

Abstract

Scheduling of personnel in a hospital environment is vital to improving the service provided to patients and balancing the workload assigned to clinicians. Many approaches have been tried and successfully applied to generate efficient schedules in such settings. However, due to the computational complexity of the scheduling problem in general, most approaches resort to heuristics to find a non-optimal solution in a reasonable amount of time. We designed an integer linear programming formulation to find an optimal schedule in a clinical division of a hospital. It mitigates computational complexity issues by maintaining a minimal set of constraints, yet still provides the flexibility necessary to adapt the formulation to a variety of clinical divisions.

We then conducted a case study for our approach using data from the Infectious Diseases division at St. Michael's Hospital in Toronto, Canada. We analyzed and compared the results of our approach to manually-created schedules at the hospital, and found improved adherence to departmental constraints and clinician preferences. We then used simulated data to examine the sensitivity of the runtime of our linear program for various parameters and observed reassuring results, signifying the practicality and generalizability of our approach in different real-world scenarios.

1 Introduction

On-call schedules for a fixed number of health-care providers are central to the efficient running of hospitals. Hospital departments provide services where patient needs, and thus the system's demands, often exceed the available supply. For example, it is important that a hospital department allocates its resources, such as the availability of a finite number of clinicians, optimally, to ensure the best possible service for its patients. Carefully allocated on-call schedules are meant to simultaneously ensure sufficient resources are provided to patients while not overworking clinicians to prevent costly mistakes [ref]. It is common practice for on-call schedules to be created manually. Yet manually-created schedules are prone to errors and potential for biases [ref]. First, when there is a large number of clinicians in a single department, or the constraints that need to be satisfied by the department are very complex, a manual method may not provide an optimal schedule. Second, such methods are likely to overlook certain constraints that must be maintained to have an operational department, such as XXXX. Third, manual scheduling is often time-consuming for the person developing the schedule. For these reasons, it is important to develop automated methods that can generate optimal schedules that satisfy the given constraints of the hospital department.

Automated methods to optimize schedules have been studied and applied in many industries, including transportation [??], manufacturing [??], [...]. Of special interest to a clinician on-call scheduling problem are the approaches to

schedule nurses, who often work in shifts. In the nurse scheduling problem, the goal is to find an optimal assignment of nurses to shifts that satisfies all of the hard constraints, such as hospital regulations, and as many soft constraints as possible, which may include nurse preferences. A wide variety of approaches, including exact and heuristic approaches, have been used to solve the nurse scheduling problem: integer linear programming [??], network flows [??], genetic algorithms [??], simulated annealing [??], and artificial intelligence [??].

Many of these approaches were designed to satisfy the requirements of a specific hospital department which causes a large number of variables and constraints to be incorporated into the problem formulation. While these department-specific approaches allow end-users to find precise schedules that satisfy the needs of the department and the preferences of the nurses and clinicians in that department, they are difficult to readily adapt to other departments in the same hospital or other hospitals. Moreover, the large number of variables and constraints also leads to computational complexity issues [ref], especially when using exact methods for finding the solution. In this paper, we tackle a version of the nurse scheduling problem arising from a case study of one clinical division, providing two different services simultaneously (general infectious disease (ID) consults; and HIV consults service) at St. Michael’s Hospital in Toronto, Canada. Our goal is to (1) present a simple integer linear programming formulations for the scheduling problem as developed for the hospital, and describe the adaptability of the formulation to solving similar problems in other departments; (2) compare the performance of the ILP scheduler to the results of the manual approach; and (3) analyze the robustness of the algorithm in difficult instances of the problem.

We begin by describing the problem in Section 2, and presenting our ILP formulation in Section 3. Next, we compare the results of our formulation to manually-created schedules, and evaluate the performance of the algorithm on simulated data in Section 4. Finally, we discuss and interpret the results in Section 5.

