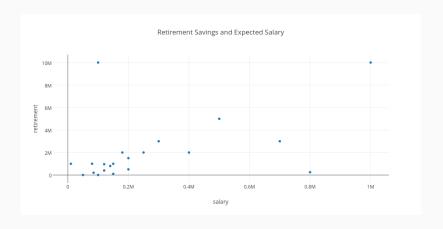
Econ 103 – Statistics for Economists

Chapter 2 feat. Z Scores and OLS

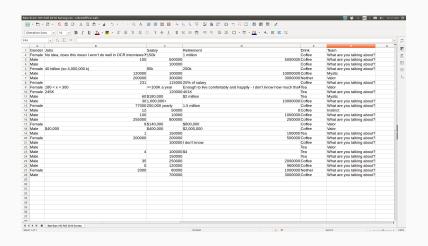
Mallick Hossain

University of Pennsylvania

Survey Results



Problems with Surveys

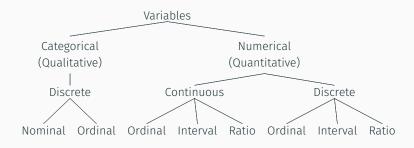


Types of Variables

Discussion!

- · What are the differences between the following variables?
 - · "Age" and "gender"
 - "Gender" and "class standing"
 - "SAT score" and "job creation"

A Few Definitions: A Taxonomy of Variables



Definitions

- Discrete: Can be a countable number of values
- · Continuous: Can take on any value

Discussion!

Can you order the following from weakest to strongest? Interval, Nominal, Ordinal, Ratio.

· Nominal: no order to the categories

- · Nominal: no order to the categories
- · Ordinal: categories with natural order

- · Nominal: no order to the categories
- · Ordinal: categories with natural order
- · Interval: only differences meaningful, no natural zero

- · Nominal: no order to the categories
- · Ordinal: categories with natural order
- · Interval: only differences meaningful, no natural zero
- · Ratio: differences and ratios meaningful, natural zero

Summary Statistics

Definitions

- 1. Measures of Central Tendency
 - Mean: the average ("balance point")

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

 Median: the middle observation (if data has even number of observations, take the mean of the middle two observations)

Definitions

2. Percentiles

 P^{th} Percentile = Value in $(P/100) \cdot (n+1)^{th}$ Ordered Position

An Example: n = 12

```
60 63 65 67 70 72 75 75 80 82 84 85

Q_1 = value in the 0.25(n+1)^{th} ordered position

= value in the 3.25^{th} ordered position

= 0.75 * 65 + 0.25 * 67

= 65.5
```

Definitions

- 3. Measures of Spread
 - · Variance: the spread from the mean

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

· Standard Deviation: another way to measure the spread

$$S = \sqrt{S^2}$$

· Range: the distance between the highest and lowest value

$$Range = |x_{max} - x_{min}|$$

• Interquartile Range (IQR): the distance between the upper and lower quartiles

$$IQR = |x_{75\%} - x_{25\%}|$$

Why Squares?

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

Why Squares?

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

What's Wrong With This?

$$\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x}) = \frac{1}{n-1} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} \bar{x} \right] = \frac{1}{n-1} \left[\sum_{i=1}^{n} x_i - n\bar{x} \right]$$
$$= \frac{1}{n-1} \left[\sum_{i=1}^{n} x_i - n \cdot \frac{1}{n} \sum_{i=1}^{n} x_i \right]$$
$$= \frac{1}{n-1} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} x_i \right] = 0$$

Definitions

- 4. Measure of Symmetry
 - Skewness: a measure of symmetry, positive values means the right tail is longer and vice versa

Skewness =
$$\frac{1}{n} \frac{\sum_{i=1}^{n} (x_i - \bar{x})^3}{s^3}$$

Skewness – A Measure of Symmetry

Skewness =
$$\frac{1}{n} \frac{\sum_{i=1}^{n} (x_i - \bar{x})^3}{s^3}$$

What do the values indicate?

 $Zero \Rightarrow symmetry$, positive right-skewed, negative left-skewed.

