Diffre- Kellman Protocol. (DH) · Fix a finite cyclic group & of order in (03, &=(Zp)) · Fine a generator q in & (eg, &= £1, 8, 9, 9; ..., 8"5) Choose a random bin 31, ng choose a random a in fi., n] B = 9 mode Ba = (gb) = tab = gab = (ga) = A and p Comprétational Diffie-Mehman (CDH) 6: Amite cyclic group of order n. ODH assumption holds if: g, g, g, g, g, g, g For all efficient algorithms A: where g = 2 generators of 65 Some Trapadoor Permutations (TRPs) are constancted directly from CDH

Secure Trapsoor Princtions (TDFS)

· (&, F, F !) is a secure 750 F which can be evaluated but cannot be inverted without it

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Challenger	Adversary	
(ph, sh) 4 811	1/2 y= F(pe, x)	×
2 ×		

Def: (G, F, F") is a secure FAF of for all of A.

Ado [A, F] = P2[n=n:] < negl.

· (E, F, F) - scoure FDF X-> Y.

· (E, P, F) - sym with ene scheme over (k, M, e)

· H: X -> K - a Lash function

 $\frac{\mathcal{E}\left(\rho k, m\right)}{x \leftarrow \lambda} \cdot \frac{\mathcal{P}\left(\rho k, x\right)}{y \leftarrow \mathcal{P}\left(\rho k, x\right)} = \frac{\mathcal{P}\left(s k, (y, c)\right)}{x \leftarrow \mathcal{F}'\left(s k, y\right)}$ $\frac{k \leftarrow \mathcal{H}(x)}{c \leftarrow \mathcal{E}_{S}(k, m)} \cdot \frac{k \leftarrow \mathcal{H}(x)}{k \leftarrow \mathcal{H}(x)}, \quad m \leftarrow \mathcal{P}_{S}(k, c)$ output (y, c)output $x \leftarrow \mathcal{P}_{S}(k, c)$

· Como apply & directly to plantest (deterministic)

Arcithmetic mod

· Let N-p q where p, a are prime

· ZN = 20,1,2, N-13 (ZN) = 2 rveriable

· Fact a c ZN is invertable if god (= N) =1.

· Num of elements on (ZN) is of (N) = (p-1)(q-1) = N-p-q +1

· Euler's theorem: Vx e (ZN) : x +(N) = 1

R8A TOP

· G(): cheose random pumas p.g = 1024 Bits.

generation set $N = \rho q$.

Algorithm choose integers e, d such that $e \cdot d = t \pmod{f(N)}$

=> output pk = (N, e)8k = (N, d)

· F(pk, n): Z" -> Z"; RISA(2) = 20° (in ZN)

• F'(8k, y); $yd = R8A(\pi)^d = \pi^{ed} = \pi^{\frac{1}{2}+|n|}$.

involving the permutation $= (\pi^{\frac{1}{2}(N)})^{\frac{1}{2}}$. $\pi = 1$ $\pi = 1$

18 = 1

Def. (RSD assumption) RSA is a one way permitotion.

For all off algorithms A:

Pr [A(N, e, y) = y'e] z negl.

where P. q = n Bit primes,

NE PG y + Z + Mang