$$\lim_{v \to -5} \frac{v^2 + 6v + 5}{v + 5} = \boxed{-4}$$

Hint: Factor the numerator.