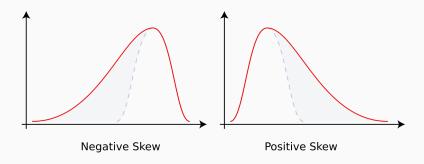
Why cubed?

To get the desired sign.

Why divide by s³?

So that skewness is unitless

Skewness – A Measure of Symmetry



Definitions

- 5. Relationship between variables
 - · Covariance: how two variables vary together
 - Correlation: normalized version of covariance (ranges between -1 and +1)
 - · Regression: an estimation of how two variables are related

Charts

Some Data Visualization Quotes

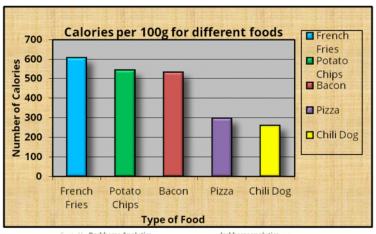
- 1. "Overload, clutter, and confusion are not attributes of information, they are failures of design" –Edward Tufte
- 2. "...few people will appreciate the music if I just show them the notes. Most of us need to listen to the music to understand how beautiful it is. But often, that's how we present statistics; we just show the notes we don't play the music." –Hans Rosling

An Illustration

https://i.imgur.com/W4BKCVU.gif

Before and After

Before



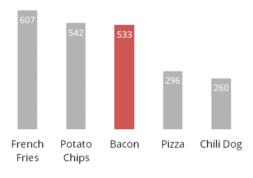
Created by Darkhorse Analytics

www.darkhorseanalytics.com

Before and After

After

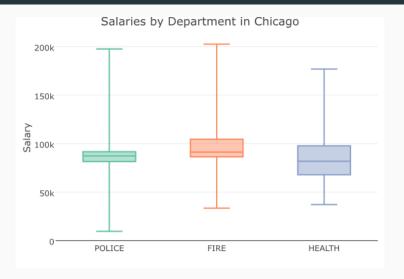
Calories per 100g



Created by Darkhorse Analytics

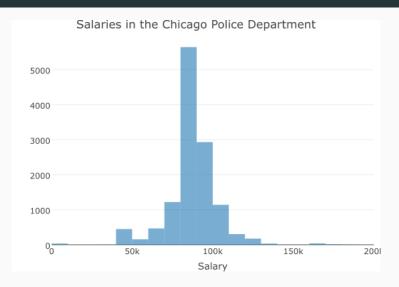
www.darkhorseanalytics.com

Illustrating with Charts (Box and Whisker Chart)



What summary statistics can you infer from this chart?

Illustrating with Charts (Histogram)

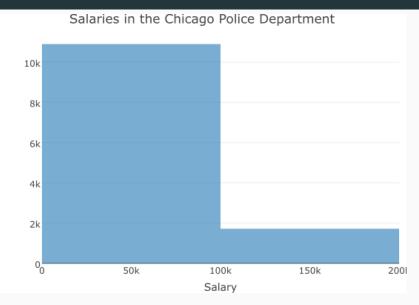


What summary statistics can you infer from this chart?

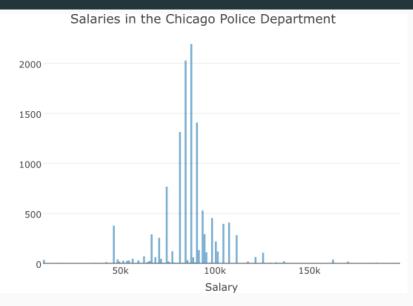
Histograms are Really Important

- 1. Histograms show the frequency of different observations
- 2. Important Choice: How many bins?

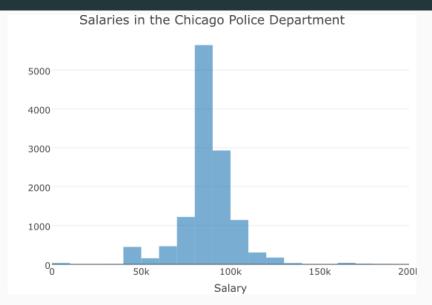
Too Few Bins (Oversmoothing)



Too Many Bins (Undersmoothing)



Just Right! (Usually around 20 bins or so)



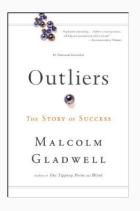
Questions to Ask Yourself about Each Summary Statistic

- 1. What does it measure?
- 2. What are its units compared to those of the data?
- 3. How do its units change if those of the data change?
- 4. What are the benefits and drawbacks of this statistic?