2 Problem

At St. Michael’s Hospital, the division of infectious diseases (ID) offers general ID and HIV consultation on inpatients as two parallel services. Each service provides clinical care throughout the year, during regular work weeks as well as weekends and holidays. The clinicians in the division typically receive a schedule in advance, outlining their on-call service dates for the full year. In the yearly schedule each clinician is assigned to blocks of regular work weeks and weekends. Each block corresponds to two consecutive work weeks. Apart from long (holiday) weekends, a work week starts on Monday at 8 A.M. and ends on Friday at 5 P.M. Accordingly, weekend service starts on Friday at 5 P.M., and ends on Monday at 8 A.M. During the weekend, ID and HIV consultation

services are combined and provided by one clinician. During the regular work week the ID and HIV services are led by one clinician each.

Several constraints are placed on the on-call assignments. First, each clinician has limits on the number of blocks they can and must work during the year, depending on the type of consultation. For instance, a clinician might have to provide 3-5 blocks of general ID consultation as well as 2-3 blocks of HIV consultation throughout the year. These limits may change from year to year as the number of clinicians in the department changes. Moreover, the schedule should not assign a clinician to work for two blocks or two weekends in a row. The schedule should also distribute both regular and holiday weekends equally among all clinicians.

In addition to maintaining a balanced work load among clinicians, the schedule should also accommodate their preferences. Clinicians provide their requests for time off ahead of schedule generation so that the requests may be integrated into the schedule. Individuals may specify days, weeks or weekends off, with the understanding that any blocks overlapping with their request will be assigned to a different clinician where possible. For example, if a clinician only requests a given Monday and Tuesday off, the schedule will generally avoid assigning the entire block to that clinician. Clinicians also prefer to have their weekend and block assignments close together, so the schedule should account for this when distributing assignments. A summary of the outlined constraints is given in Table 1.

In most scheduling problems, the constraints can be divided into hard and soft constraints. Hard constraints must be satisfied by any candidate solution, while soft constraints can be used to select a more favourable solution from all candidate solutions [ref]. Typically, soft constraints are encoded as objective functions rather than actual constraints. These objective functions are maximized or minimized when finding a solution. In the case of our clinician scheduling problem, we chose Block Requests, Weekend Requests and Block-Weekend Adjacency as our soft constraints, while the rest of the constraints are hard. Though it is important to take clinician requests into account when constructing the schedule, it is crucial that the work-load of the schedule is balanced among all clinicians, and the needs of the patients are fulfilled.

It is important to note that - irrespective of how the schedule is generated - clinicians may exchange certain weeks or days throughout the year after the schedule is implemented. The approach to solving the clinician scheduling problem does not account for these future exchanges, and only focuses on the full year time horizon.

Constraint Name	Description	Type
Block Coverage	each service needs to have exactly one clinician that covers any given block	Hard
Weekend Coverage	every weekend needs to have exactly one clinician that covers it	Hard
Min/Max	for a given service, each clinician can only work between the minimum and maximum number of allowed blocks	Hard
No Consecutive Blocks	any clinician should not work two consecutive blocks, across all services	Hard
No Consecutive Weekends	any clinician should not work two consecutive weekends	Hard
Equal Weekends	weekends should be equally distributed between clinicians	Hard
Equal Holidays	long weekends should be equally distributed between clinicians	Hard
Block Requests	each clinician can request to be off service during certain blocks throughout the year	Soft
Weekend Requests	each clinician can request to be off service during certain weekends throughout the year	Soft
Block-Weekend Adjacency	the block and weekend assignments of a given clinician should be adjacent	Soft

Table 1: Summary of the constraints for the clinician scheduling problem

3 Methods

In this section, we present an application of 0-1 Linear Programming to solve the clinician scheduling problem presented in Section 2. First, we describe the sets, indices and variables present in the formulation of the program. We then convert the constraints given in Table 1 into mathematical terms, and outline the objective function of the linear program.

3.1 Sets and Indices

We denote the set of all services that clinicians in a single department can provide as \mathcal{S} . The following formulation assumes that all clinicians are able to provide all services. The set of all clinicians in the department is denoted as \mathcal{C} . The sets of blocks and weekends that clinicians will be assigned to are denoted as \mathcal{B} and \mathcal{W} respectively. The block size used in our experiments is 2 weeks, but the following LP formulation does not specify a particular size for blocks, and so it can be adapted to the needs of the department in question. A subset of weekends are denoted \mathcal{L} , corresponding to established long/holiday weekends such as the Canadian Civic Day weekend in August. Lastly, we denote with \mathcal{BR}_c and \mathcal{WR}_c the block and weekend requests of clinicians as subsets of all blocks

and weekends, respectively. For instance, if clinician c 's requests intersect with blocks 1 and 2, and weekend 1, then $\mathcal{BR}_c = \{1, 2\}$ and $\mathcal{WR}_c = \{1\}$. Table 2 presents a summary of the sets and indices described.

