compete leapace permaterion

· F'(8k, y); yd = R8A(x)d = xed = xe ++(n)involving the premidation = (x4(N))*. x = 1 x = 1x

Def. (R8A assumption) R8A is a one way permitation.

For all off algorithms A:

Pr [A(N,e,y) = y'e] ~ negl.

where P.g = n Bit primes,

NE PG