

# Lecture 2 Review Quiz

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University of Pennsylvania

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3. Why do we prefer standard deviation over variance?
  - The units of standard deviation are the same as the variable. Variance is the units squared

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  - The number of standard deviations the data is away from the mean

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9. Ready for the next lecture?

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