Some of the information regarding items 2 and 3 is on the homework rather than in the slides because working it out for yourself is a good way to check your understanding.

Outliers

What is an Outlier?



Outlier: A very unusual observation relative to the other observations in the dataset (i.e. very small or very big).

- Assume our data is 1, 2, 3, 4, 5. What are our summary stats (mean, median, variance, range, IQR)
- What will be affected if the data includes an outlier and becomes 1, 2, 3, 4, 4990?

• Mean changes from 3 to 1000

- Mean changes from 3 to 1000
- · Median remains at 3

- Mean changes from 3 to 1000
- Median remains at 3
- · Variance changes from 2.5 to 4,975,032

- Mean changes from 3 to 1000
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- · Range changes from 4 to 4889

- Mean changes from 3 to 1000
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- · Range changes from 4 to 4889
- IQR remains at 2
- When Does the Median Change? IQR?

- · Mean changes from 3 to 1000
- · Median remains at 3
- · Variance changes from 2.5 to 4,975,032
- · Range changes from 4 to 4889
- · IQR remains at 2
- When Does the Median Change? IQR?
 - · Ranks would have to change.

Summary of Sensitivity

Variance

Essentially the average squared distance from the mean. Sensitive to both skewness and outliers.

Standard Deviation

√Variance, but more convenient since same units as data

Range

Difference between larges and smallest observations. *Very* sensitive to outliers.

Interquartile Range

Range of middle 50% of the data. Insensitive to outliers, skewness.

Sample vs. Population

Essential Distinction: Sample vs. Population

For now, you can think of the population as a list of N objects:

Population: x_1, x_2, \ldots, x_N

from which we draw a sample of size n < N objects:

Sample: x_1, x_2, \ldots, x_n

Important Point:

Later in the course we'll be more formal by considering probability models that represent the *act of sampling* from a population rather than thinking of a population as a list of objects. Once we do this we will no longer use the notation *N* as the population will be *conceptually infinite*.

Essential Distinction: Parameter vs. Statistic

N individuals in the Population, n individuals in the Sample:

	Parameter (Population)	Statistic (Sample)
Mean	$\mu = \frac{1}{N} \sum_{i=1}^{N} x_i$	$\bar{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$
Var.	$\sigma^{2} = \frac{1}{N} \sum_{i=1}^{N} (x_{i} - \mu)^{2}$	$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$
S.D.	$\sigma = \sqrt{\sigma^2}$	$S = \sqrt{S^2}$

Key Point

We use a sample $x_1, ..., x_n$ to calculate statistics (e.g. \bar{x} , s^2 , s) that serve as estimates of the corresponding population parameters (e.g. μ , σ^2 , σ).

Why Do Sample Variance and Std. Dev. Divide by n-1?

$$\sigma^{2} = \frac{1}{N} \sum_{i=1}^{N} (x_{i} - \mu)^{2}$$

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}$$

There is an important reason for this, but explaining it requires some concepts we haven't learned yet.

Some Intuition

- Intuition 1: If we only had one data point, what would be the sample variance? Would it even be defined?
- Intuition 2: We know that the deviations from the sample mean sum to zero (see discussion of why variance is squared). Hence, we only need to know n-1 of the deviations since the last one will be whatever it takes to make the sum of them equal to 0. Hence, it would be proper to divide by n-1 instead of n

Z Scores

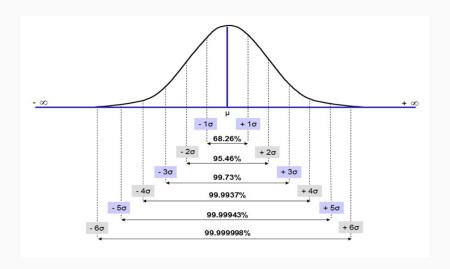
Why Mean and Variance (and Std. Dev.)?

