

# Interpolation

wiki: <https://en.wikipedia.org/wiki/Interpolation>

distinguish between

1. function approximation: [https://en.wikipedia.org/wiki/Function\\_approximation](https://en.wikipedia.org/wiki/Function_approximation)
2. curve fitting: [https://en.wikipedia.org/wiki/Curve\\_fitting#Functions](https://en.wikipedia.org/wiki/Curve_fitting#Functions)

## parameter

```
num_data = 5;
data_x = linspace(0,1,num_data);
data_y = rand(size(data_x));

num_interp_x = 100;
interp_x = linspace(0,1,num_interp_x);
```

## built-in

```
fig = figure();
ax = axes(fig, 'NextPlot','add','Box','on');
hline0 = plot(ax, data_x, data_y, 'LineStyle','none', 'Marker','+', 'MarkerSize', 15, 'LineWidth', 2);

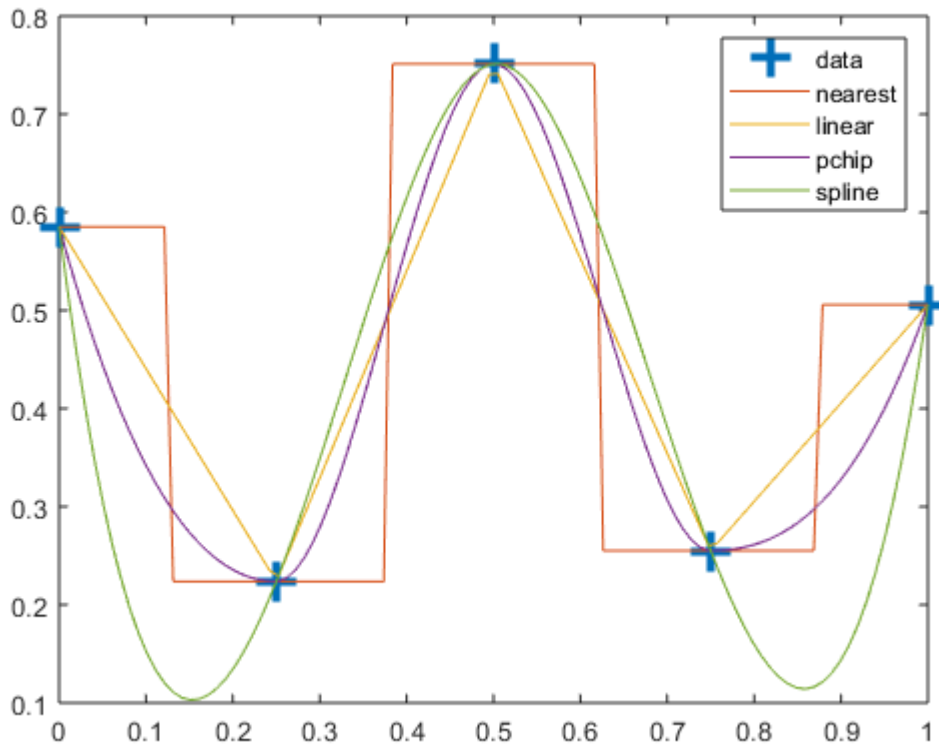
tmp1 = interp1(data_x, data_y, interp_x, 'nearest'); %doc('interp1')
hline1 = plot(ax, interp_x, tmp1);

tmp1 = interp1(data_x, data_y, interp_x, 'linear');
hline2 = plot(ax, interp_x, tmp1);

tmp1 = interp1(data_x, data_y, interp_x, 'pchip');
hline3 = plot(ax, interp_x, tmp1);

tmp1 = interp1(data_x, data_y, interp_x, 'spline');
hline4 = plot(ax, interp_x, tmp1);

legend([hline0,hline1,hline2,hline3,hline4],{'data', 'nearest', 'linear', 'pchip','spline'})
```



## Lagrangian

wiki: [https://en.wikipedia.org/wiki/Lagrange\\_polynomial](https://en.wikipedia.org/wiki/Lagrange_polynomial)

formula:

