Diffre- Kellman Protocol. (DH) · Fix a finte cyclic group & of order in (23, &=(Zp)) · Fine a generator g in & leg, &= 11, 2, 9, 9; ..., 8" 5) alcose a random bir 33, ng choose a random a in fr. n. ] B = 9 mode Ba = (g6) = tab = gab = (ga)6 = A made Comprétational Diffie- Mehman (CDH) 6: Anite oyelie group of order n. COH assumption holds if: g, g, g, g, g, g For all efficient algorithms A: where g = 2 generators of 85 Some Trapadoor Permutations (TRPs) are constancted directly from CDH

## Lecure Traploor Functions (TDFS)

· (f, F, F) is a secure 750 F which can be evaluated but cannot be inverted without it

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Challenger	Adversary
(pk, sk) = 011	y=F(p4, x) x'
2	

Def: (G, F, F) is a secure FAF of for all of A.

Ado [A, F] = P2[x=xi] < negl.

· (E, F, F) - secure FAF X-> Y.

· (Es, Ps) - sym with ene scheme over (k, M, e)

· k · x - x - a lash function

 $\frac{\mathcal{E}(pk, m)}{x \leftarrow \lambda} \cdot \frac{\mathcal{P}(pk, n)}{y \leftarrow \mathcal{P}(pk, n)} \cdot \frac{\mathcal{P}(sk, (y, c))}{m \leftarrow \mathcal{F}'(sk, y)}$   $\frac{k \leftarrow \mathcal{H}(x)}{c \leftarrow \mathcal{E}_{s}(k, m)} \cdot \frac{k \leftarrow \mathcal{H}(n)}{c \leftarrow \mathcal{P}_{s}(k, c)}$   $\frac{\partial \mathcal{E}(pk, m)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(k, n)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(k, c)}{\partial \mathcal{E}(pk, n)}$   $\frac{\partial \mathcal{E}(pk, m)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(pk, n)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(pk, n)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(pk, n)}{\partial \mathcal{E}(pk, n)}$   $\frac{\partial \mathcal{E}(pk, m)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial \mathcal{E}(pk, n)}{\partial \mathcal{E}(pk, n)} \cdot \frac{\partial$ 

· Course apply F directly to plantest (deterministic)

## Arcithmetic mod

· Let N-pq where p, q are prime

· ZN = 20,12, N-13 (ZN) = 2 vocable

· Fact a c Zu is invertable if god (a, N) =1.

· Num of elements in (Z) " is if (N) - (1-1/9-1) - N-p-2 -1

· Eulor's theorem : Vne (ZN)\*: ne +(N) = 1

## R8A TEP

· G(): cheese random pumos p.q = 1024 Bits.

generation set N = pq.

Algorithm choose integers e, d such that e d = 1 (mod f(N))

=> output pk = (N, e)8k = (N, d)

· F(pk, n): Z" -> Z"; RISA(2) = 20° (in ZN)

• F'(8k, y);  $yd = R8A(x)^d = xed = xe^{4+(N)-1}$ involving the permutation  $= (x^{4(N)})^k$ . x = 1 = x

Def. (RSD assumption) RSA is a one way permutation.

For all off algorithms A:

Pr[A(N,e,y)=y'e] z negl.

where p. q = n. bit primes,

y + Z + Manag