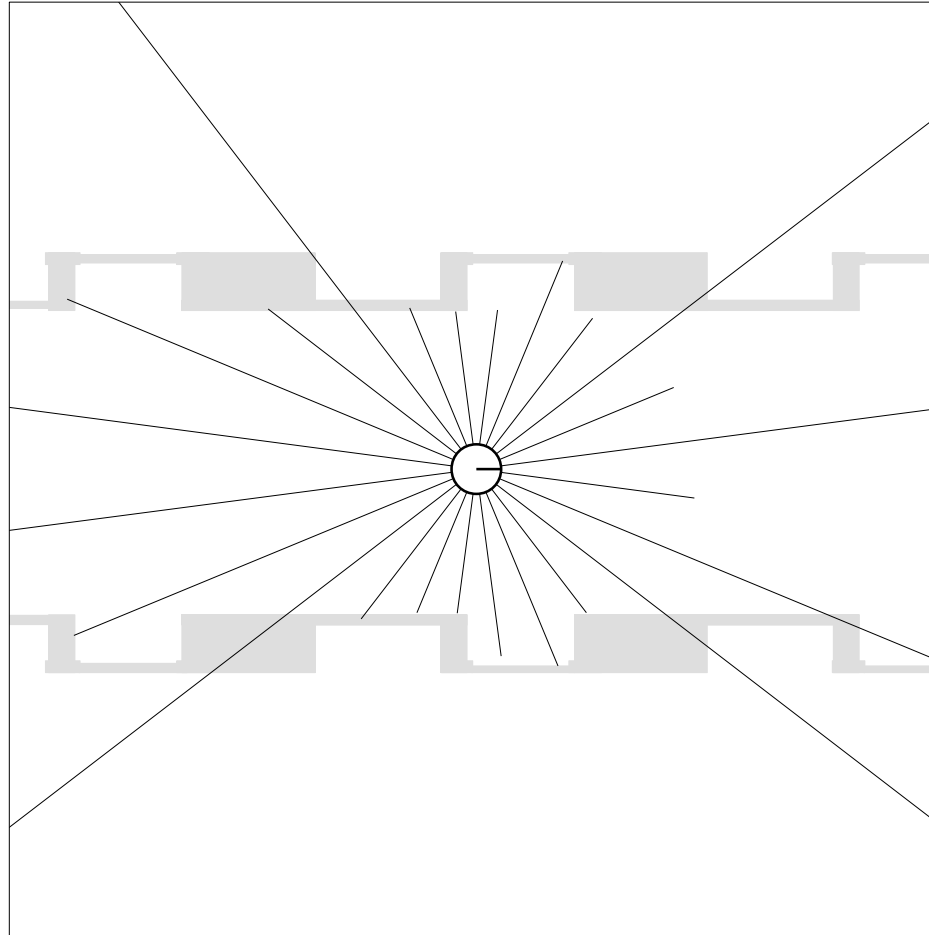




# Measurement model Lab



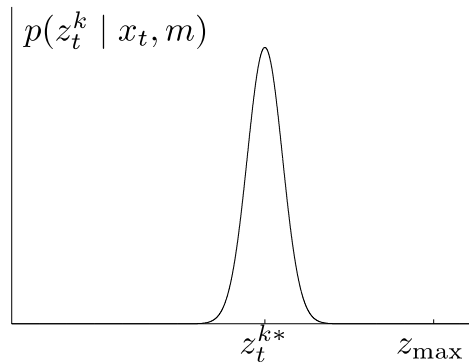
# Beam model for range finders



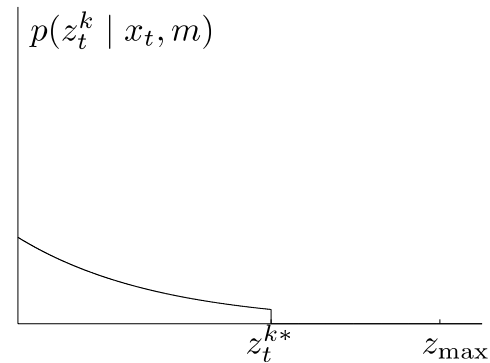


# Different sources of errors

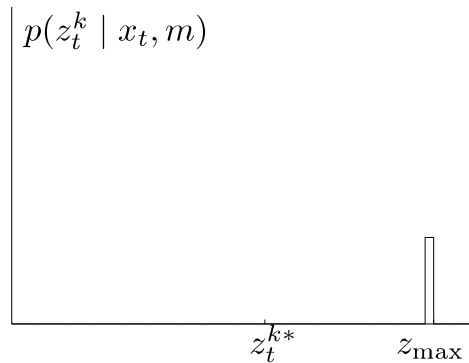
(a) Gaussian distribution  $p_{\text{hit}}$



