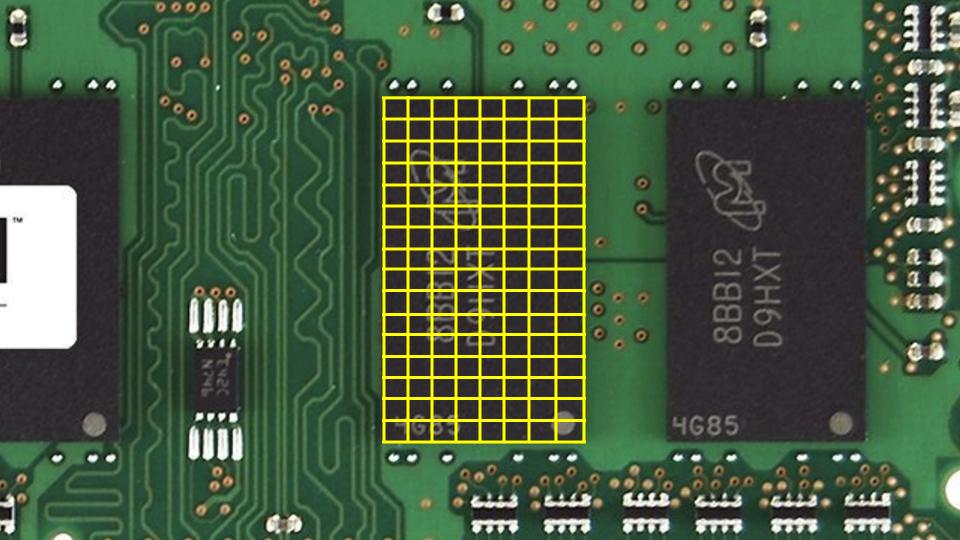
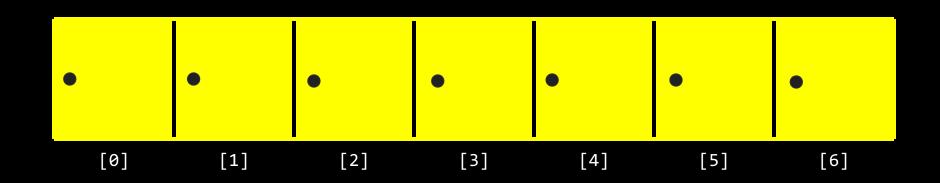
Introdução à Computação