Set	Index	Description
$\mathcal{S} = \{1, \dots, S\}$	s	services
$\mathcal{C} = \{1, \dots, C\}$	c	clinicians
$\mathcal{B} = \{1, \dots, B\}$	b	blocks
$\mathcal{W} = \{1, \dots, W\}$	w	weekends
$\mathcal{L} \subset \mathcal{W}$		long weekends
$\mathcal{BR}_c \subset \mathcal{B}$		block requests of clinician c
$\mathcal{WR}_c \subset \mathcal{W}$		weekend requests of clinician c

Table 2: Description of sets and indices in the problem

3.2 Variables

Since each clinician may be assigned to work on any service, during any block of the year, we denote such an assignment as $X_{c,b,s}$. A value of 1 indicates that the given clinician c is assigned to provide service s during block b . Similarly, we define weekend assignments as $Y_{c,w}$, although these are not indexed by service, as clinicians are expected to provide all services during the weekends. To optimize the soft constraint Block-Weekend Adjacency, we maximize the product $X_{c,b,s} \cdot Y_{c,w}$ for adjacent blocks and weekends. To formulate such an objective as a linear function of variables, we introduce another set of variables, denoted by $Z_{c,b,s}$, with additional constraints on its range. Further details regarding this variable are described in Section 3.4. We then introduce a set of constants $m_{c,s}$ and $M_{c,s}$ to constrain the minimal and maximal number of blocks each clinician is allowed to work during the year. Table 3 presents a summary of the constants and variables in the problem.

Name	Description
$X_{c,b,s} \in \{0, 1\}$	assignment of clinician c to service s on block b
$Y_{c,w} \in \{0, 1\}$	assignment of clinician c on weekend w
$Z_{c,b,s} \in \{0, 1\}$	helper variable for optimizing Block-Weekend adjacency
$m_{c,s}$	minimum number of blocks clinician c should cover on service s
$M_{c,s}$	maximum number of blocks clinician c should cover on service s

Table 3: Description of variables and constants in the problem

3.3 Constraints

We now present the hard constraints in Table 1 using the variables defined above.

$$\begin{aligned}
\sum_{c=1}^C X_{c,b,s} &= 1 & \forall b \in \mathcal{B}, s \in \mathcal{S} & \quad (\text{Block Coverage}) \\
\sum_{c=1}^C Y_{c,w} &= 1 & \forall w \in \mathcal{W} & \quad (\text{Weekend Coverage}) \\
m_{c,s} &\leq \sum_{b=1}^B X_{c,b,s} \leq M_{c,s} & \forall c \in \mathcal{C}, s \in \mathcal{S} & \quad (\text{Min/Max}) \\
X_{c,b,s} + X_{c,b+1,s} &\leq 1 & \forall c \in \mathcal{C}, b \leq B-1, s \in \mathcal{S} & \quad (\text{No Consecutive Blocks}) \\
Y_{c,w} + Y_{c,w+1} &\leq 1 & \forall c \in \mathcal{C}, w \leq W-1 & \quad (\text{No Consecutive Weekends}) \\
\left\lfloor \frac{W}{C} \right\rfloor &\leq \sum_{w=1}^W Y_{c,w} \leq \left\lceil \frac{W}{C} \right\rceil & \forall c \in \mathcal{C} & \quad (\text{Equal Weekends}) \\
\left\lfloor \frac{|\mathcal{L}|}{C} \right\rfloor &\leq \sum_{w \in \mathcal{L}} Y_{c,w} \leq \left\lceil \frac{|\mathcal{L}|}{C} \right\rceil & \forall c \in \mathcal{C} & \quad (\text{Equal Holidays})
\end{aligned}$$

