

Signals and Circuits

AERN 35500

Passive Filters and resonance

Chapter 10: 10-8(Basic applications) pp. 473-477

Chapter 12: 12-8(Basic applications) pp. 561-563

Chapter 13: 13-4 (series Resonant Filter) pp. 595-603

Text books:

Floyd, T. L., and Buchla, D. M., *Electroics Fundamentals: Circuits, Devices & Applications*, 8th Edition, Pearson, 2009.



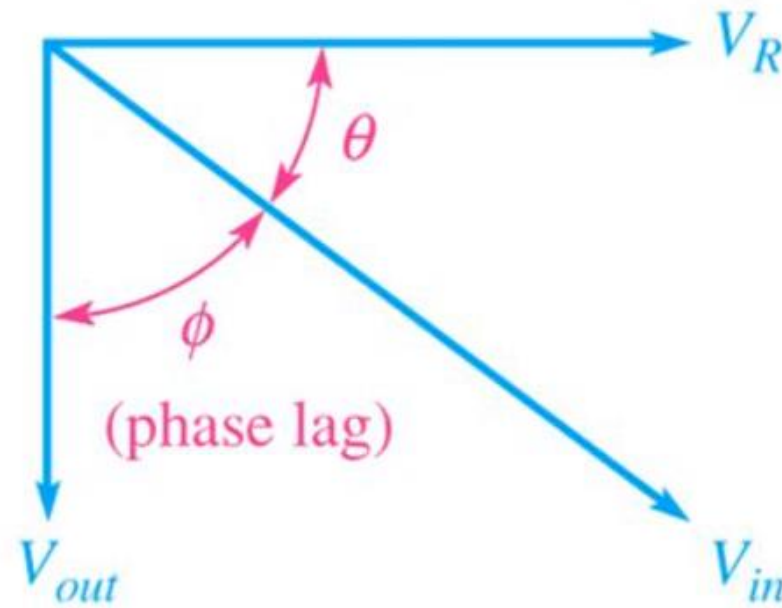
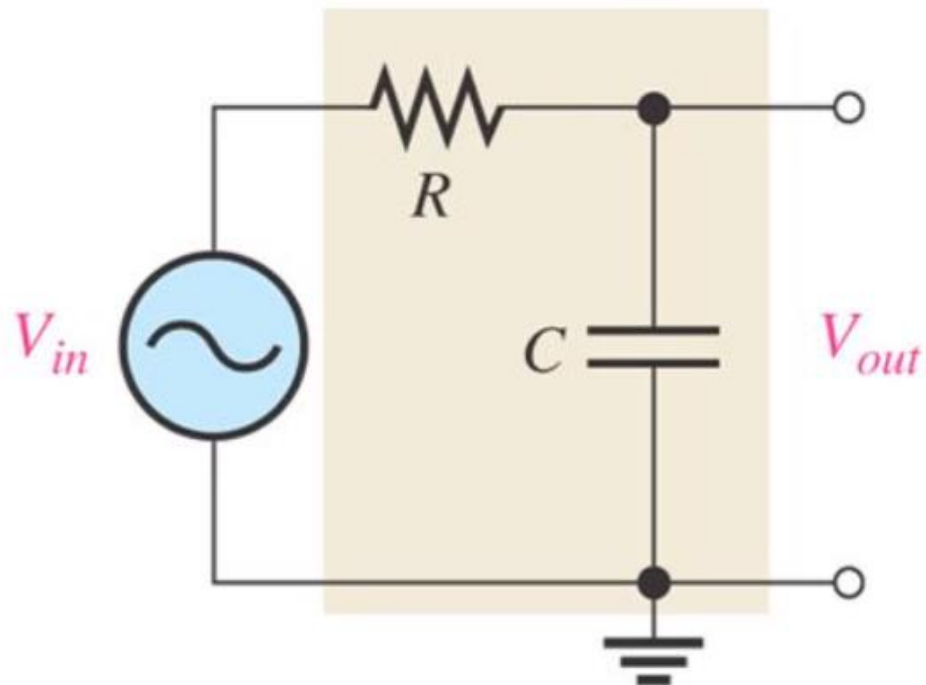
Filter

A circuit that discriminates among frequencies, attenuating (weakening) some while allowing others to pass.

They usually consist of a capacitor and/or an inductor connected in series to a resistor.

The output voltage is taken either from the reactive or the resistive element in the circuit.

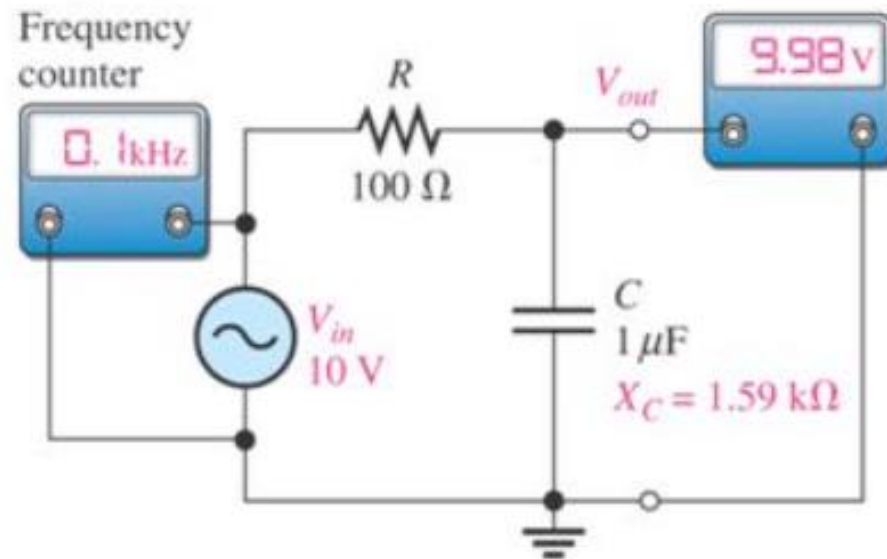
Passive filter



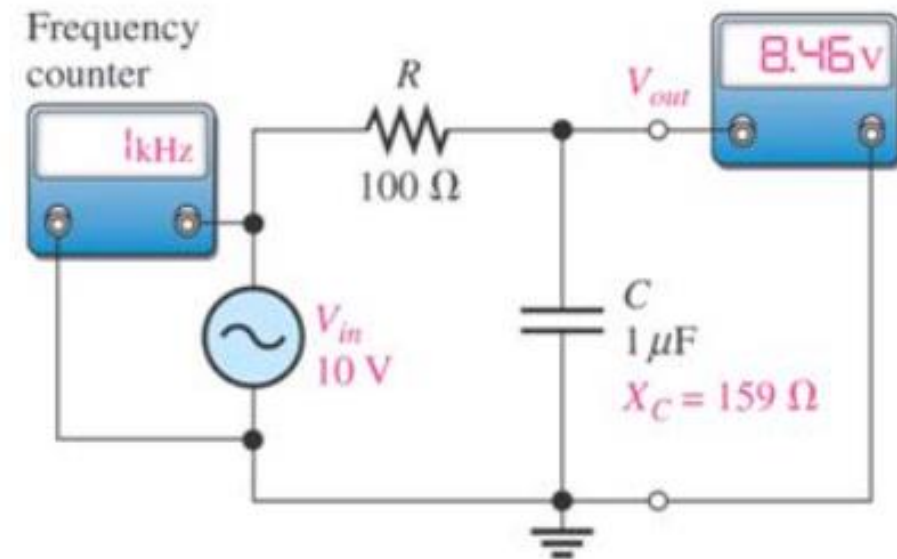
$$V_{out} = \frac{X_C V_{in}}{\sqrt{R^2 + X_C^2}}$$

$$X_C = \frac{1}{2\pi fC}$$

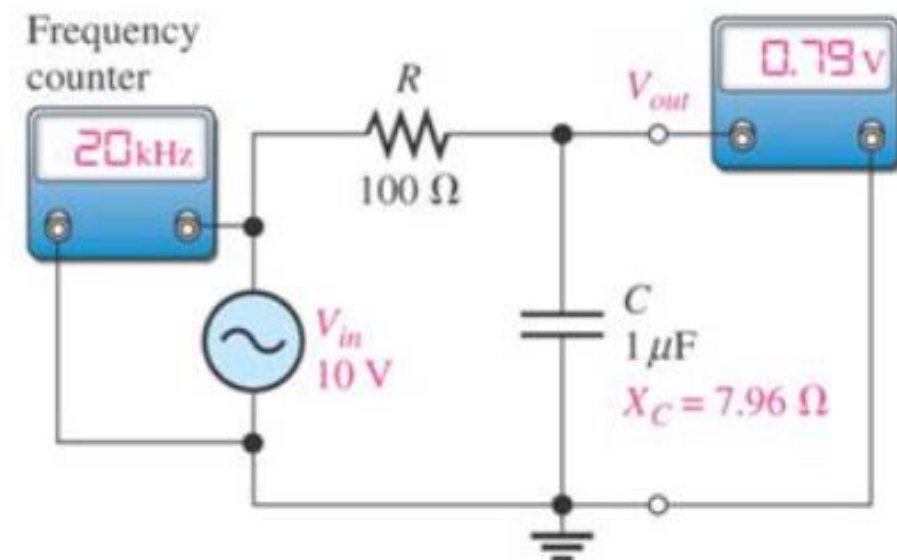
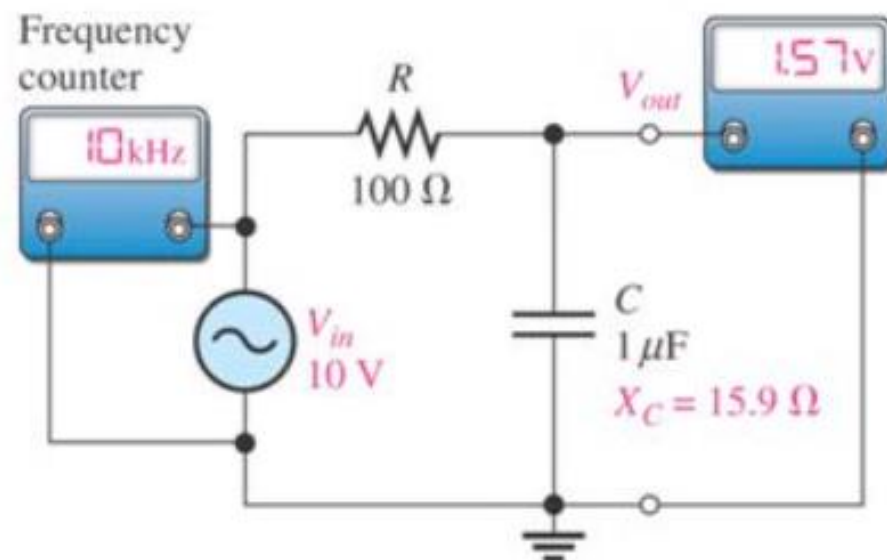
Passive filter