input → output

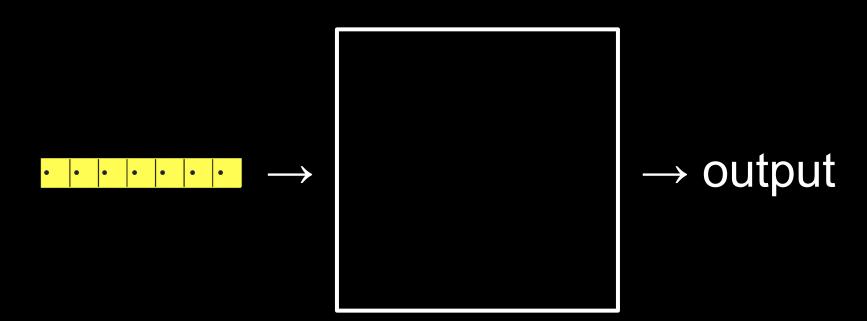


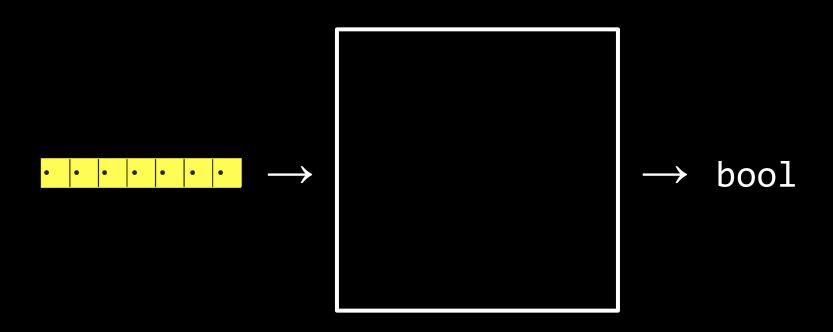
4 6 8 2 7 5 0



searching

input → output

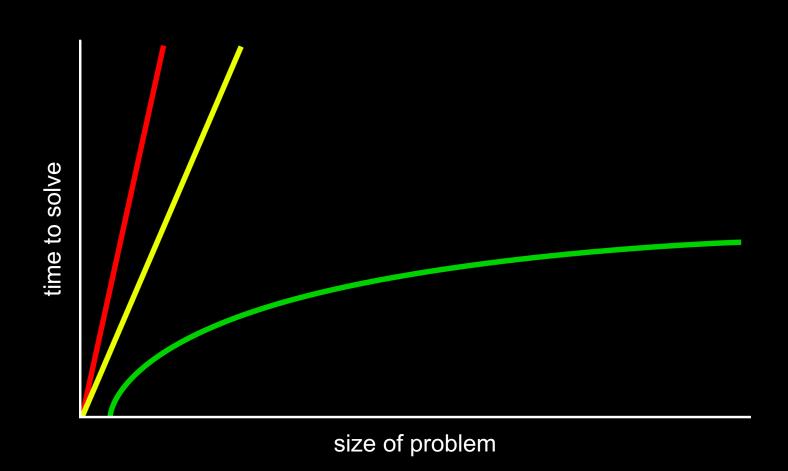


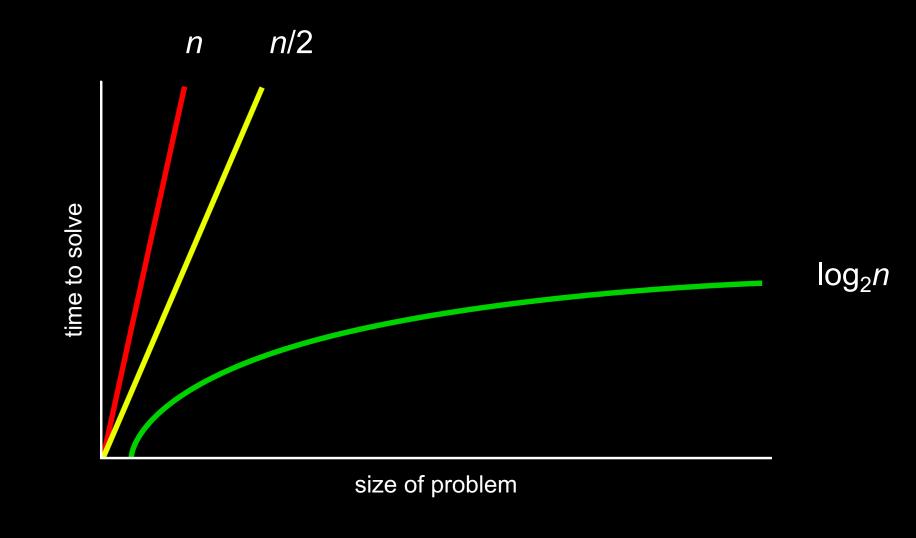


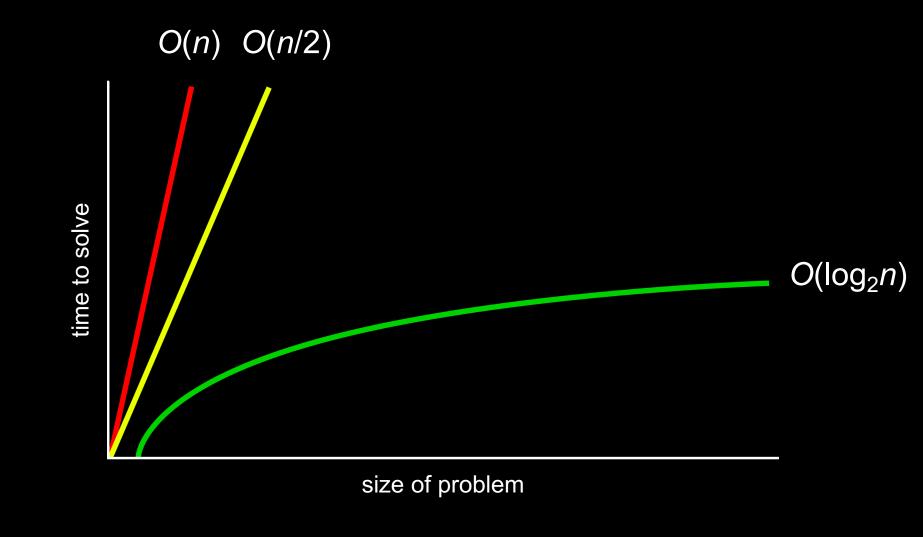
algorithms

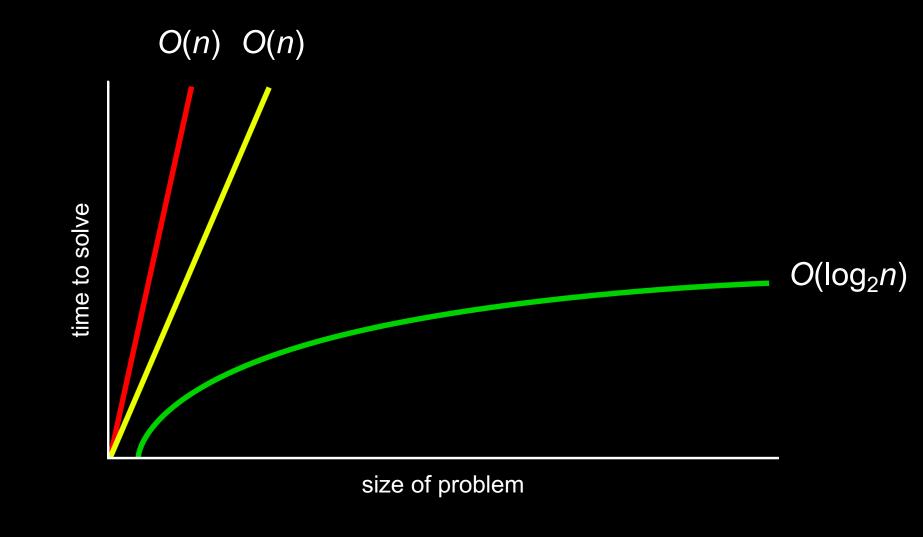
running times

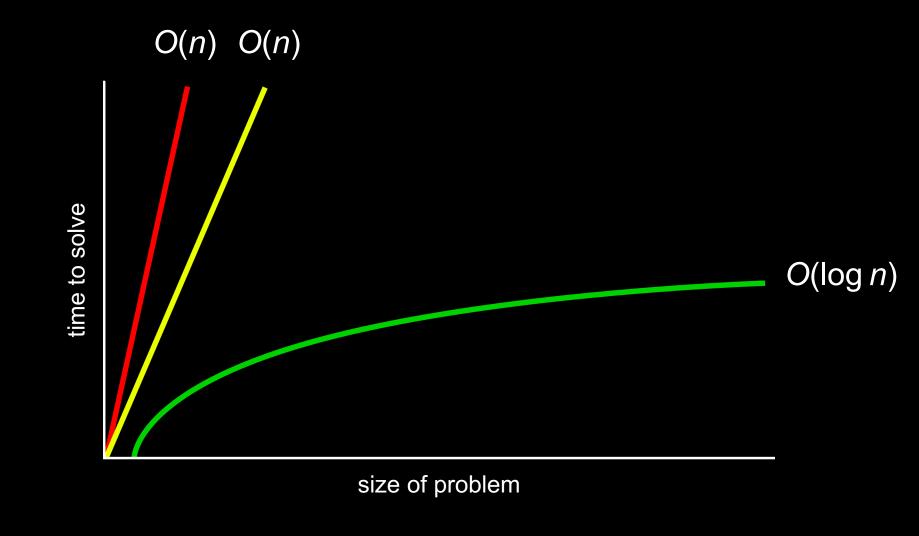


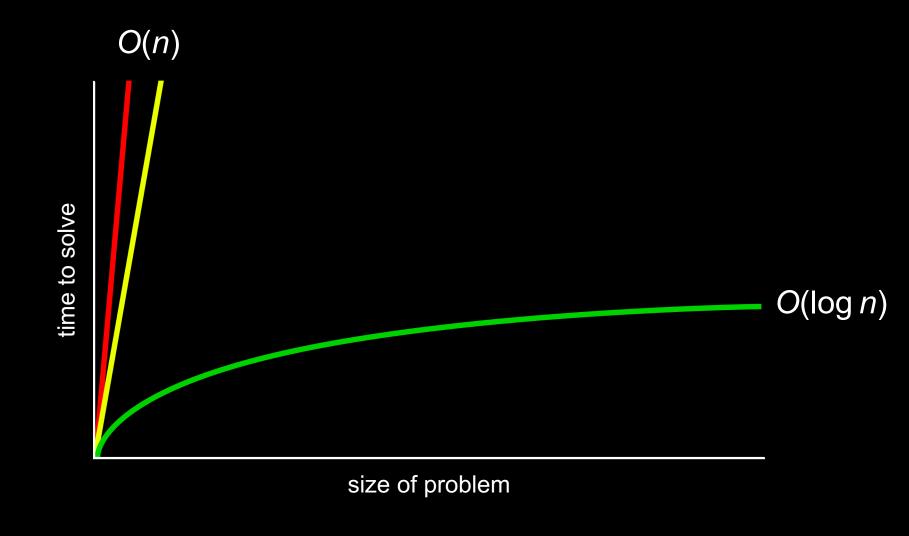












 $O(n^2)$

 $O(n \log n)$

O(*n*)

 $O(\log n)$

O(1)

ΩеΘ

linear search

For each door from left to right

If number is behind door

Return true