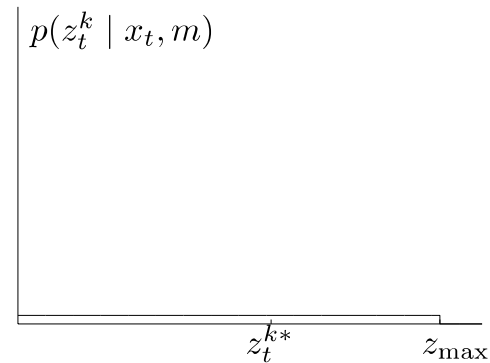
(b) Exponential distribution  $p_{\text{short}}$



(c) Uniform distribution  $p_{\text{max}}$

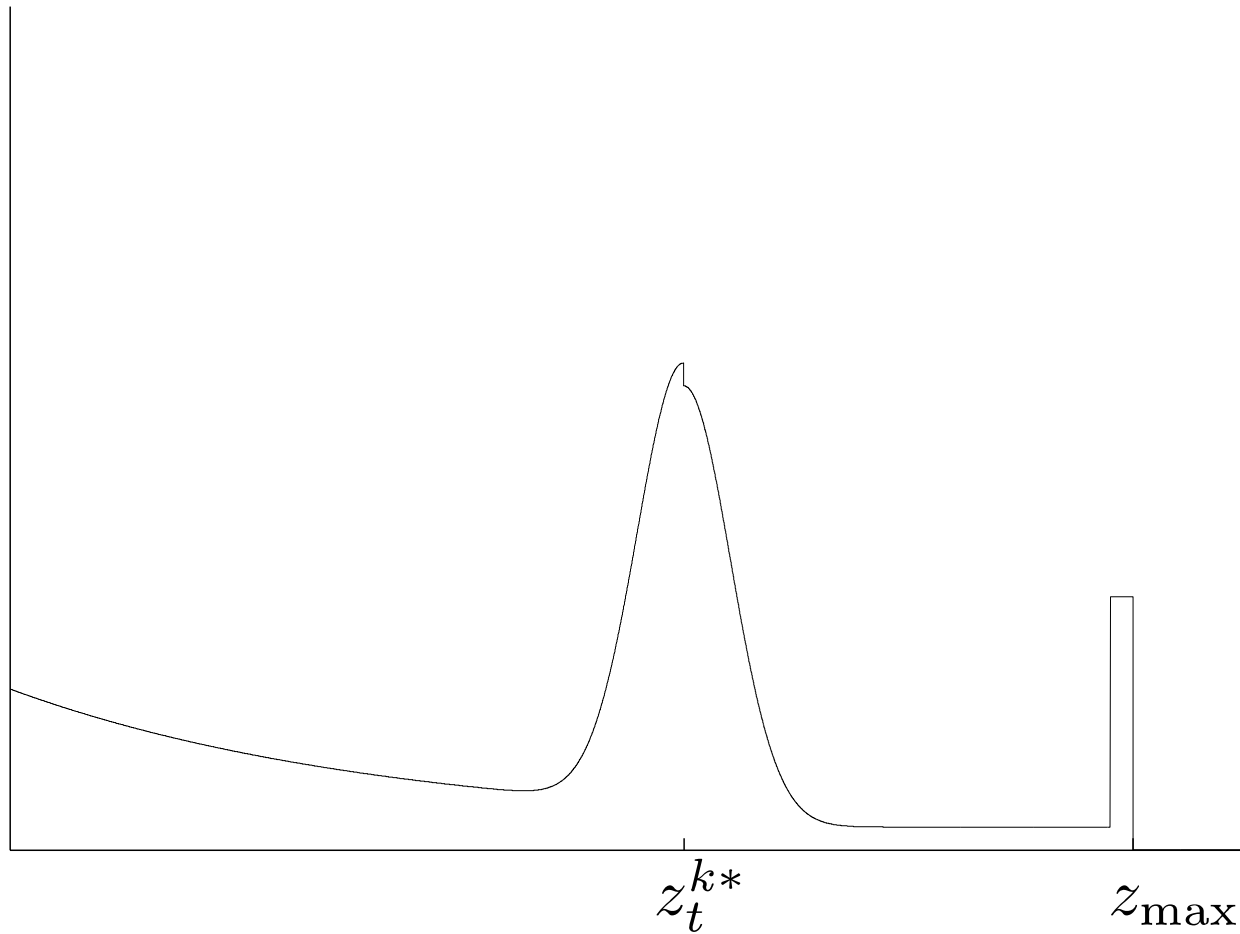


(d) Uniform distribution  $p_{\text{rand}}$





# Final distribution





# Beam range finder algorithm

```
1:  Algorithm beam_range_finder_model( $z_t, x_t, m$ ):  
2:       $q = 1$   
3:      for  $k = 1$  to  $K$  do  
4:          compute  $z_t^{k*}$  for the measurement  $z_t^k$  using ray casting  
5:           $p = z_{\text{hit}} \cdot p_{\text{hit}}(z_t^k \mid x_t, m) + z_{\text{short}} \cdot p_{\text{short}}(z_t^k \mid x_t, m)$   
6:               $+ z_{\text{max}} \cdot p_{\text{max}}(z_t^k \mid x_t, m) + z_{\text{rand}} \cdot p_{\text{rand}}(z_t^k \mid x_t, m)$   
7:           $q = q \cdot p$   
8:      return  $q$ 
```



# Measurement noise

- The measurement probability is given by:

Found through ray casting

$$p_{hit}(z_t^k | x_t, m) = \begin{cases} \eta N(z_t^k; z_t^{k*}; \sigma_{hit}^2) & \text{if } 0 < z_t^k < z_{max} \\ 0 & \text{Otherwise} \end{cases}$$

$$N(z_t^k; z_t^{k*}; \sigma_{hit}^2) = \frac{1}{\sqrt{2\pi\sigma_{hit}^2}} e^{-\frac{1}{2} \frac{(z_t^k - z_t^{k*})^2}{\sigma_{hit}^2}}$$