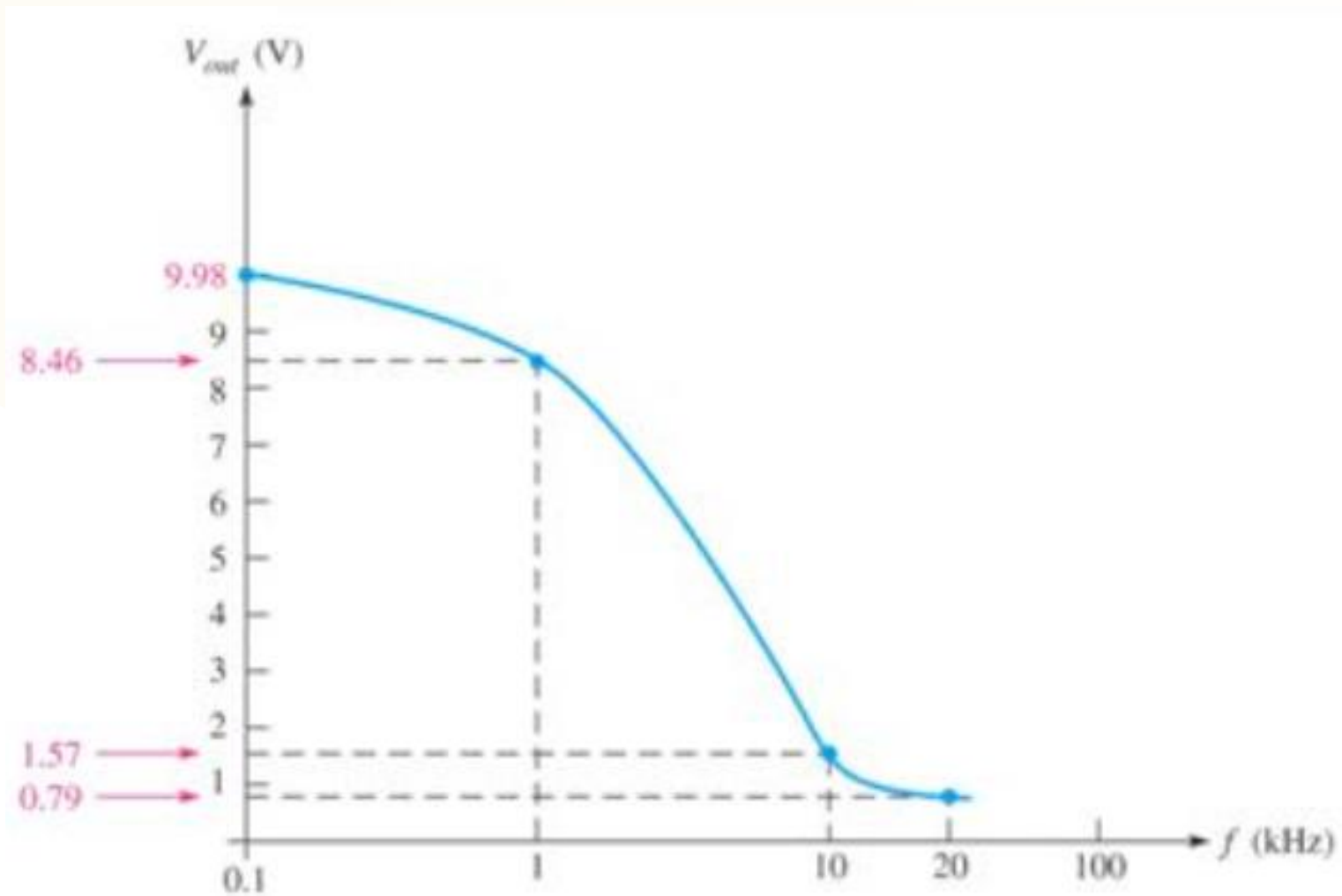
(a) $f = 0.1 \text{ kHz}$, $X_C = 1.59 \text{ k}\Omega$, $V_{out} = 9.98 \text{ V}$



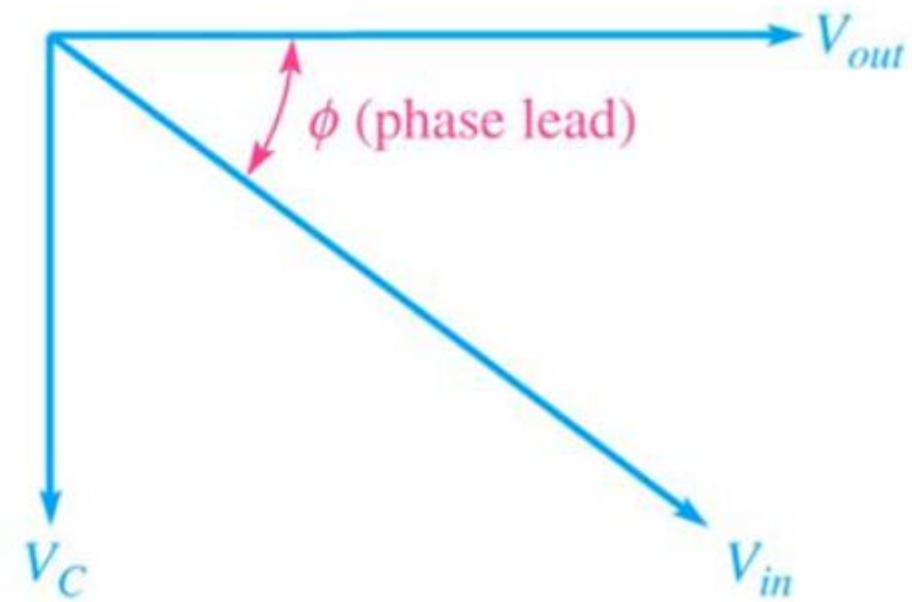
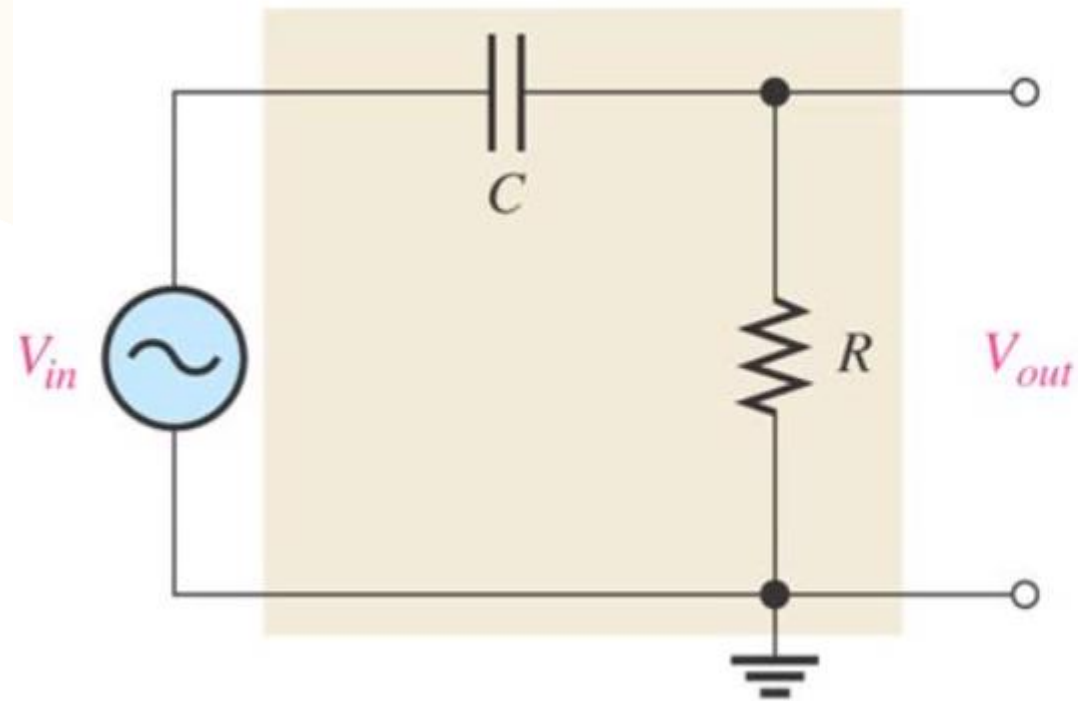
(b) $f = 1 \text{ kHz}$, $X_C = 159 \Omega$, $V_{out} = 8.46 \text{ V}$