Return false

For i from 0 to n-1

Return false

If number behind doors[i]

Return true

 $O(n^2)$

 $O(n \log n)$

O(n) linear search

 $O(\log n)$

O(1)

 $\Omega(n^2)$

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(1)$ linear search

binary search

```
If no doors
    Return false
If number behind middle door
    Return true
Else if number < middle door
    Search left half
Else if number > middle door
    Search right half
```

```
If no doors
    Return false
```

If number behind doors[middle] Return true

Else if number < doors[middle]</pre>

Search doors[0] through doors[middle - 1]

Else if number > doors[middle]

Search doors[middle + 1] through doors[n - 1]

 $O(n^2)$

 $O(n \log n)$

O(*n*)

O(log *n*) binary search

O(1)

 $\Omega(n^2)$

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(1)$ binary search

int numbers[]

Code

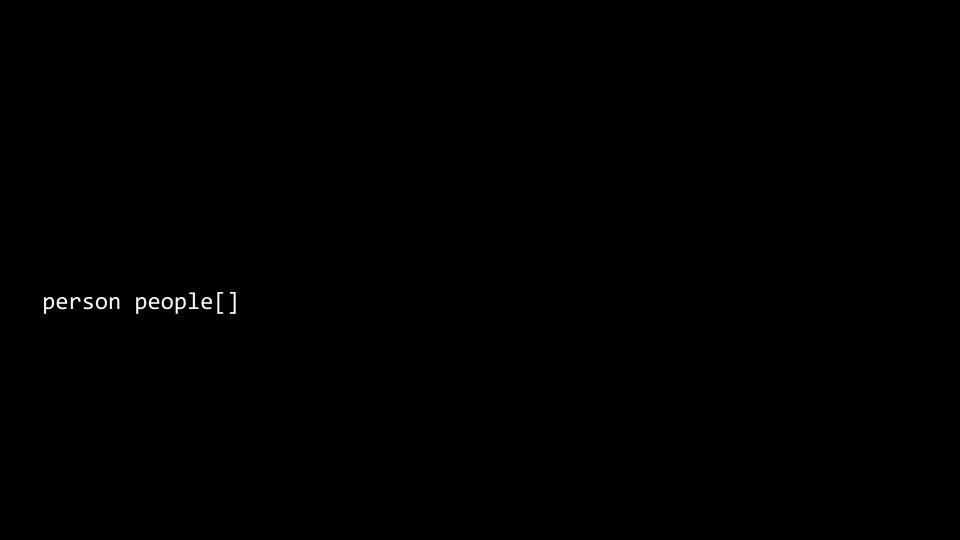
- numbers.c
- names.c
 - o strcmp
- phonebook0.c
 - Telefones como números vs strings?

string names[]

string numbers[]

string names[]

data structures



string name;

string number;

```
typedef struct
{
    string name;
    string number;
}
person;
```