1. 
$$p_k(x) = \frac{(x - x_0) \dots (x - x_{k-1})(x - x_{k+1}) \dots (x - x_N)}{(x_k - x_0) \dots (x_k - x_{k-1})(x_k - x_{k+1}) \dots (x_k - x_N)}$$
2. 
$$p_i(x_k) = \delta_{ik}$$
3. 
$$L(x) = \sum_i p_i(x) f_i$$

```
interp_y = zeros(num_data, num_interp_x);

for ind1 = 1:num_data
    tmp1 = data_x([1:(ind1-1), (ind1+1):num_data]);
    interp_y(ind1,:) = prod(interp_x - tmp1', 1) / prod(data_x(ind1) - tmp1) * data_y(ind1);
end

fig = figure();
ax = axes(fig, 'NextPlot', 'add', 'Box', 'on');
ylim_min = min(min(sum(interp_y, 1)), min(interp_y(:)));
ylim_max = max(max(sum(interp_y, 1)), max(interp_y(:)));
ax.XLim = [min(interp_x), max(interp_x)];
ax.YLim = [ylim_min, ylim_max];
```

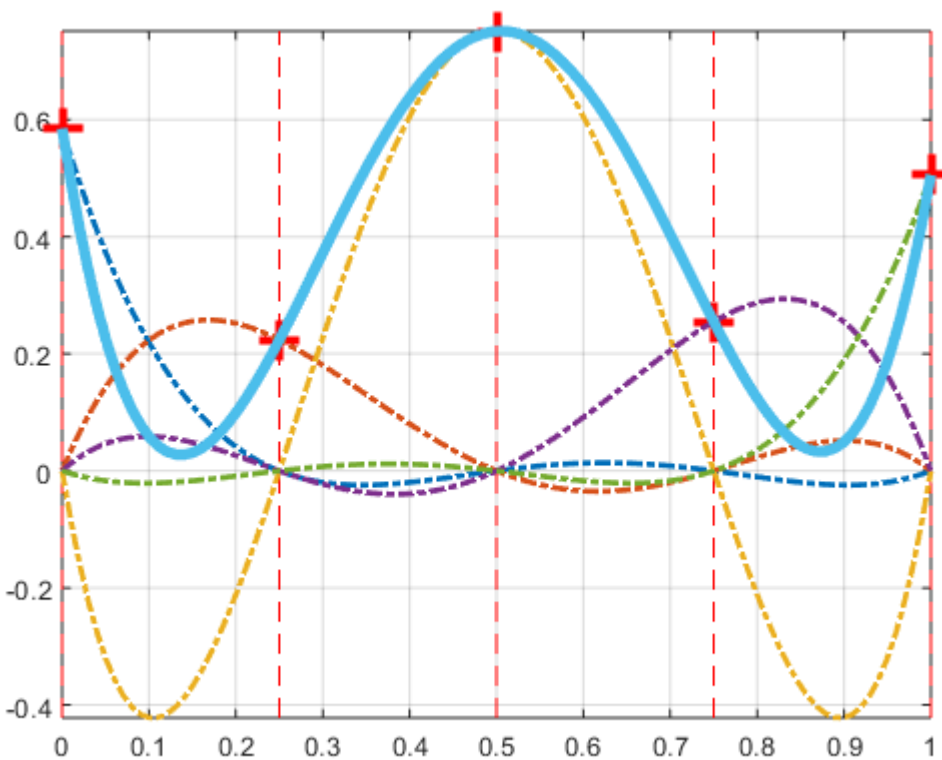
```

grid(ax, 'on')
ax.Title.FontSize = 20;
hLine = gobjects(1,num_data+1);

hLine_data = line(data_x,data_y,'LineStyle','None',...
    'Marker','+','LineWidth',3,'Color',[1,0,0],'MarkerSize',15);
for ind1 = 1:num_data
    line([data_x(ind1),data_x(ind1)],ax.YLim,'LineStyle','--','Color',[1,0,0]);
end

for ind1 = 1:num_data
    hLine(ind1) = plot(interp_x,interp_y(ind1,:), 'LineWidth',2,'LineStyle','-');
end
hLine(end) = plot(interp_x,sum(interp_y,1), 'LineWidth',4);