Passive filter



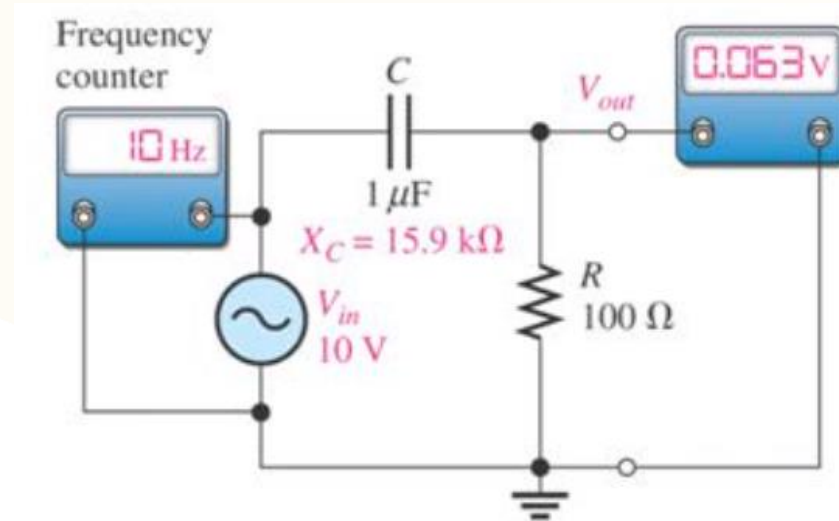
Passive filter



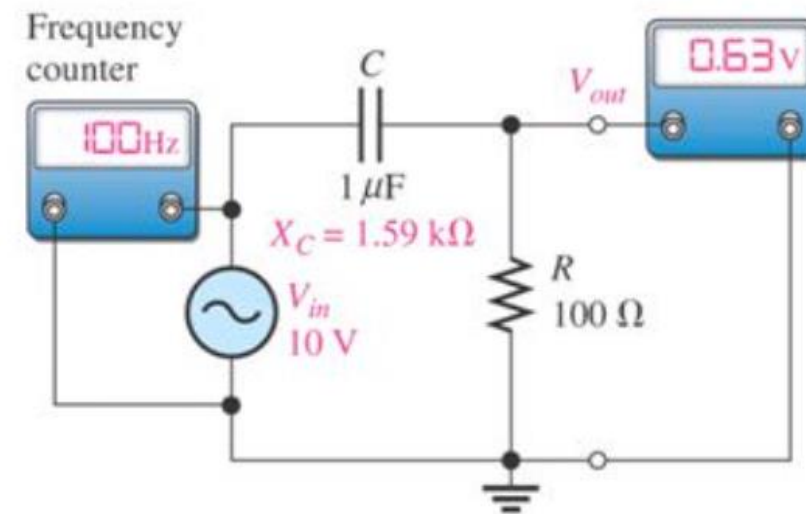
$$V_{out} = \frac{RV_{in}}{\sqrt{R^2 + X_C^2}}$$

$$X_C = \frac{1}{2\pi fC}$$

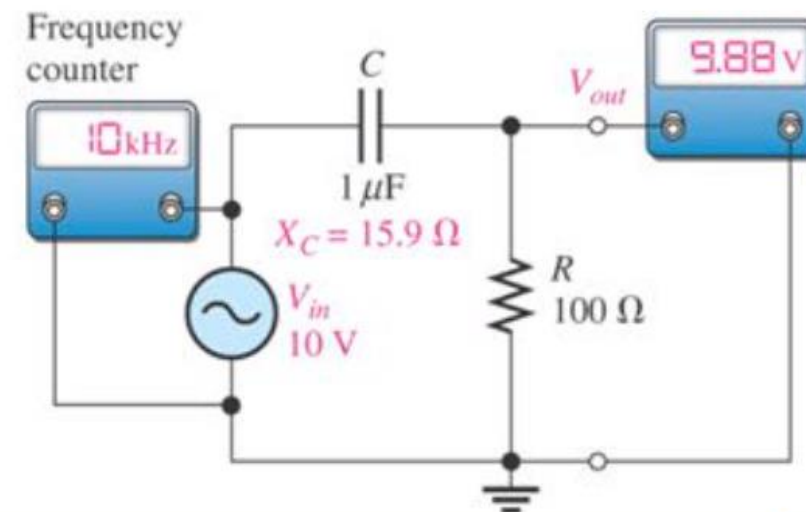
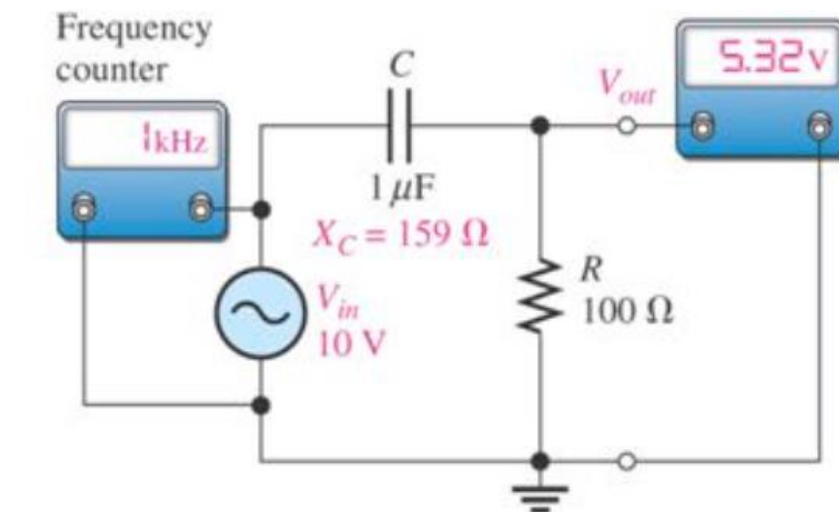
Passive filter



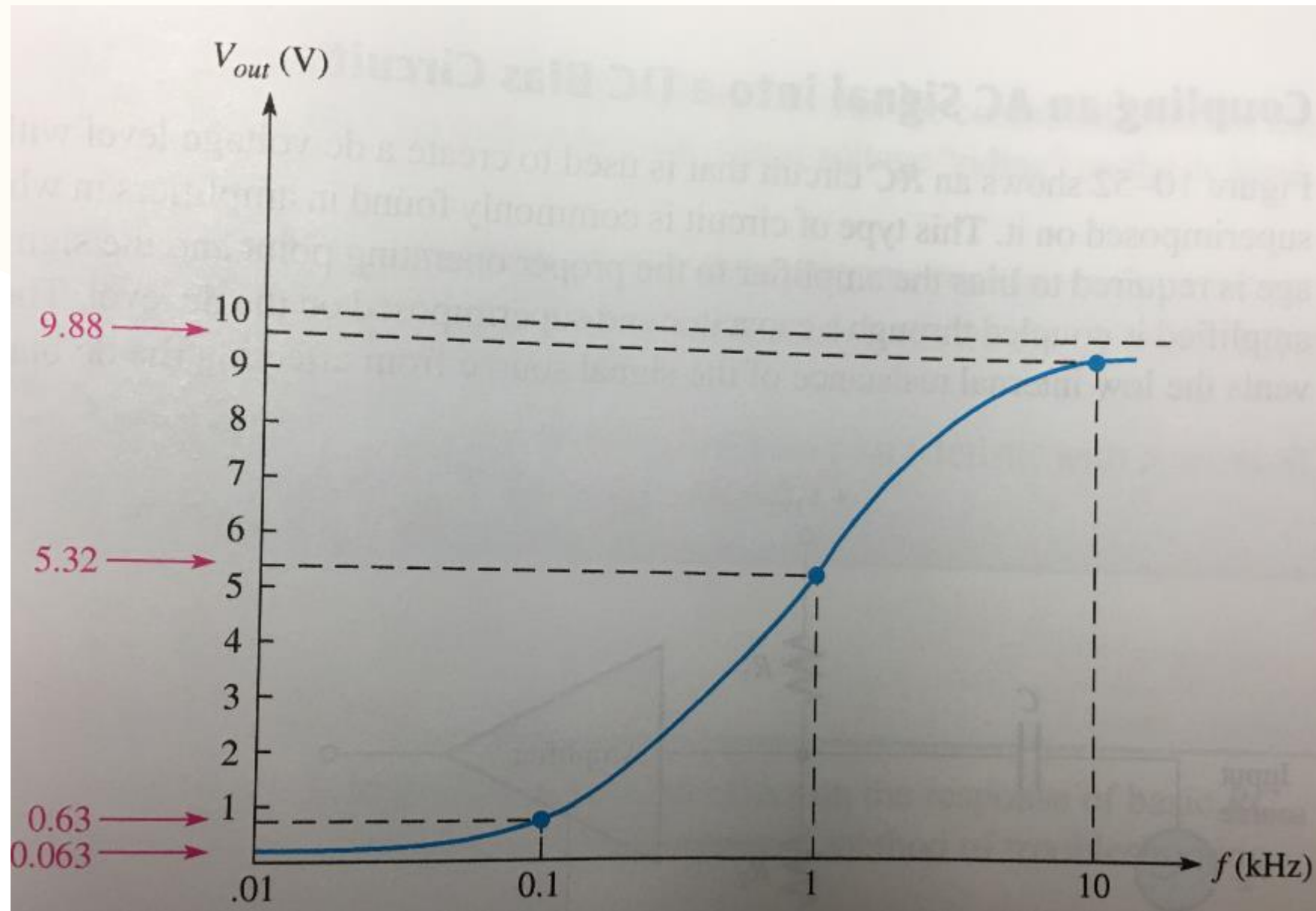
(a) $f = 10 \text{ Hz}$, $X_C = 15.9 \text{ k}\Omega$, $V_{out} = 0.063 \text{ V}$