3.4 Objectives

As described in Section 2, the soft constraints of the clinician scheduling problem include: (1) satisfying clinician block off requests, (2) satisfying clinician weekend off requests, and (3) assigning weekends closer to blocks. We convert these soft constraints into linear objective functions of the binary variables defined in Section 3.2. Objectives (1) and (2) can be written as the following linear functions:

$$\begin{aligned}
Q_1(X) &= \sum_{c=1}^C \sum_{b=1}^B \sum_{s=1}^S (-1)^{\mathbb{1}(b \in \mathcal{BR}_c)} \cdot X_{c,b,s} & (\text{Block Requests}) \\
Q_2(Y) &= \sum_{c=1}^C \sum_{w=1}^W (-1)^{\mathbb{1}(w \in \mathcal{WR}_c)} \cdot Y_{c,w} & (\text{Weekend Requests})
\end{aligned}$$

where $\mathbb{1}(\cdot)$ is the indicator function that has value 1 when the condition is met and 0 otherwise. In the above two objectives, we penalize any assignments that conflict with a block or weekend request, and aim to maximize the non-conflicting assignments. The Block-Weekend Adjacency is optimized by considering the product $X_{c,b,s} \cdot Y_{c,w}$ for values of w “adjacent” to the value of b . For instance, clinicians might want to be assigned during a weekend that falls within an assigned block. So if clinician c is assigned to work during block 3, corresponding to weeks 5 and 6 assuming 2-week blocks, they might also want to be assigned to work during weekend 5. In that case, we would like $X_{c,b=3,s} \cdot Y_{c,w=5}$ to be 1, since that indicates both variables are assigned. If at least one of the two variables is not assigned, the product will be 0. This leads

to the maximization objective

$$Q_3(X, Y) = \sum_{c=1}^C \sum_{b=1}^B \sum_{s=1}^S X_{c,b,s} \cdot Y_{c,w=\varphi(b)} \quad (\text{Block-Weekend Adjacency})$$

where $\varphi(b)$ maps a block one-to-one to an adjacent weekend, by some appropriate definition of adjacency. For instance, in the above example we will have $\varphi(b) = 2b - 1$.

However, as it is, Q_3 is not a linear function of its variables and cannot be optimized in a linear programming framework. An approach used to convert such functions into linear objectives involves introducing a helper variable and additional constraints [ref ??]. In our case, introducing a variable $Z_{c,b,s}$ for every product $X_{c,b,s} \cdot Y_{c,w}$ with $w = \varphi(b)$, and constraining Z such that

$$Z_{c,b,s} \leq X_{c,b,s} \quad (1)$$

$$Z_{c,b,s} \leq Y_{c,w=\varphi(b)} \quad \forall s \in \mathcal{S} \quad (2)$$

allows us to rewrite Q_3 as a linear function of Z ,

$$Q_3(Z) = \sum_{c=1}^C \sum_{b=1}^B \sum_{s=1}^S Z_{c,b,s} \quad (3)$$

Indeed, whenever $X_{c,b,s} \cdot Y_{c,w} = 1$, $Z_{c,b,s}$ can attain a maximum value of 1, and whenever $X_{c,b,s} \cdot Y_{c,w} = 0$, at least one of $X_{c,b,s}$ or $Y_{c,w}$ must be 0, so $Z_{c,b,s}$ will be constrained to attain a maximum value of 0, giving us the correct adjacency maximization objective.

Thus, our clinician scheduling problem is a multiple objective optimization problem. The most common approach to solving multiple objective optimization problems is by optimizing a weighted sum of the normalized objective functions, as this guarantees the optimal solution to be Pareto optimal [ref ??]. This is the approach we decided to use in our problem, to ensure all three objectives are considered when finding a solution. Under the assumption that each clinician in \mathcal{C} provides all types of services in \mathcal{S} , the normalized objectives can be written as follows,

$$\bar{Q}_1(X) = \frac{Q_1(X)}{C \cdot B \cdot S} \quad (\text{Block Requests})$$

$$\bar{Q}_2(Y) = \frac{Q_2(Y)}{C \cdot W} \quad (\text{Weekend Requests})$$

$$\bar{Q}_3(Z) = \frac{Q_3(Z)}{C \cdot B \cdot S} \quad (\text{Block-Weekend Adjacency})$$

where we divide each of the original objective functions by the sum of the absolute values of its coefficients [ref ??]. The final weighted objective is given by

$$\alpha \bar{Q}_1(X) + \beta \bar{Q}_2(Y) + (1 - \alpha - \beta) \bar{Q}_3(Z) \quad (4)$$

with $0 \leq \alpha, \beta \leq 1$.

