Exercise 1 Let

$$f(x) = \begin{cases} |x| & \text{if } x < 1, \\ \frac{x^2 - a^2}{x - a} & \text{if } x > 1. \end{cases}$$

If $\lim_{x\to 1} f(x)$ exists, what must be the value of a?

$$a = \boxed{0}$$

Hint: Equate the two one sided limits of f at x=1 to obtain an equation involving a.