(b) $f = 100 \text{ Hz}$, $X_C = 1.59 \text{ k}\Omega$, $V_{out} = 0.63 \text{ V}$

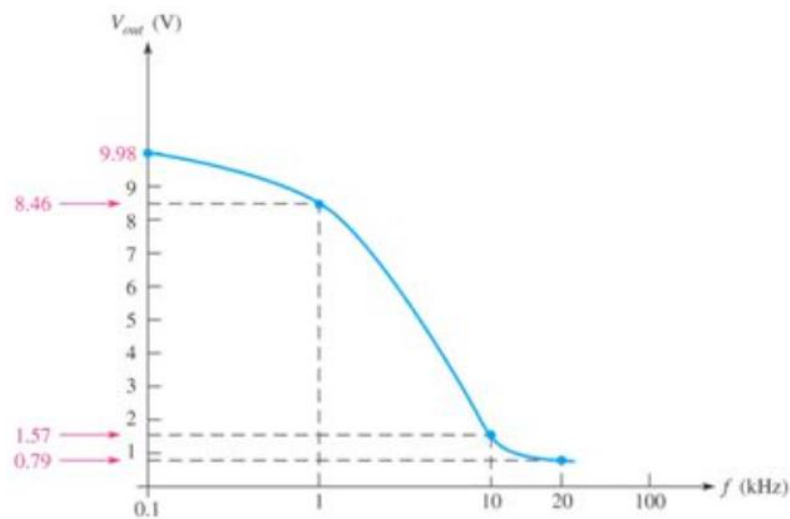
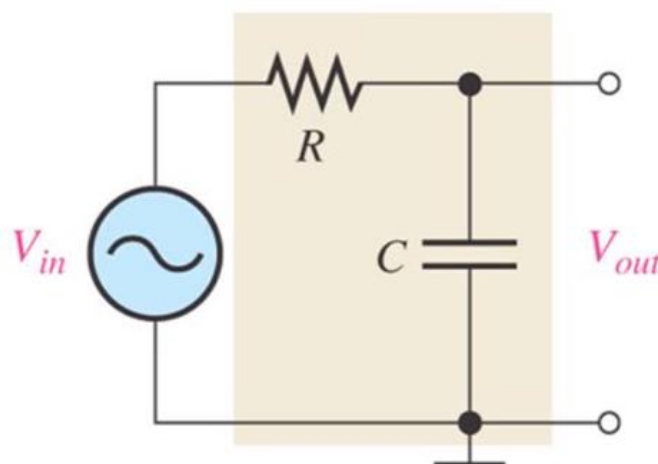


Passive filter



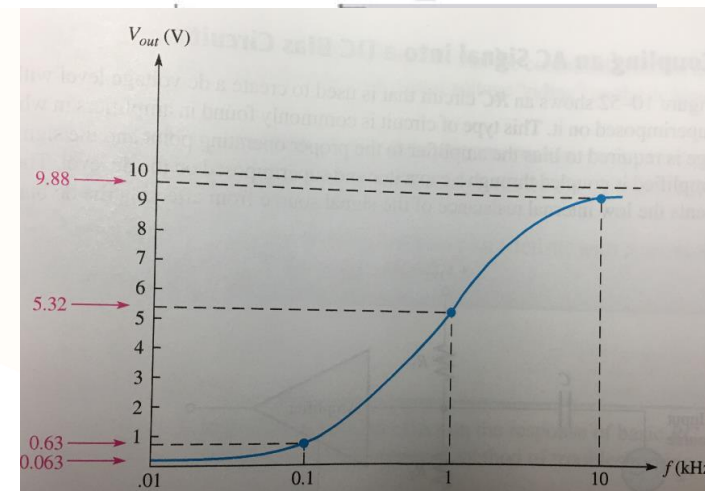
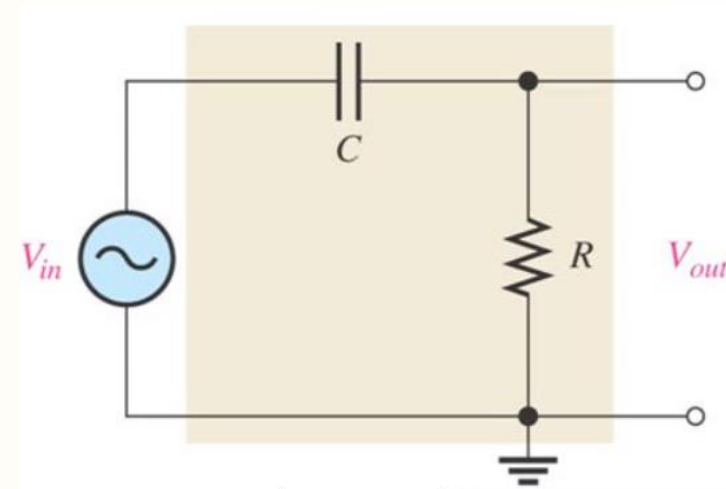
Passive filter

Passive RC filter



RC low-pass filter

A **low-pass circuit** is realized by taking the output across the capacitor, just as in a **lag network**

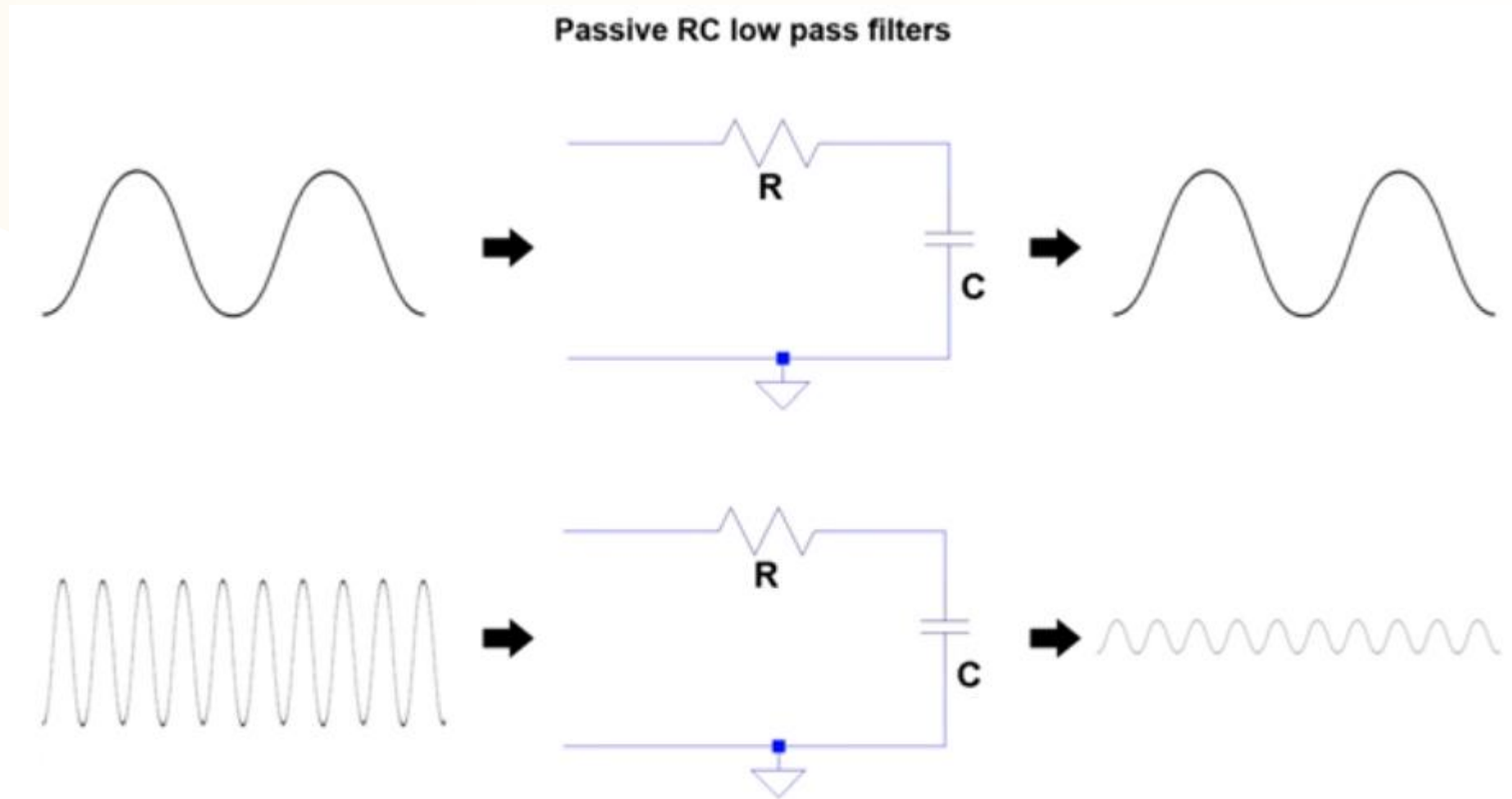


RC High-pass filter

A **high-pass circuit** is implemented by taking the output across the resistor, as in a **lead network**