[...]

4 Results

4.1 Software

We developed a software package with a user interface that implements the above LP problem and allows configuration of clinicians at [ref ??], to be used by the ID division at St. Michael's Hospital. The software was used to generate the results in the following sections, using real data as well as simulated data as input.

4.2 Infectious Diseases Division

We used clinician time-off requests and minimum/maximum requirements from 2015-2018 as input data for the LP problem. Table 4 presents the optimal schedule generated using the software as well as the manually-created schedule for data from 2018. The schedule is color-coded to distinguish between the different clinicians assigned.

Week #	LP Solution			Historical Data		
	HIV	ID	Weekend	HIV	ID	Weekend
1	A	E	E	A	E	H
2	A	E	H	A	E	A
3	B	F	F	B	H	G
4	B	F	H	B	H	I
5	A	G	A	A	G	F
6	A	G	E	A	G	C
7	B	C	C	A	F	B
8	B	C	G	D	C	G
9	D	I	D	B	C	D
10	D	I	H	B	D	H
11	A	B	B	A	B	F
12	A	B	I	A	B	A
13	C	F	F	C	H	H
14	C	F	I	C	H	I
15	A	H	H	B	I	C
16	A	H	D	B	I	E
17	B	E	B	A	E	D
18	B	E	H	A	E	E
19	A	I	I	A	C	F
20	A	I	D	A	C	C
21	C	D	C	B	G	A
22	C	D	I	B	G	C
23	B	F	F	C	F	D
24	B	F	G	C	F	C
25	A	H	A	C	C	G
26	A	H	H	D	I	D
27	C	D	D	A	B	E
28	C	D	E	A	B	I
29	A	B	A	B	D	D
30	A	B	B	B	D	A
31	C	E	C	C	F	E
32	C	E	A	C	F	F
33	B	D	D	B	F	I
34	B	D	E	B	I	C
35	A	I	A	A	G	G
36	A	I	G	A	G	I
37	D	C	C	D	C	A
38	D	C	F	D	D	E
39	B	E	E	A	B	D
40	B	E	B	B	I	I
41	A	G	G	B	I	G
42	A	G	E	D	F	F
43	C	I	C	C	F	C
44	C	I	I	D	E	I
45	A	F	A	D	E	E
46	A	F	F	A	B	A
47	B	G	B	A	B	D
48	B	G	I	A	D	G
49	D	C	D	A	D	F
50	D	C	B	B	G	G
51	B	G	G	B	G	E

Table 4: Comparison of schedules for 2018

First, we evaluated the software-generated schedule by comparing it with the manually-created schedule. Specifically, we examined the adherence of each schedule to the constraints presented in table 1. As shown in table 5, the optimal schedule generated using the software satisfied all mandatory constraints. In contrast, the manually-created schedule was not able to satisfy all mandatory constraints. In particular, we see that the manual schedule assigned clinicians to multiple consecutive blocks in all four years. Moreover, the manual schedule did not have an equal distribution of weekends and holidays for all four years of data. Evaluating the objectives, we see that LP outperforms the manually created schedule in all four years, by accommodating almost all time-off requests and ensuring that weekends are always assigned close to blocks.

