Diffie- Kellman Protocol. (DH) · Fix a finite cyclic group & of order in (29, &=(Zp)). · Pin a generator g in & (e.g., &= £1, 8, 92, 93, ..., 8"-5) Choose a random bin 31, ng choose a random a in II. , n] A=ga mod p B = g mode $B^{a} = (g^{6})^{a} = k_{AB} = g^{ab} = (g^{a})^{6} = A^{6}$ Comprédational Diffie-Mehman (CDH) 6: Amite oyelie group of order n. COH assumption holds if: q, g, g, g, g => g as For all efficient algorithms A: Some Trapadoor Permutations (TRPs) are constancted directly from CADH

Lecure Trappoor Prenctions (TDFS)

· (f, F, F') is a secure TDF which can be evaluated but among be inverted without it

Challenger	Adversary
(pt, st) - 01	PK, YZF(PK,X)
2 d X	

Def: (B, F, F) is a secure TAF of for all of A.

Ado [A, F] = P2[x=xi] < negl.

· (6, F, F) - seave TOF X-> Y.

· (Es, Ds) - sym with ene scheme over (k, M, e).

· k · x > x - a bash function.

 $\frac{\mathcal{E}(pk, m)}{x \leftarrow X} \cdot y \leftarrow P(pk, x) \qquad |\mathcal{R}(sk, (y, c))|^{\frac{1}{2}}$ $\frac{k \leftarrow \mathcal{H}(x)}{x \leftarrow \mathcal{E}_{S}(k, m)} \qquad |\mathcal{R} \leftarrow \mathcal{F}^{-1}(sk, y)|$ $\frac{k \leftarrow \mathcal{H}(x)}{cutput}(y, c) \qquad |\mathcal{R}(k, m)| \qquad |\mathcal{R}(k, m)|$ $\frac{k \leftarrow \mathcal{H}(x)}{cutput} \cdot y \cdot c \leftarrow \mathcal{E}_{S}(k, m) \qquad |\mathcal{R}(k, m)|$ $\frac{k \leftarrow \mathcal{H}(x)}{cutput} \cdot y \cdot c \leftarrow \mathcal{E}_{S}(k, m) \qquad |\mathcal{R}(k, m)|$

0

· Course apply & directly to plantest (deterministic)

Arcithmedic mod

· Let N=pq where p, q are prime

· ZN = 20,12, N-13 , (ZN) = 2 nverlable elements in ZNJ

· Fact ne EZN is invertable if god (=, N) =1.

· Num of elements in (2) " is if (N) = 11-1/9-1 = N-p-9-4

· Euler's theorem: $\forall x \in (Z_N)^* : x^{f(N)} = 1$

R8A TEP

· G(): choose random primes p. q = 1024 bits.

generation set N = Pq. algorithm choose integers e, d such that e d = 1 (mod f(N))

=> output pk = (N,e) 8k = (N, d)

· F(pk, n): Z, -> Z, ; R/8A(2) = 20° (1- ZN) compute teaploor permitation

· F'(8k, y); yd = R8A(x)d = xed = xe ++(w)-1 inventing the permittation = (x4(N)) * . x = 1.2 = 12

Def. (R8A assumption) R8A is a one way permetation.

For all eff. algorithms A:

Pr [A(N, e, y) = y'e] ~ negl.

where p.g = n. Bit primes, NE PG ye Z * Silvey