$$\eta = \left( \int_0^{z_{max}} \mathcal{N}(z_t^k; z_t^{k*}, \sigma_{hit}^2) dz_t^k \right)^{-1}$$



# Unexpected objects

- The probability of having such a object (or short reading) is:

$$p_{short}(z_t^k | x_t, m) = \begin{cases} \eta \lambda_{short} e^{-\lambda_{short} z_t^k} & \text{if } 0 \leq z_t^k \leq z_t^{k*} \\ 0 & \text{Otherwise} \end{cases}$$

- The cumulative probability is given by:

$$\begin{aligned} \int_0^{z_t^{k*}} \lambda_{short} e^{-\lambda_{short} z_t^k} dz_t^k &= -e^{-\lambda_{short} z_t^{k*}} + e^{-\lambda_{short} 0} \\ &= 1 - e^{-\lambda_{short} z_t^{k*}} \end{aligned}$$

- $\eta$  is found as:

$$\eta = \frac{1}{1 - e^{-\lambda_{short} z_t^{k*}}}$$



# Failures

- Sometimes obstacles are missed altogether. Examples include sonars measuring specular objects, or lasers sensing black, light absorbing objects, or in bright sunlight.
- A sensor error is returned as a *max-range measurement* ( $z_{max}$ )
- This will be modeled as a point-mass distribution:

$$p_{\max} \left( z_t^k \mid x_t, m \right) = I(z = z_{\max}) = \begin{cases} 1 & \text{if } z = z_{\max} \\ 0 & \text{Otherwise} \end{cases}$$