	2015		2016		2017		2018	
	LP	Historical	LP	Historical	LP	Historical	LP	Historical
Constraint								
Block Coverage	✓	✓	✓	✓	✓	✓	✓	✓
Weekend Coverage	✓	✓	✓	✓	✓	✓	✓	✓
Min/Max	✓	✓	✓	✓	✓	✓	✓	✓
No Consecutive Blocks	✓		✓		✓		✓	
No Consecutive Weekends	✓		✓		✓	✓	✓	✓
Equal Weekends	✓		✓		✓		✓	
Equal Holidays	✓		✓	✓	✓		✓	✓
Objective								
Satisfied Block Requests	123/129	121/129	120/126	116/126	99/99	95/99	124/128	121/128
Satisfied Weekend Requests	113/113	111/113	119/119	112/119	75/75	75/75	115/115	113/115
Adjacent Block-Weekend Assignments	26/26	9/26	26/26	6/26	26/26	7/26	26/26	5/26

Table 5: Comparison of constraint satisfaction and objectives in LP-generated and historical schedules

4.3 Simulations

We then examined the properties of the LP problem using simulated data. Specifically, we examined the influence of expanding the following parameters on the runtime of the algorithm: number of clinicians; number of services offered in the division; amount of time-off requests per clinician throughout the year. We also examined the effect of a longer time-horizon on the runtime.

The effect of an increasing number of requests per clinician on the runtime of the LP solver is shown in figure 1. We executed the program on a department with 10 clinicians offering two services, similar to the department at St. Michael’s Hospital. For simplicity, each clinician was configured with $|\mathcal{BR}| = \{0, 5, 10, 15\}$ non-overlapping block requests. The increase in the number of requests did not affect the runtime of the LP solver, indicating that it can accommodate a lot of flexibility in clinician requests. Moreover, we see that all four runs were completed in under 1 second.

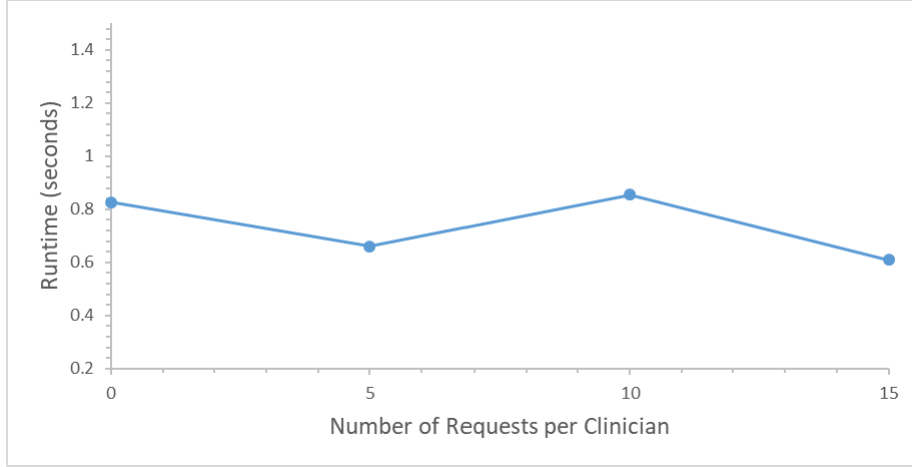


Figure 1: Runtime of LP solver with an increasing number of requests per clinician

Figure 2 presents the change in runtime when increasing the number of 2-week blocks $B = \{26, 52, 78, 104\}$ in a department with 10 clinicians offering two services. There does not seem to be a strong effect on runtime when we lengthen the time-horizon of the schedule, and in fact the solver was able to find an optimal schedule for all time horizons within 3 seconds.

The effect of increasing the number of services on the runtime of the program is shown in Table 6. We executed the algorithm for $S = \{1, 2, 3\}$ total services and $C = \{10, 20, 30, 50\}$ clinicians in total across all services. For 2 concurrent services, a roster of 30 or more clinicians becomes impractical to schedule, as