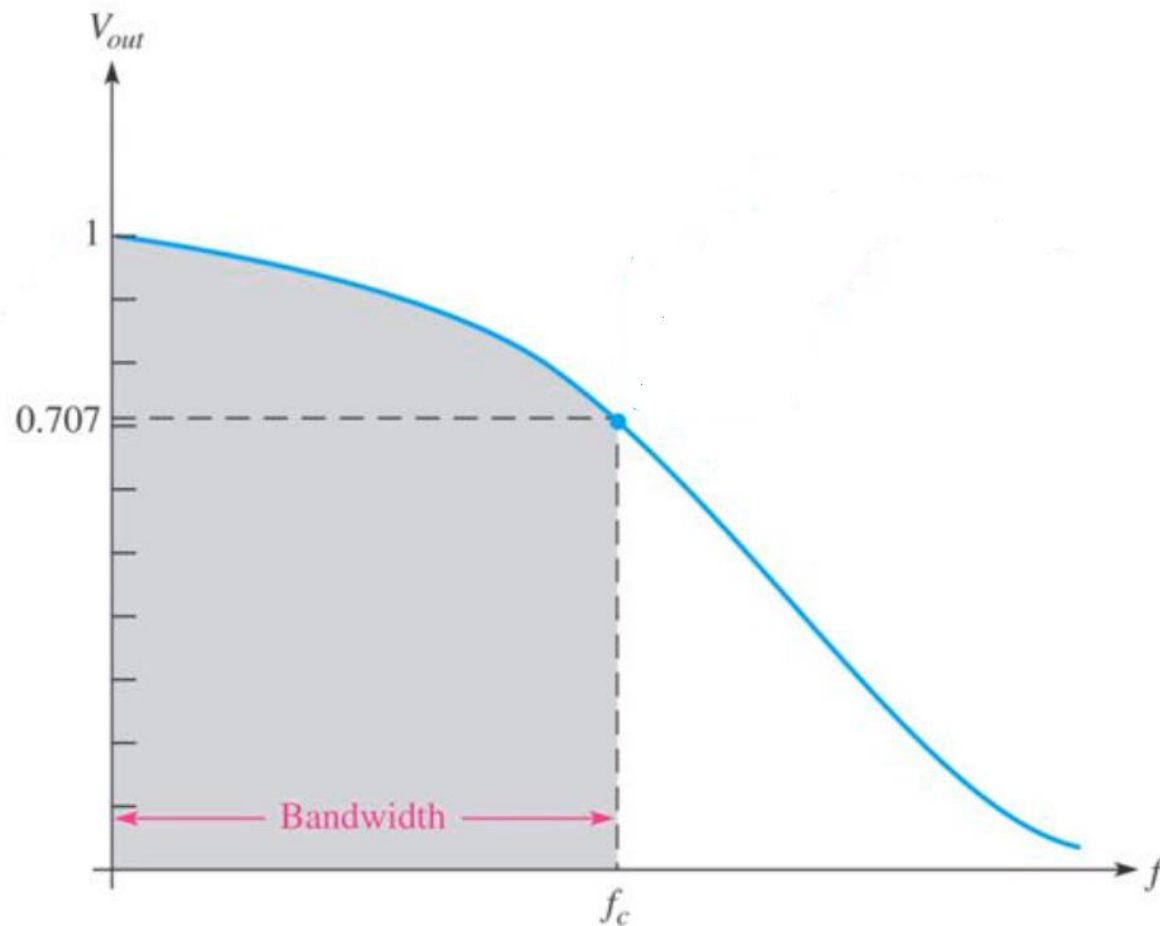
Passive filter

E. g.



Passive filter

passive RC filter



RC low-pass filter

Cut-off frequency

$$R = X_C = \frac{1}{2\pi C f_c}$$

$$f_c = \frac{1}{2\pi RC}$$

$$\theta = 45^\circ$$

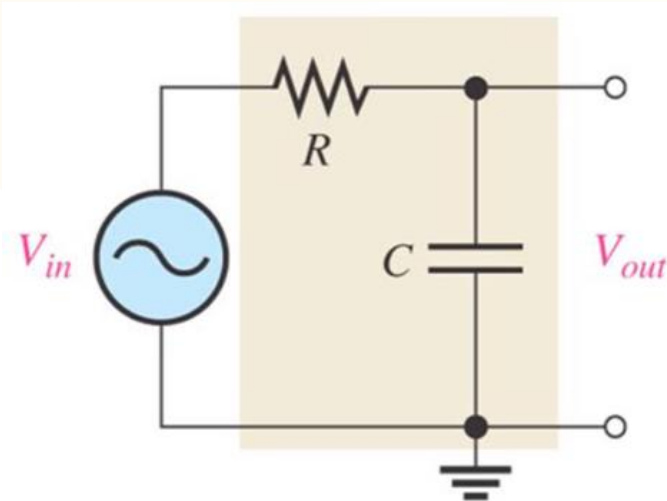
Bandwidth

The range of frequencies that is considered to be passed from the input to the output a circuit is called a bandwidth.

Passive filter

passive RC filter

E. G.



Note: Cut-off frequency

$$R = X_C = \frac{1}{2\pi C f_c} \quad f_c = \frac{1}{2\pi RC}$$

$$V_{out} = \frac{X_C V_{in}}{\sqrt{R^2 + X_C^2}}$$

$$R = 3.9k\Omega$$

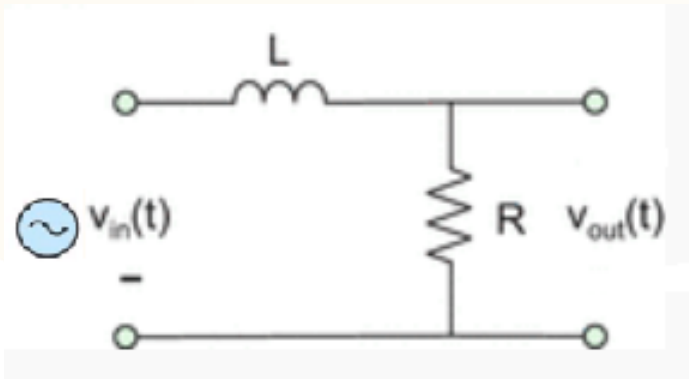
V_{in} amplitude is 1v

$$C = 0.039 \mu F$$

Draw a response curve for this circuit by plotting the output voltage versus frequency for 0 Hz to 10 KHz in 1 kHz increments.