Empirical Rule

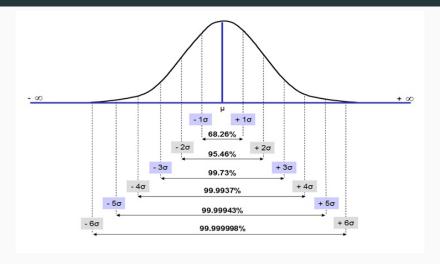
For large populations that are approximately bell-shaped, standard deviation tells where most observations will be relative to the mean:

- $\cdot \approx$ 68% of observations are in the interval $\mu \pm \sigma$
- $\cdot pprox$ 95% of observations are in the interval $\mu \pm 2\sigma$
- Almost all of observations are in the interval $\mu \pm 3\sigma$

Standard Deviations



Standard Deviations



Physics uses a five-sigma rule (i.e. this could only happen normally 0.00057% of the time!)

$$Z_i = \frac{X_i - \bar{X}}{S}$$

$$z_i = \frac{x_i - \bar{x}}{s}$$

Unitless

Allows comparison of variables with different units.

$$z_i = \frac{x_i - \bar{x}}{s}$$

Unitless

Allows comparison of variables with different units.

Detecting Outliers

Measures how "extreme" one observation is relative to the others.

$$z_i = \frac{x_i - \bar{x}}{s}$$

Unitless

Allows comparison of variables with different units.

Detecting Outliers

Measures how "extreme" one observation is relative to the others.

Linear Transformation

$$\bar{z} = \frac{1}{n} \sum_{i=1}^{n} z_i = \frac{1}{n} \sum_{i=1}^{n} \frac{x_i - \bar{x}}{s} = \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} \bar{x} \right]$$

$$\bar{z} = \frac{1}{n} \sum_{i=1}^{n} z_i = \frac{1}{n} \sum_{i=1}^{n} \frac{x_i - \bar{x}}{s} = \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} \bar{x} \right]$$
$$= \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - n\bar{x} \right] = \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - n \cdot \frac{1}{n} \sum_{i=1}^{n} x_i \right]$$

$$\bar{Z} = \frac{1}{n} \sum_{i=1}^{n} z_i = \frac{1}{n} \sum_{i=1}^{n} \frac{x_i - \bar{x}}{s} = \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} \bar{x} \right]$$

$$= \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - n\bar{x} \right] = \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - n \cdot \frac{1}{n} \sum_{i=1}^{n} x_i \right]$$

$$= \frac{1}{n \cdot s} \left[\sum_{i=1}^{n} x_i - \sum_{i=1}^{n} x_i \right] = 0$$

$$s_z^2 = \frac{1}{n-1} \sum_{i=1}^n (z_i - \bar{z})^2 = \frac{1}{n-1} \sum_{i=1}^n z_i^2 = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right)^2$$

$$S_{z}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (z_{i} - \bar{z})^{2} = \frac{1}{n-1} \sum_{i=1}^{n} z_{i}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{x_{i} - \bar{x}}{s_{x}} \right)^{2}$$
$$= \frac{1}{s_{x}^{2}} \left[\frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2} \right] = \frac{s_{x}^{2}}{s_{x}^{2}} = 1$$

$$S_{z}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (z_{i} - \bar{z})^{2} = \frac{1}{n-1} \sum_{i=1}^{n} z_{i}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{x_{i} - \bar{x}}{s_{x}} \right)^{2}$$
$$= \frac{1}{s_{x}^{2}} \left[\frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2} \right] = \frac{s_{x}^{2}}{s_{x}^{2}} = 1$$

So what is the standard deviation of the z-scores?