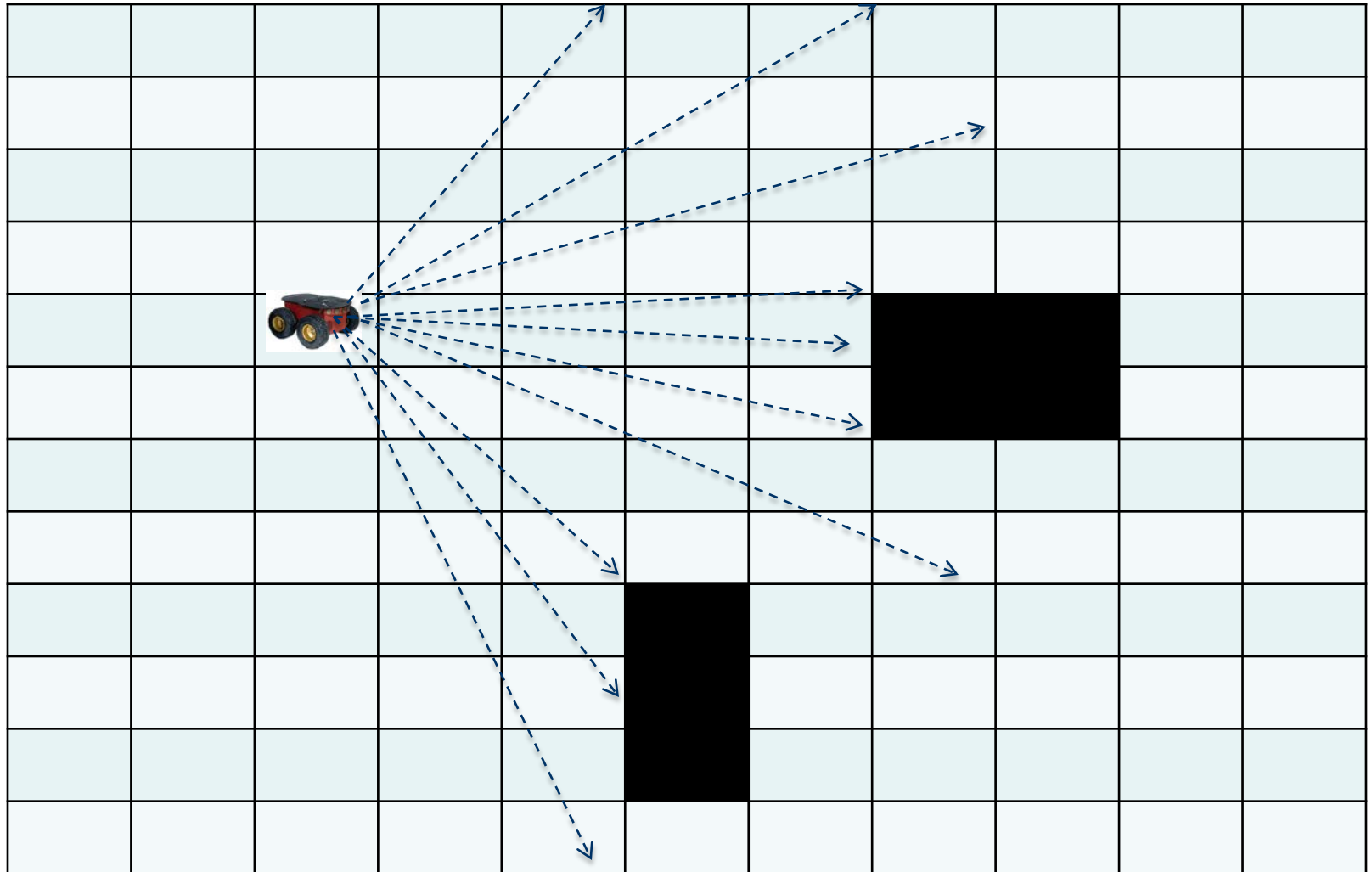
# Random measurements

- Range finders occasionally produce entirely unexplained measurements (phantom sonar readings, when bouncing off a wall).
- These measurements are modeled by a uniform distribution spread over the entire sensor measurement range.

$$p_{rand}(z_t^k | x_t, m) = \begin{cases} \frac{1}{z_{\max}} & \text{if } 0 \leq z_t^k < z_{\max} \\ 0 & \text{Otherwise} \end{cases}$$



# How to compute the mean value $z_k^{t*}$ ?





# How to perform ray casting

- Given a map and the position and the orientation of the SENSOR in the map, it is possible to calculate the “true” distance from the sensor to the nearest object.
- Simplest raycasting methods consider a straight line starting from the center of the sensor at an angle specified by the orientation. The algorithm returns the distance from the sensor to the nearest object.
- You will be provided with two functions, `castrays` and `castraysingle`.



# Castraysingle

`castraysingle(xc,yc,theta, map,lidarrange)` takes as input:

- Coordinates of the center of the sensor and its orientation.
- The map should be imported using  
`A = imread('maze.jpg');`  
`map_bw = im2bw(A,0.5);`
- Lidarrange is the range of the sensor in pixels



# The challenge

- Import the map file provided
- Position your robot at a specified location in the map
- Read from the sensor
- Apply raycasting at given angle and position of the sensor
- Calculate the different probabilities
- Output the final probability  $q$

Tips: You can consider a very high weight  $z_{hit}$  and very low probabilities for unexpected objects.