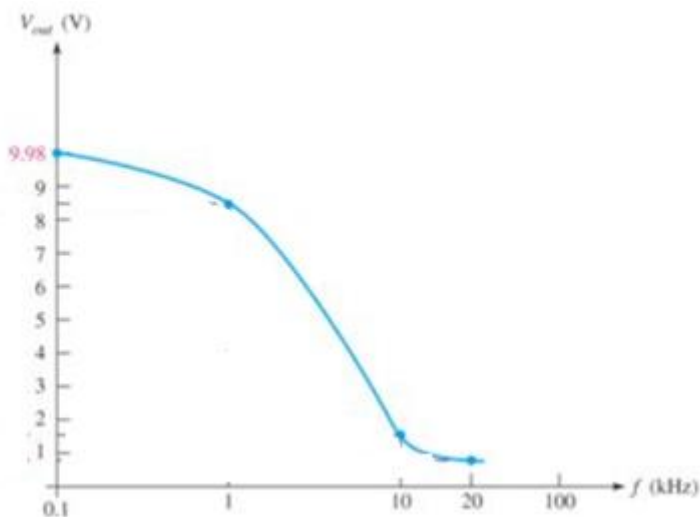
Passive filter

RL passive filter

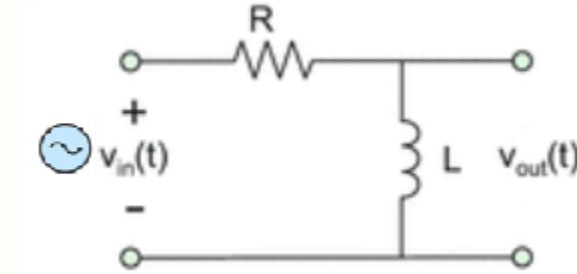


$$V_R = \frac{RV_S}{\sqrt{R^2 + X_L^2}}$$

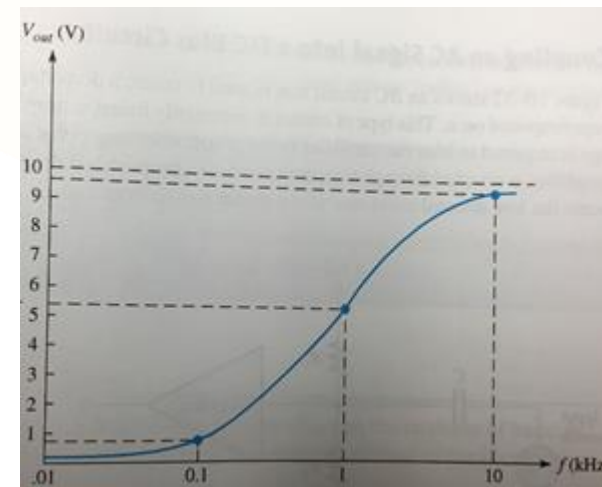
$$X_L = 2\pi Lf$$



RL low-pass filter



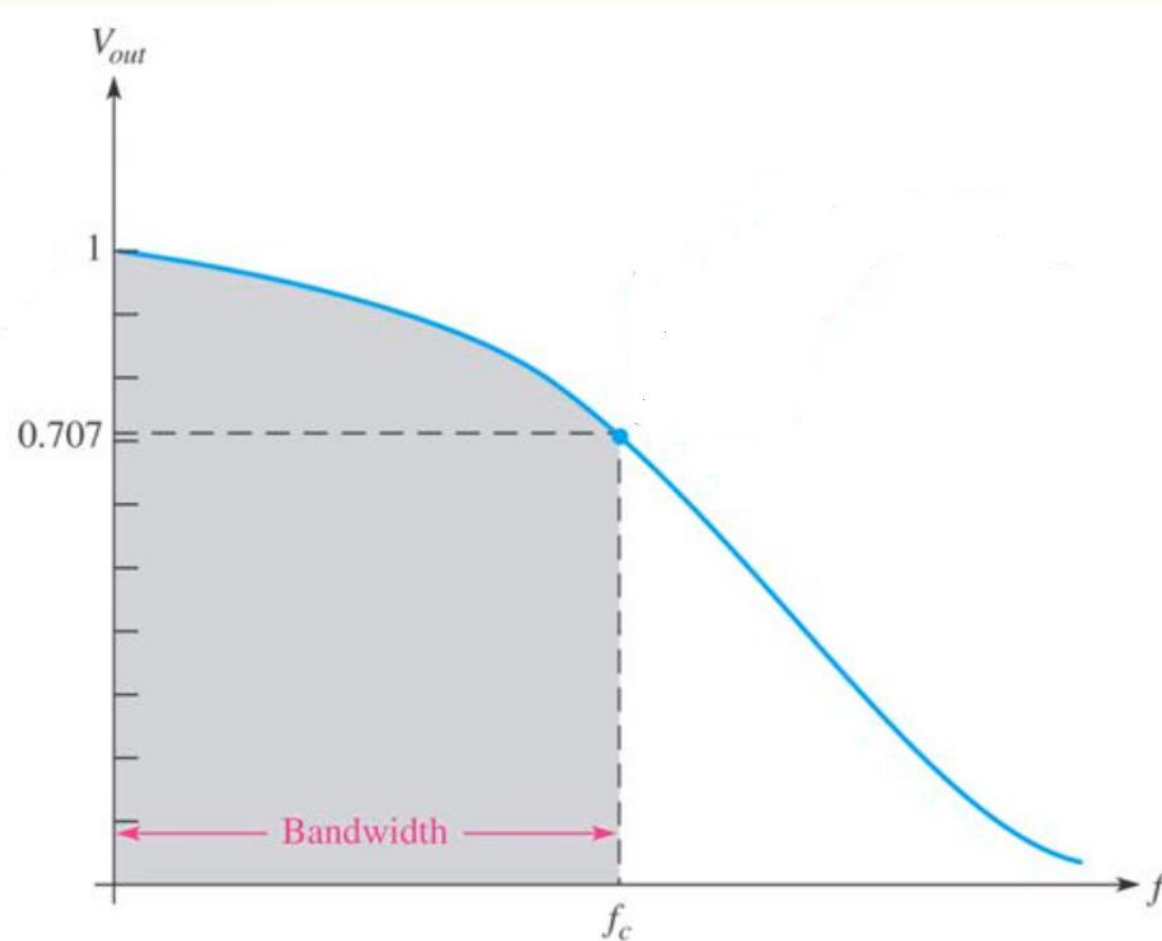
$$V_L = \frac{X_L V_S}{\sqrt{R^2 + X_L^2}}$$