Population Z-scores and the Empirical Rule: $\mu \pm 2\sigma$

If we knew the population mean μ and standard deviation σ we could create a *population version* of a z-score. This leads to an important way of rewriting the Empirical Rule:

Bell-shaped population \Rightarrow approx. 95% of observations x_i satisfy

$$\mu - 2\sigma \le x_i \le \mu + 2\sigma$$
$$-2\sigma \le x_i - \mu \le 2\sigma$$
$$-2 \le \frac{x_i - \mu}{\sigma} \le 2$$

Covariance and Correlation

Covariance and Correlation: Linear Dependence Measures

Two Samples of Numeric Data

 x_1, \ldots, x_n and y_1, \ldots, y_n

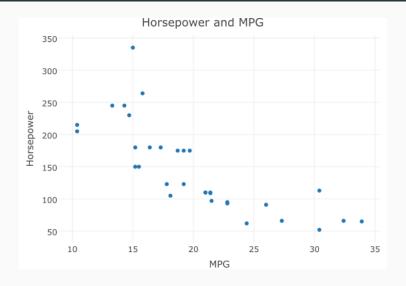
Dependence

Do x and y both tend to be large (or small) at the same time?

Key Point

Use the idea of centering and standardizing to decide what "big" or "small" means in this context.

Are Engine Cylinders and Horsepower Related?



Recall Formulas

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

$$\bar{y} = \frac{1}{n} \sum_{i=1}^{n} y_i$$

$$s_x = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

$$s_y = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (y_i - \bar{y})^2}$$

Covariance

$$s_{xy} = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})$$

- · Centers each observation around its mean and multiplies.
- · Zero ⇒ no linear dependence
- Positive ⇒ positive linear dependence
- Negative ⇒ negative linear dependence
- Population parameter: σ_{xy}
- · Units?

Covariance

$$s_{xy} = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})$$

- · Centers each observation around its mean and multiplies.
- · Zero ⇒ no linear dependence
- Positive ⇒ positive linear dependence
- · Negative ⇒ negative linear dependence
- Population parameter: σ_{xy}
- · Units?
- If you know this, you know variance!

Correlation

$$r_{xy} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{x_i - \overline{x}}{s_x} \right) \left(\frac{y_i - \overline{y}}{s_y} \right) = \frac{s_{xy}}{s_x s_y}$$

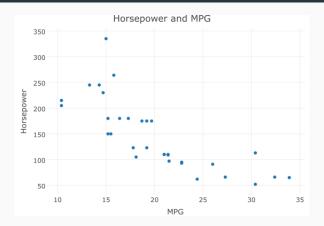
- · Centers and standardizes each observation
- Bounded between -1 and 1
- · Zero ⇒ no linear dependence
- Positive ⇒ positive linear dependence
- Negative ⇒ negative linear dependence
- Population parameter: ho_{xy}
- Unitless

Game!

guessthecorrelation.com

Introduction to Regression

Least Squares Regression – Predict Using a Line



- In order to fit a line through this, we need to estimate y = a + bx
- How do we find a and b?

Finding a and b

 Linear regression chooses the slope (b) and intercept (a) that minimize the sum of squared vertical deviations

$$\sum_{i=1}^{n} d_i^2 = \sum_{i=1}^{n} (y_i - a - bx_i)^2$$

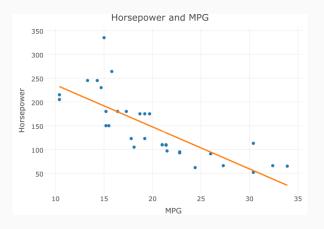
· Why do we square the deviations?

Important Point About Notation

minimize
$$\sum_{i=1}^{n} d_i^2 = \sum_{i=1}^{n} (y_i - a - bx_i)^2$$
$$\hat{y} = a + bx$$

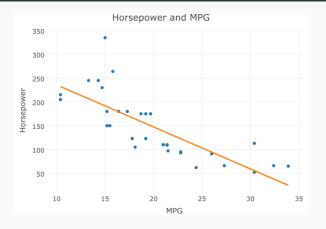
- $(x_i, y_i)_{i=1}^n$ are the observed data
- \hat{y} is our prediction for a given value of x
- Neither x nor \hat{y} needs to be in our dataset!

