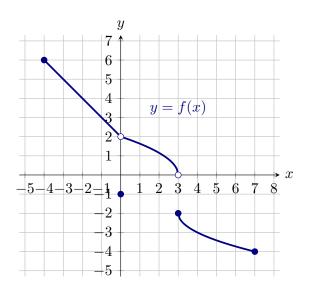
**Exercise** 1 The entire graph of a function f is given below.



The domain of f is  $\begin{bmatrix} -4 \end{bmatrix}$ ,  $\begin{bmatrix} 7 \end{bmatrix}$ .

The range of f (from bottom to top) is  $\begin{bmatrix} -4 \\ -2 \end{bmatrix} \cup \{ -1 \} \cup \{ 0 , 2 \} \cup \{ 2 , 6 \}$ .

Find the following limits, if they exist. If a limit does not exist, explain why.

$$\lim_{x \to 0} f(x) = \boxed{2}$$

## Multiple Choice:

- (a) The limit does exist.  $\checkmark$
- (b) The limit does not exist because f(0) does not exist.
- (c) The limit does not exist because f(0) is not close to the values of f near 0.
- (d) The limit does not exist because  $\lim_{x\to 0^-} f(x) \neq \lim_{x\to 0^+} f(x)$ .

$$\lim_{x \to 3^{-}} f(x) = \boxed{0}$$

## Multiple Choice:

- (a) The limit does exist. ✓
- (b) The limit does not exist because f(3) does not exist.
- (c) The limit does not exist because f(3) is not close to the values of f near
- (d) The limit does not exist because  $\lim_{x\to 3^-} f(x) \neq \lim_{x\to 3^+} f(x)$ .

## $\lim_{x \to 3^+} f(x) = \boxed{-2}$

Multiple Choice:

- (a) The limit does exist.  $\checkmark$
- (b) The limit does not exist because f(3) does not exist.
- (c) The limit does not exist because f(3) is not close to the values of f near
- (d) The limit does not exist because  $\lim_{x\to 3^-} f(x) \neq \lim_{x\to 3^+} f(x)$ .

$$\lim_{x \to 3} f(x) = \boxed{DNE}$$

Multiple Choice:

- (a) The limit does exist.
- (b) The limit does not exist because f(3) does not exist.
- (c) The limit does not exist because f(3) is not close to the values of f near
- (d) The limit does not exist because  $\lim_{x\to 3^-} f(x) \neq \lim_{x\to 3^+} f(x)$ .  $\checkmark$

Find the following values.

$$f(0) = \boxed{-1}$$
$$f^{-1}(-2) = \boxed{3}$$