Diffie- Kellman Protocol. (DH) · Fix a finite cyclic group & of order n (29, &=(Zp)). · Fine a generator g in & (eg, &= \$1,8,9,9,9,...,8") Choose a random bin ft, ng choose a random a in II. , n] A=ga mod p B = g mode Ba = (g6) = tab = gab = (ga)6 = A6 Comprédational Diffie-Mehman (CDH) 6: Amite cyclic group of order n. ODH assumption holds if: g, g, g, g, g, g. For all efficient algorithms A: where $g \leftarrow 2$ generators of 85 and g = gab and Some Trapadoor Permutations (TRPs) are constancted directly from CAH

Lecure Trappoor Prenetions (TDFS)

. (f, F, F') is a secure TDF which can be evaluated but asmost be inverted without it

Challenger	Adversary
(pk, sk) = 01)	pk, y= F(pe, x)
z e X	

Def: (B, F, F) is a secure FAF of for all of A.

Ado [A, F] = P2[x=xi] < negl.

· (6, F, F) - seave TOF X-> Y.

· (Es, Ds) - sym with ene scheme over (k, M, c)

· h. x > x - a bash function.

 $\frac{\mathcal{E}(pk, m)}{x \leftarrow X} \cdot \frac{\mathcal{P}(pk, x)}{y \leftarrow \mathcal{P}(pk, x)} = \frac{\mathcal{P}(sk, (y, c))}{x \leftarrow \mathcal{F}'(sk, y)} \cdot \frac{\mathcal{P}(sk, y)}{k \leftarrow \mathcal{H}(x)} \cdot \frac{\mathcal{P}'(sk, y)}{k \leftarrow \mathcal{H}(m)} \cdot \frac{\mathcal{P}'(sk, y)}{m \leftarrow \mathcal{P}'(sk, e)}$ output (y, c) output m

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· Council apply & directly to plantast (deterministic)

Arcithmedic mod

· Let N=pq where p, q are prime

· ZN = 20,12, N-13 (ZN) = 2 overlable elements in ZNJ

· Fact no ZN is invertable if ged (= N) =1.

· Num of elements in (2) " is if (N) = 11-1/9-1 = N-p-9-1

· Euler's theorem: $\forall x \in (Z_N)^* : x^{f(N)} = 1$

R8A TEP

· G(): choose random pumos p.q a 1024 bits.

generation set N = Pq. algorithm choose integers e, d such that e d = 1 (mod f(N))

=> output pk = (N,e) 8k = (N, d)

· F(pk, n): Z, -> Z, ; RSA(2) = 20 (1- ZN) compute teapleon permitation

· F'(8k, y); yd = R8A(x)d = xed = xe +4(w). inverting the permittation = $(nf(n))^k$. $n = 1 \cdot n = n$

Def. (R8A assumption) R8A is a one way permutation.

For all off algorithms A:

Pr [A(N, e, y) = y'e] ~ negl.

where p. q = n. bit primes. NE PG ye Z* Helosy