Prediction 28 MPG?



$$\widehat{hp} = 324.08 - 8.83mpg$$

Prediction 28 MPG?



$$\widehat{hp} = 324.08 - 8.83mpg$$

$$76.84 = 324.08 - 8.83 * 28$$

You Need to Know How To Derive This

Minimize the sum of squared vertical deviations from the line:

$$\min_{a,b} \sum_{i=1}^{n} (y_i - a - bx_i)^2$$

How should we proceed? Select all that apply.

- (a) Differentiate with respect to x
- (b) Differentiate with respect to y
- (c) Differentiate with respect to a
- (d) Differentiate with respect to b
- (e) You can't fool me! You can't solve this with calculus.

Derivation

Objective Function

$$\min_{a,b} \sum_{i=1}^n (y_i - a - bx_i)^2$$

FOC with respect to a

Derivation

Objective Function

$$\min_{a,b} \sum_{i=1}^{n} (y_i - a - bx_i)^2$$

FOC with respect to a

$$-2\sum_{i=1}^{n} (y_i - a - bx_i) = 0$$

$$\sum_{i=1}^{n} y_i - \sum_{i=1}^{n} a - b\sum_{i=1}^{n} x_i = 0$$

$$\frac{1}{n} \sum_{i=1}^{n} y_i - \frac{na}{n} - \frac{b}{n} \sum_{i=1}^{n} x_i = 0$$

$$\bar{y} - a - b\bar{x} = 0$$

Regression Line Goes Through the Means!

$$\bar{y} = a + b\bar{x}$$

Substitute $a = \bar{y} - b\bar{x}$

$$\sum_{i=1}^{n} (y_i - a - bx_i)^2 = \sum_{i=1}^{n} (y_i - \bar{y} + b\bar{x} - bx_i)^2$$
$$= \sum_{i=1}^{n} [(y_i - \bar{y}) - b(x_i - \bar{x})]^2$$

FOC wrt b

$$-2\sum_{i=1}^{n} [(y_i - \bar{y}) - b(x_i - \bar{x})](x_i - \bar{x}) = 0$$

$$\sum_{i=1}^{n} (y_i - \bar{y})(x_i - \bar{x}) - b\sum_{i=1}^{n} (x_i - \bar{x})^2 = 0$$

$$b = \frac{\sum_{i=1}^{n} (y_i - \bar{y})(x_i - \bar{x})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$

Simple Linear Regression

Problem

$$\min_{a,b} \sum_{i=1}^{n} (y_i - a - bx_i)^2$$

Solution

$$b = \frac{\sum_{i=1}^{n} (y_i - \bar{y}) (x_i - \bar{x})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$

$$a = \bar{y} - b\bar{x}$$

Relating Regression to Covariance and Correlation

$$b = \frac{\sum_{i=1}^{n} (y_i - \bar{y}) (x_i - \bar{x})}{\sum_{i=1}^{n} (x_i - \bar{x})^2} = \frac{\frac{1}{n-1} \sum_{i=1}^{n} (y_i - \bar{y}) (x_i - \bar{x})}{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2} = \frac{s_{xy}}{s_x^2}$$
$$r = \frac{s_{xy}}{s_x s_y} = b \frac{s_x}{s_y}$$

Comparing Regression, Correlation and Covariance

Units

Correlation is unitless, covariance and regression coefficients (a, b) are not. (What are the units of these?)

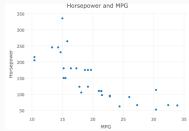
Symmetry

Correlation and covariance are symmetric, regression isn't. (Switching *x* and *y* axes changes the slope and intercept.)

$$s_{mpg,hp} = -321 \quad s_{mpg} = 6 \quad s_{hp} = 69$$

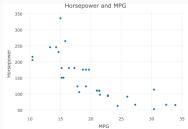
What is the sample correlation between MPG (x) and horsepower (y)?

$$m\bar{p}g = 20, \quad h\bar{p} = 147$$



$$s_{mpg,hp} = -321$$
 $s_{mpg} = 6$ $s_{hp} = 69$ $m\bar{p}g = 20$, $h\bar{p} = 147$

What is the sample correlation between MPG (x) and horsepower (y)?