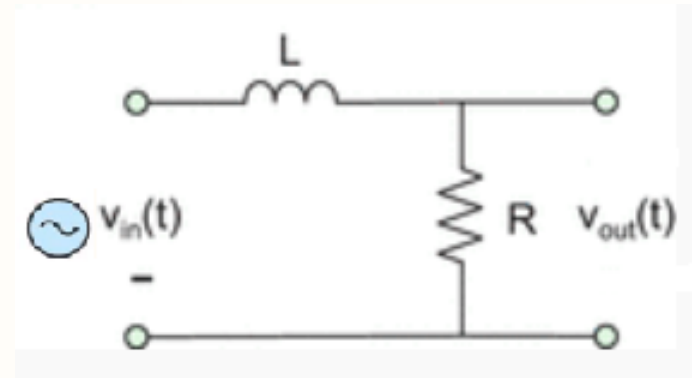
RL High-pass filter

Passive filter

Passive RL filter



RL low-pass filter



Cut-off frequency

$$R = X_L = 2\pi L f_c$$

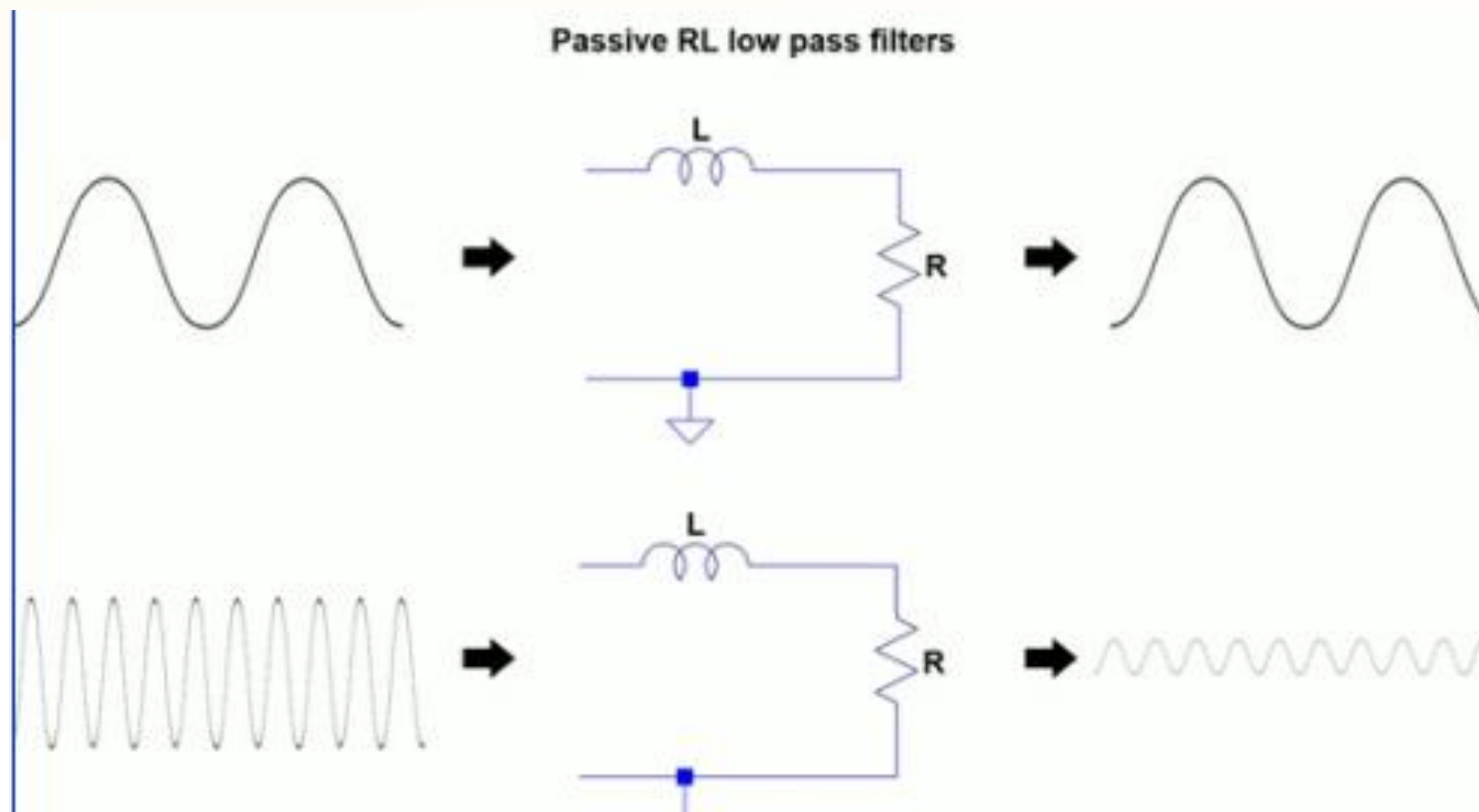
$$f_c = \frac{R}{2\pi L}$$

$$\theta = 45^\circ$$

Passive filter

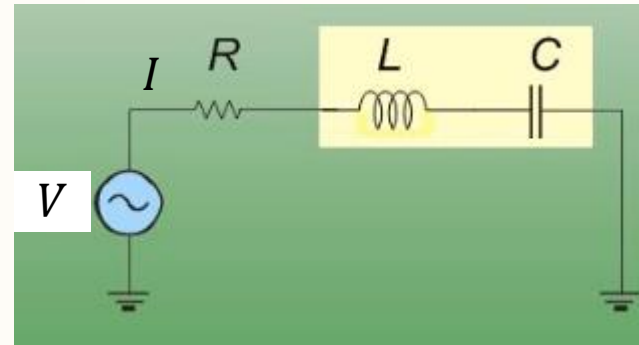
Passive RL filter

E. g.

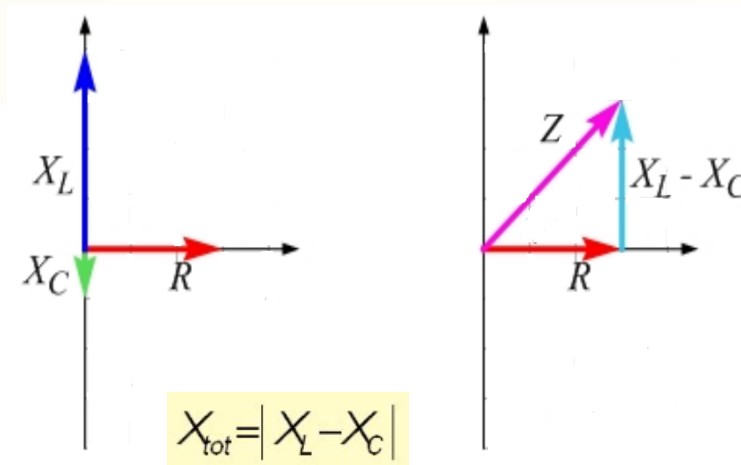


Resonance

RCL impedance



Impedance triangle



$$X_{\text{tot}} = |X_L - X_C|$$

$$Z_{\text{tot}} = \sqrt{R^2 + X_{\text{tot}}^2}$$

$$\theta = \tan^{-1}\left(\frac{X_{\text{tot}}}{R}\right)$$

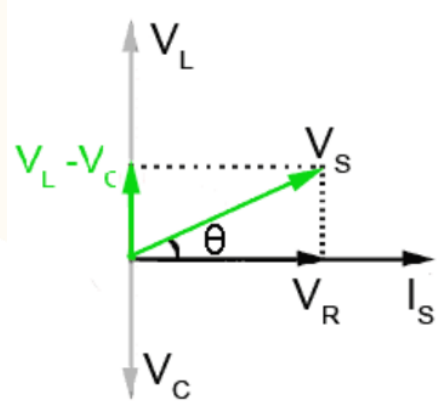
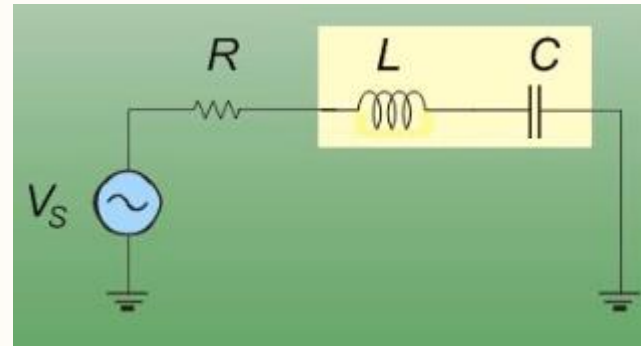
voltage leads current by θ if $X_L > X_C$

voltage lags current by θ if $X_L < X_C$

Figures: <https://slideplayer.com/slide/6379082/>

Resonance

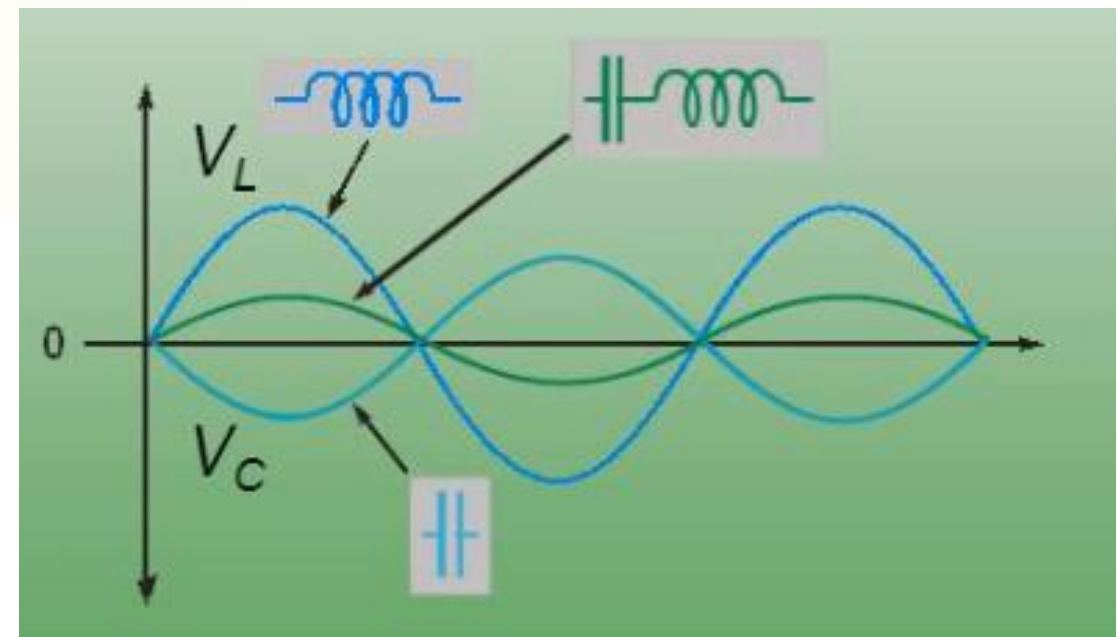
RCL voltage



V_L and V_C always has 180 degree phase difference.

E. G.

$$V_L > V_C$$



$$V_R = \frac{RV_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$V_L = \frac{X_L V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$V_C = \frac{X_C V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

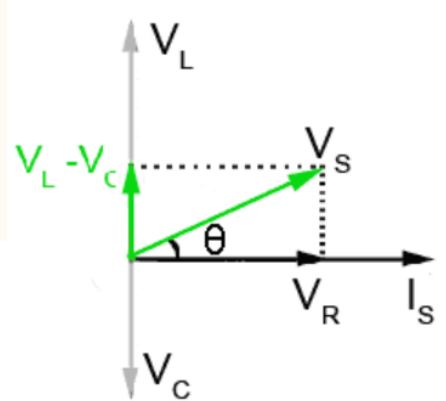
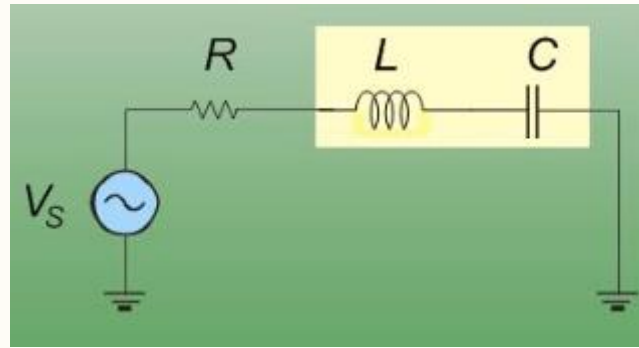
$$V_{LC} = \frac{|X_L - X_C| V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

Source voltage leads current by θ if $X_L > X_C$

Source voltage lags current by θ if $X_L < X_C$

Phase angle among I , V_R , V_L , V_C , and V_{LC} ?

Figures: <https://slideplayer.com/slide/6379082/>



V_C and V_L always has 180 degree phase angle

$$V_R = \frac{RV_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$V_L = \frac{X_L V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$V_C = \frac{X_C V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

$$V_{LC} = \frac{|X_L - X_C| V_S}{\sqrt{R^2 + (X_L - X_C)^2}}$$

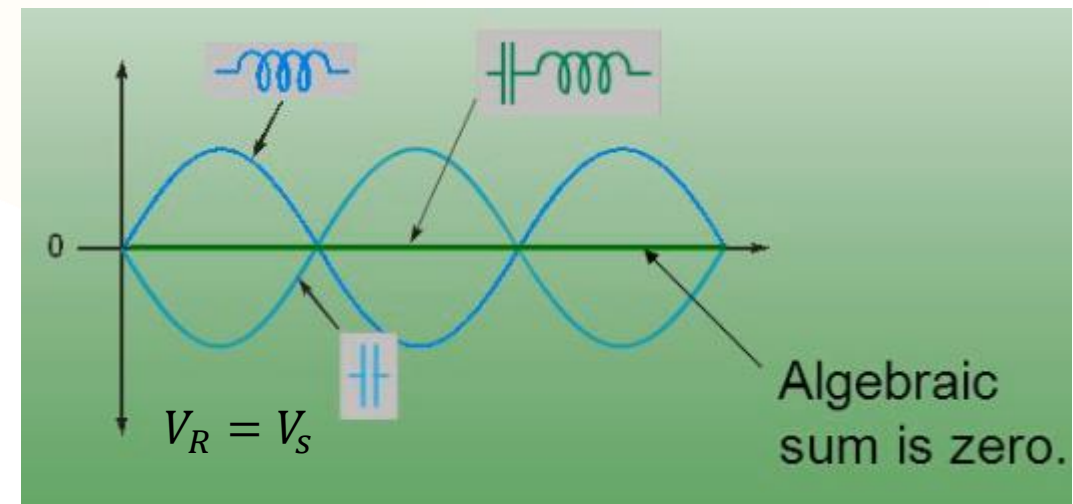
Source voltage leads current by θ if $X_L > X_C$

Source voltage lags current by θ if $X_L < X_C$

Phase angle among I , V_R , V_L , V_C , and V_{LC} ?

When $X_L = X_C$?