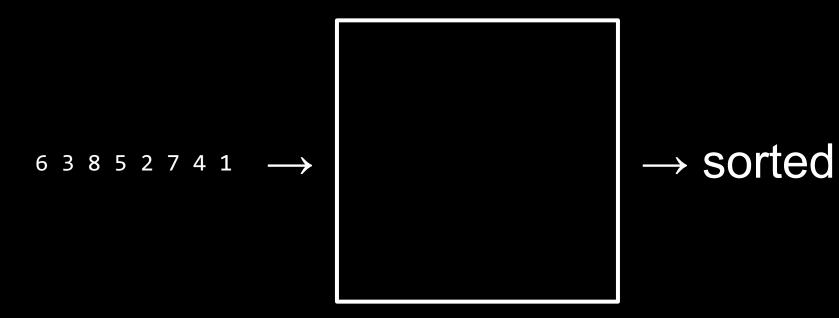
Code

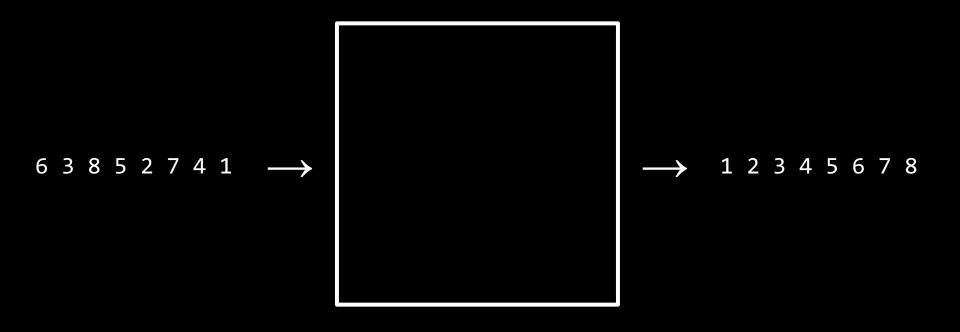
- phonebook1.c
 - o struct em C

sorting

input → output

unsorted → output

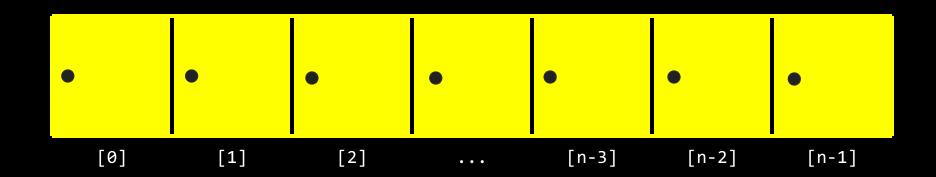




selection sort

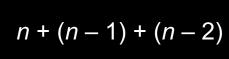
5 2 7 4 1 6 3 0

For	r i from 0 to n-1							
	Find	smallest	number	betwe	een	numbers[i]	and	numbers[n-1]
	Swap	smallest	number	with	nun	mbers[i]		





n + (n - 1)



 $n + (n-1) + (n-2) + \dots + 1$

n + (n-1) + (n-2) + ... + 1n(n + 1)/2

$$n + (n-1) + (n-2) + ... + 1$$

 $n(n + 1)/2$
 $(n^2 + n)/2$

$$n + (n - 1) + (n - 2) + ... + 1$$

 $n(n + 1)/2$
 $(n^2 + n)/2$

 $n^2/2 + n/2$

$$n + (n - 1) + (n - 2) + ... + 1$$

 $n(n + 1)/2$
 $(n^2 + n)/2$
 $n^2/2 + n/2$
 $O(n^2)$

 $O(n^2)$

 $O(n \log n)$

O(*n*)

 $O(\log n)$

O(1)

 $O(n^2)$ selection sort

 $O(n \log n)$

O(*n*)

 $O(\log n)$

O(1)

For	r i from 0 to n-1							
	Find	smallest	number	betwe	een	numbers[i]	and	numbers[n-1]
	Swap	smallest	number	with	nun	mbers[i]		

 $\Omega(n^2)$

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(1)$

 $\Omega(n^2)$ selection sort

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(1)$

 $\Theta(n^2)$

 $\Theta(n \log n)$

 $\Theta(n)$

 $\Theta(\log n)$

Θ(1)

 $\Theta(n^2)$ selection sort

 $\Theta(n \log n)$

 $\Theta(n)$

 $\Theta(\log n)$

Θ(1)

bubble sort

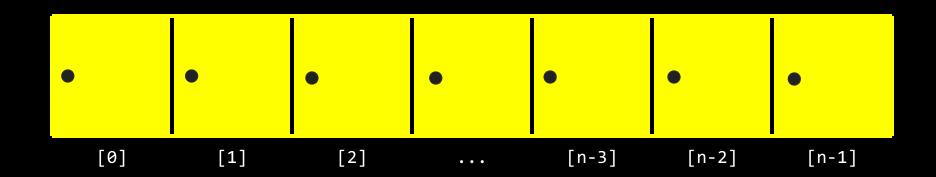
5 2 7 4 1 6 3 0

If numbers[i] and numbers[i+1] out of order

Repeat n-1 times

For i from 0 to n-2

Swap them





$$(n-1) \times (n-1)$$

 $n^2 - 1n - 1n + 1$

$$(n-1) \times (n-1)$$

 $n^2 - 1n - 1n + 1$

 $n^2 - 2n + 1$

$$(n-1) \times (n-1)$$

 $n^2 - 1n - 1n + 1$

$$n^2 - 2n + 1$$

 $O(n \log n)$

O(*n*)