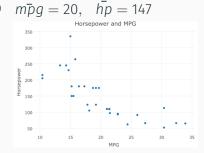
$$r = \frac{s_{xy}}{s_x s_y} = \frac{-321}{6 \times 69} \approx -0.78$$

$$s_{mpg,hp} = -321$$
 $s_{mpg} = 6$ $s_{hp} = 69$

What is the value of *b* for the regression:

$$\hat{y} = a + bx$$

where x is MPG and y is horsepower?

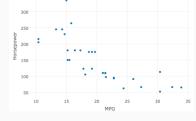


$$s_{mpg,hp} = -321$$
 $s_{mpg} = 6$ $s_{hp} = 69$ $m\bar{p}g = 20$, $h\bar{p} = 147$

What is the value of *b* for the regression:

$$\hat{y} = a + bx$$

where *x* is MPG and *y* is horsepower?

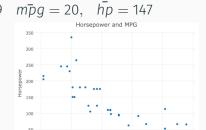


$$b = \frac{s_{xy}}{s_x^2} = \frac{-321}{6^2} \approx -8.9$$

 $s_{mpg,hp} = -321$ $s_{mpg} = 6$ $s_{hp} = 69$ What is the value of a for the regression:

$$\hat{y} = a + bx$$

where x is MPG and y is horsepower? (prev. slide b = -8.9)

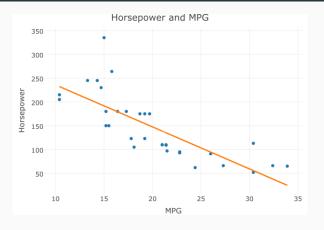


 $s_{mpg,hp} = -321$ $s_{mpg} = 6$ $s_{hp} = 69$ mpg = 20, hp = 147 What is the value of a for the regression:

$$\hat{y} = a + bx$$

where x is MPG and y is horsepower? (prev. slide b = -8.9)

$$a = \bar{y} - b\bar{x} = 147 - (-8.9) \times 20 \approx 325$$



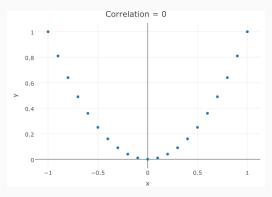
$$a \approx 325$$

$$b \approx -8.9$$

$$\widehat{hp} = 324.08 - 8.83 mpg$$

EXTREMELY IMPORTANT

- Regression, Covariance, and Correlation: linear association.
- Linear association \neq causation.
- · Linear is not the only kind of association!



Review

Essential Distinction: Parameter vs. Statistic

N individuals in the Population, *n* individuals in the Sample:

	Parameter (Population)	Statistic (Sample)
Mean	$\mu_{X} = \frac{1}{N} \sum_{i=1}^{N} X_{i}$	$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$
Var.	$\sigma_{X}^{2} = \frac{1}{N} \sum_{i=1}^{N} (x_{i} - \mu)^{2}$ $\sigma_{X} = \sqrt{\sigma_{X}^{2}}$	$s_x^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$ $s_x = \sqrt{s^2}$
S.D.	$\sigma_{\rm X} = \sqrt{\sigma_{\rm X}^2}$	$S_X = \sqrt{S^2}$
Cov.	$\sigma_{xy} = \frac{\sum_{i=1}^{N} (x_i - \mu_x)(y_i - \mu_y)}{N}$ $\rho = \frac{\sigma_{xy}}{\sigma_x \sigma_y}$	$s_{xy} = \frac{\sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y})}{n-1}$ $r = \frac{s_{xy}}{s_x s_y}$

Related Reading

- Wonnacott: Chapter 2, Section 4-5 A+B, Section 5-3, 11-1, 11-2, Appendices to 2-2, 2-5, 11-1, and 11-2
- · How to Lie with Statistics: Chapters 2, 5, and 6
- If you're rusty on permutations, combinations, etc., read the "Permutations and Combinations" document on the course page (mallickhossain.com/econ-103)

Homework

- · Chapter 2 Problems
- Additional Problems
- R Tutorial 2