Resonance



$$V_L = V_C = \frac{X_L V_S}{R}$$

$$V_{LC} = 0$$

Source voltage leads current by 0 degree

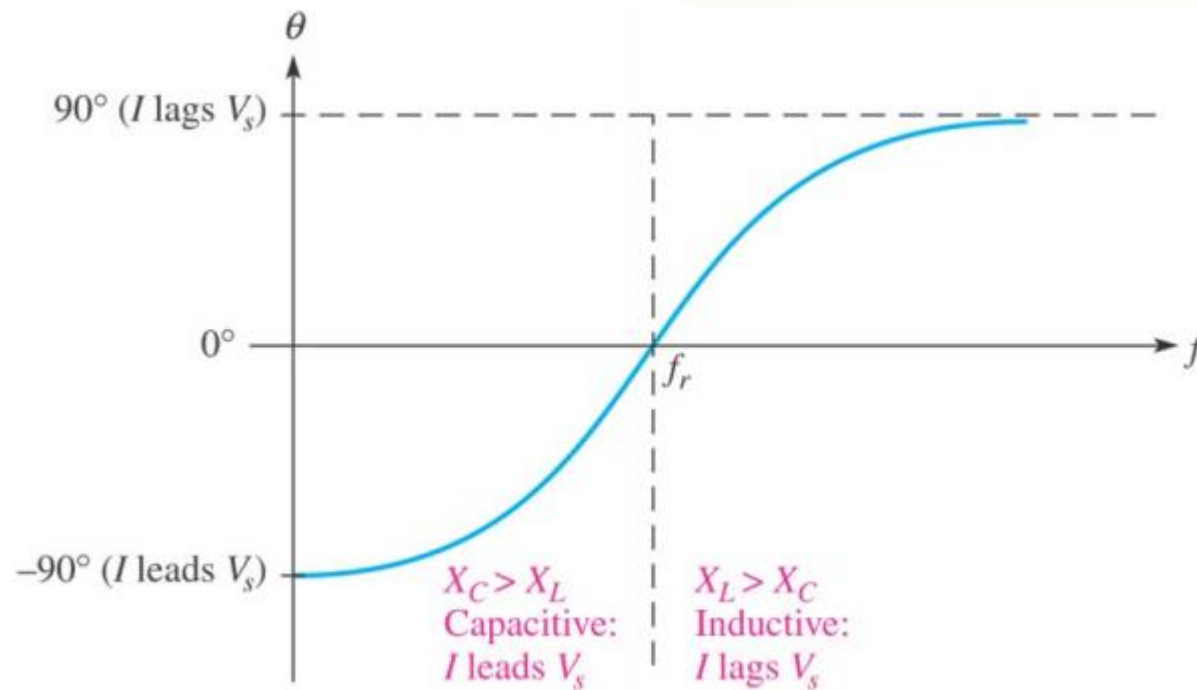
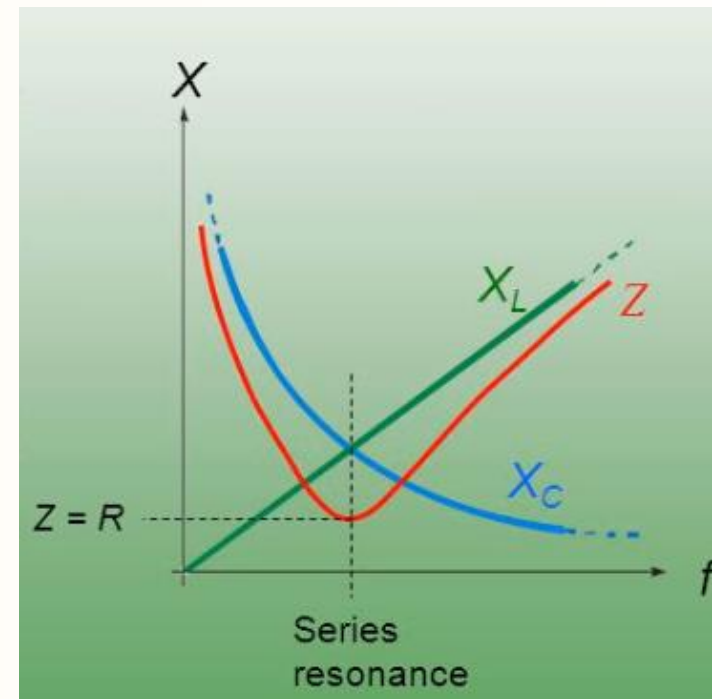
$$Z = R$$

Resonance

when $X_L = X_C$ Resonance

$$2\pi L f_r = \frac{1}{2\pi C f_r}$$

Resonant frequency $f_r = \frac{1}{2\pi\sqrt{LC}}$



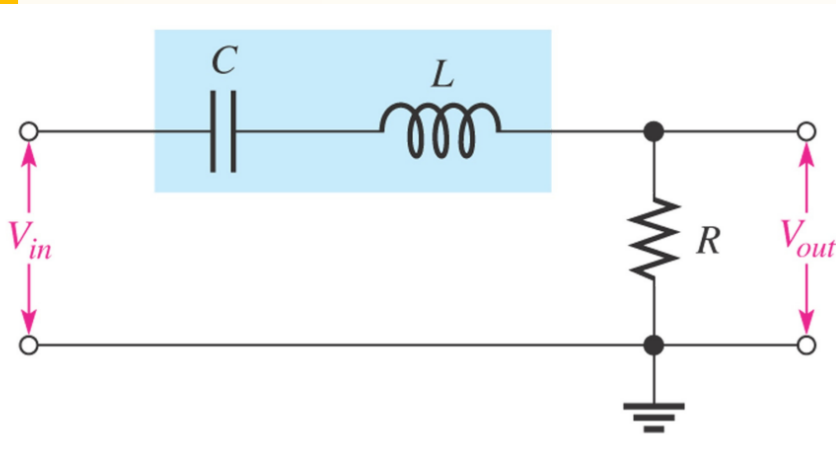
Phase angle versus frequency.

Figures: text books

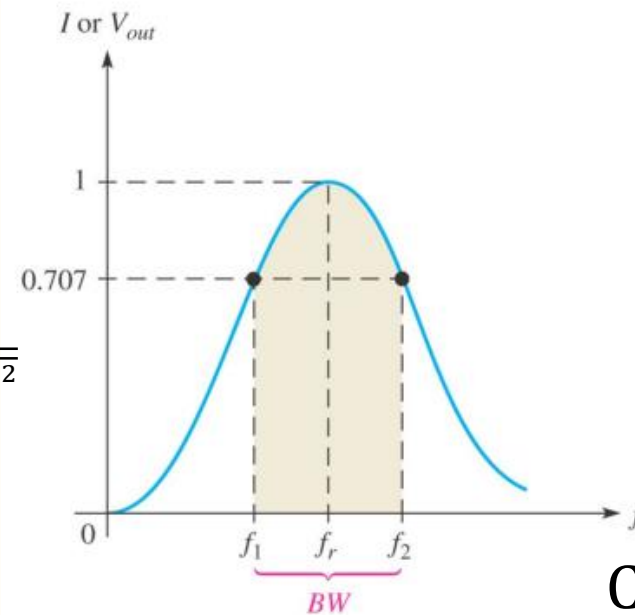
<https://slideplayer.com/slide/6379082/>

Resonance

Resonant band-pass filter



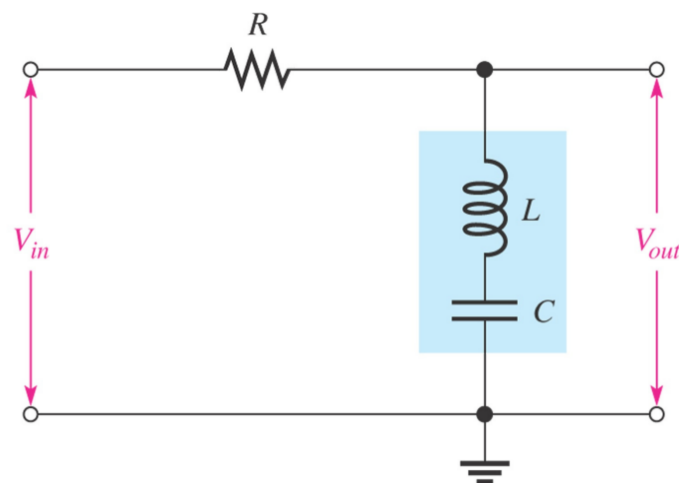
$$V_R = \frac{RV_s}{\sqrt{R^2 + (X_L - X_C)^2}}$$



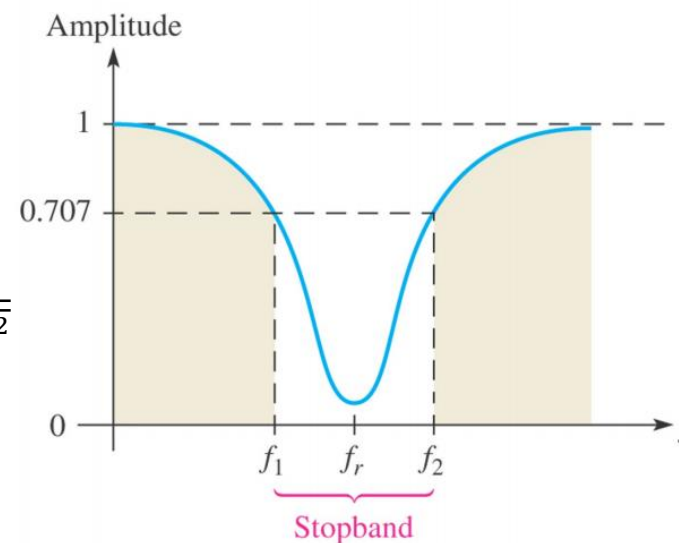
Cutoff frequency:
 when $R = |X_L - X_C|$
 f_1 is the lower cutoff frequency;
 f_2 is the upper cutoff frequency.

$$\text{Bandwidth} = f_2 - f_1$$

Resonant band-stop filter



$$V_{LC} = \frac{|X_L - X_C|V_s}{\sqrt{R^2 + (X_L - X_C)^2}}$$



Resonance

Note: Cutoff frequency:

$$\text{when } R = |X_L - X_C| \quad X_C = \frac{1}{2\pi Cf}$$

f_1 is the lower cutoff frequency;
 f_2 is the upper cutoff frequency. $X_L = 2\pi Lf$

$$\text{Bandwidth} = f_2 - f_1$$

$$R = 51\Omega$$

$$C = 0.0047\mu F$$

$$L = 10\text{ mH}$$

Determine the cutoff frequency and bandwidth.

Practice

