

Econ 103 (LPS Section) – Math Diagnostic Test

Instructions: You should be able to complete this within 25 minutes. If you have trouble completing it within that time, take note of which areas you had the most trouble with and ask questions on Piazza.

1. **Properties of Sums:** True or False?

(a) $\sum_{i=1}^n (x_i/n) = (\sum_{i=1}^n x_i)/n$

(a) _____

(b) $\sum_{k=1}^n x_k z_k = z_k \sum_{k=1}^n x_k$

(b) _____

(c) $\sum_{k=1}^m x_k y_k = (\sum_{k=1}^m x_k)(\sum_{k=1}^m y_k)$

(c) _____

(d) $(\sum_{i=1}^n x_i)(\sum_{j=1}^m y_j) = \sum_{i=1}^n \sum_{j=1}^m x_i y_j$

(d) _____

(e) $(\sum_{i=1}^n x_i)/(\sum_{i=1}^n z_i) = \sum_{i=1}^n (x_i/z_i)$

(e) _____

2. **Inequalities:** Suppose that $-z < (a - x)/b < z$ where $b > 0$. Find a lower bound L and an upper bound U such that $L < x < U$. U and L should be in terms of a , b , and z .

3. **Combinatorics:** Evaluate each of the following expressions.

(a) $4!$

(a) _____

(b) $\frac{100!}{98!}$

(b) _____

(c) $\binom{5}{3}$

(c) _____

(d) How many different ways can a deck of cards be arranged?

(d) _____

(e) How many different ways can 3 balls be pulled for the lottery? There are 10 balls numbered from 1 to 10 and the order matters

(e) _____

4. **Calculus and Optimization:** Let $f(a) = (x - a)^2 + (y - a)^2$ where x and y are constants.

(a) What value of a minimizes $f(a)$?

(b) How can you be sure this is a minimum rather than a maximum?

5. **Integration:** Imagine a rectangle whose base is the x -axis and whose bottom left corner is the origin $(0, 0)$. Suppose its area is 1 and the length of its base is 5. The area of this rectangle can be expressed as the definite integral of a function $f(x)$ from a to b .

(a) What is the function f ?

(b) What are the limits of integration (a, b) ?

6. **Integration:** Solve $\int_0^3 cx^2 dx = 1$ for c . Your answer should not involve x .

7. Let $z = \sum_{i=1}^n (y_i - a - bx_i)^2$. Evaluate $\partial z / \partial b$.

8. Let $F(x) = \int_a^x f(t) dt$. Express the derivative $F'(x)$ in terms of f .