```



## Neville interpolation

wiki: [https://en.wikipedia.org/wiki/Neville%27s\\_algorithm](https://en.wikipedia.org/wiki/Neville%27s_algorithm)

formula

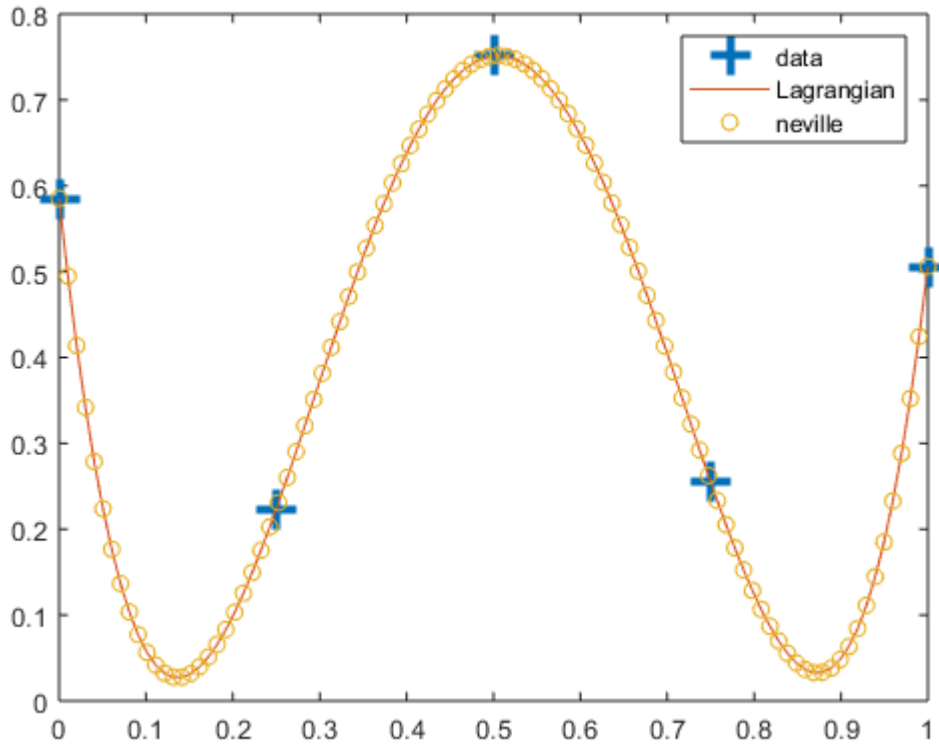
1.  $p_{ii}(x) = f_i$
2. 
$$p_{ij}(x) = \frac{(x_i - x)p_{i+1j}(x) + (x - x_j)p_{ij-1}(x)}{x_i - x_j}$$

```

y_lagrangian = my_lagrangian_interpolation(data_x, data_y, interp_x);
y_neville = my_naive_neville(data_x, data_y, interp_x);

fig = figure();
ax = axes(fig, 'NextPlot','add','Box','on');
hline0 = plot(ax, data_x, data_y, 'LineStyle', 'none', 'Marker', '+', 'MarkerSize', 15, 'LineWidth', 2);
hline1 = plot(ax, interp_x, y_lagrangian);
hline2 = plot(ax, interp_x, y_neville, 'o');
legend([hline0,hline1,hline2], {'data', 'Lagrangian', 'neville'})

```



## function

```

function y = my_lagrangian_interpolation(x0, y0, x)
% reference: https://en.wikipedia.org/wiki/Lagrange\_polynomial
% x0(1,N0) y0(1,N0) x(1,N1) y(1,N1)
N0 = size(x0,2);
y = zeros(1, size(x,2));

for ind1 = 1:N0
    tmp1 = x0([1:(ind1-1),(ind1+1):N0]);
    y = y + prod(x- tmp1',1)/prod(x0(ind1)-tmp1',1)*y0(ind1);
end
end

function y = my_naive_neville(x0, y0, x)
% reference: https://en.wikipedia.org/wiki/Neville%27s\_algorithm

```

```
% x0(1,N0) y0(1,N0) x(1,N1) y(1,N1)
% not available until 20181025
end
```