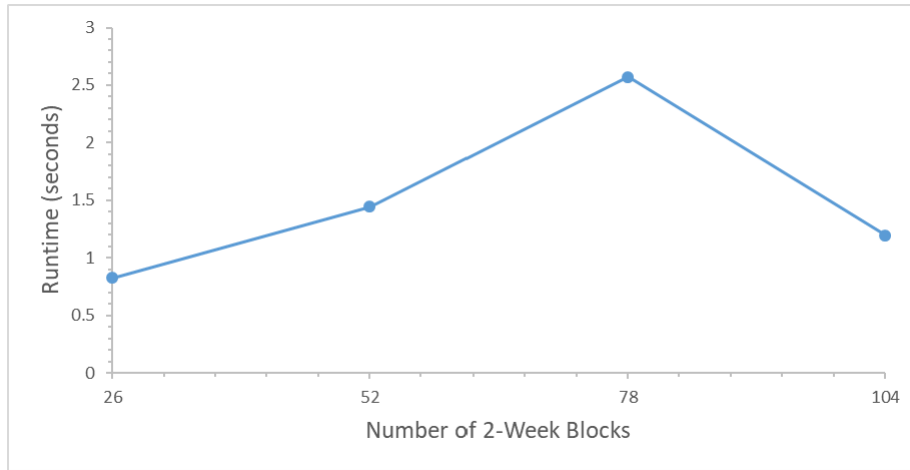


Figure 2: Runtime of LP solver with an increasing number of 2-week blocks

searching for a solution requires over 24 hours. We see similar issues for a roster of 20 or more clinicians assigned to a division with 3 concurrent services. However, when relaxing the ‘No Consecutive Blocks’ constraint, we see a great improvement in runtime for divisions with 2 and 3 services, and we are able to generate a schedule with upwards of 50 clinicians in under 1.5 seconds.

Number of Clinicians	Number of Services				
	1	2	2 (CBA)	3	3 (CBA)
10	0.16	0.74	0.16	1.40	0.23
20	0.25	7468.86	0.32	-	0.43
30	0.42	-	0.49	-	0.66
50	0.62	-	0.82	-	1.14

Table 6: Comparison of program runtime (in seconds) for different number of services and total clinicians in the division. ‘-’ indicates that a solution was not found after 24 hours. ‘CBA’ indicates that consecutive blocks were allowed when generating these schedules.

5 Discussion

In this paper our goal was to develop a rather simple, yet flexible, integer linear programming formulation to generate schedules for clinical departments at hospitals. The difficulty in applying such an approach to this task lies in the fact that ILP is an NP-hard problem, and as such, the time to find an optimal solution grows exponentially as we increase the size of the problem. As a result, the vast majority of approaches taken to create schedules for similar scenarios tend to use heuristics in order to find an approximately optimal solution in a shorter time.

Our formulation includes hard constraints to ensure the schedule satisfies hospital and logistics requirements. It also aims to satisfy the work preferences of clinicians in a clinical department by optimizing a multi-goal objective function [...]

We developed a tool that implements the ILP formulation and generates an optimal schedule based on provided input data. It provides a simple and easy-to-use user interface that can be used by any hospital staff to generate schedules well in advance. We compared the optimal schedule generated with the help of the tool to the manually-created schedules at St. Michael’s Hospital. We found that the ILP formulation was always able to find an optimal schedule satisfying all required hard constraints, unlike the manual schedule, that often did not take all constraints into account. Moreover, due to the multi-goal objective function in the ILP, the tool was able to maximize and fulfill the majority of clinician preferences and requests, more so than the manually-created schedule. These observations reinforce the idea that it is vital to employ automated tools when generating schedules in hospital departments, to reduce human error, balance the work-load of clinicians and improve the service provided to patients.

We analyzed the performance of our formulation on simulated data meant to resemble real-life clinician departments at different hospitals. Our results show that increasing the number of requests per clinician does not affect the runtime of the algorithm, highlighting the flexibility of the tool in incorporating clinician preferences. Further, we saw that the algorithm can accommodate increasing the time-horizon up to four years with little impact on runtime, which can be applied to departments that generate schedules far in advance. The most notable impact on the runtime was noticed when trying to increase the number of services offered in a single department. While such cases are unlikely to be encountered in the real-world, as most departments tend to focus on a single service [ref ??], the runtime issues can be mitigated by relaxing certain constraints.

In future work, we can look first and foremost into improving the runtime of the tool by modifying constraints and objectives, so that it can be used in larger departments offering multiple services for their patients. On top of that, we can introduce new objectives that incorporate additional clinician preferences and

allow for better distribution of work-load. However, since our ultimate goal is to maintain a ILP formulation, care must be taken not to overly complicate the model and risk running into additional time complexity issues.