 $O(\log n)$

bubble sort

 $O(n \log n)$

O(*n*)

 $O(\log n)$

Repeat n-1 times For i from 0 to n-2

If numbers[i] and numbers[i+1] out of order

Swap them

If no swaps

Quit

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(n \log n)$

 $\Omega(n)$

bubble sort

 $\Omega(\log n)$

recursion

```
If no doors
    Return false
If number behind middle door
    Return true
Else if number < middle door
    Search left half
Else if number > middle door
    Search right half
```

```
If no doors
    Return false
If number behind middle door
    Return true
Else if number < middle door
    Search left half
Else if number > middle door
    Search right half
```

```
Pick up phone book
    Open to middle of phone book
2
    Look at page
3
4
    If person is on page
5
        Call person
    Else if person is earlier in book
6
        Open to middle of left half of book
        Go back to line 3
8
9
    Else if person is later in book
10
        Open to middle of right half of book
        Go back to line 3
11
12
    Else
        Quit
13
```

```
Pick up phone book
    Open to middle of phone book
2
    Look at page
3
4
    If person is on page
5
        Call person
6
    Else if person is earlier in book
        Open to middle of left half of book
        Go back to line 3
8
9
    Else if person is later in book
10
        Open to middle of right half of book
        Go back to line 3
11
12
    Else
        Quit
13
```

```
Pick up phone book
    Open to middle of phone book
2
    Look at page
3
4
    If person is on page
5
        Call person
6
    Else if person is earlier in book
        Open to middle of left half of book
        Go back to line 3
8
9
    Else if person is later in book
        Open to middle of right half of book
10
        Go back to line 3
11
12
    Else
        Quit
13
```

```
Pick up phone book
    Open to middle of phone book
2
    Look at page
3
4
    If person is on page
5
        Call person
6
    Else if person is earlier in book
        Search left half of book
8
    Else if person is later in book
9
10
        Search right half of book
11
    Else
12
        Quit
13
```

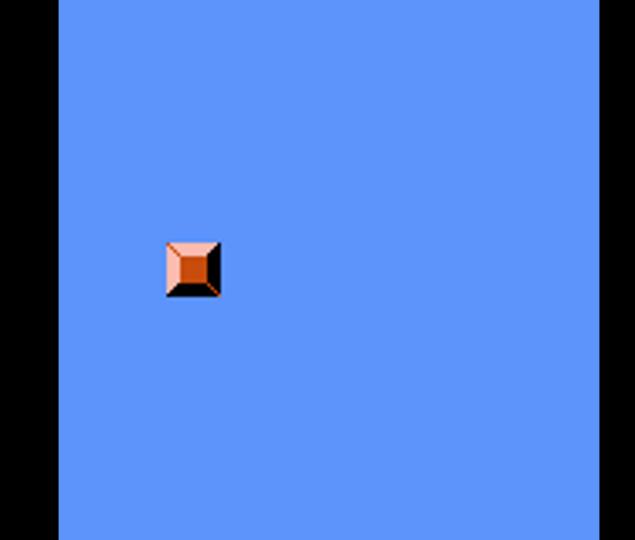
```
Pick up phone book
    Open to middle of phone book
2
    Look at page
3
4
    If person is on page
        Call person
5
6
    Else if person is earlier in book
        Search left half of book
    Else if person is later in book
8
        Search right half of book
9
    Else
10
        Quit
11
```











merge sort

Merge sorted halves

Sort right half of numbers

Sort left half of numbers

```
If only one number
Quit
Else
```

Sort left half of numbers

Sort right half of numbers

Merge sorted halves

```
If only one number
Quit
Else
Sort left half of numbers
Sort right half of numbers
Merge sorted halves
```

2 4 5 7 0 1 3 6

```
If only one number
Quit
Else
Sort left half of numbers
Sort right half of numbers
Merge sorted halves
```

5 2 7 4 1 6 3 0

 $O(n \log n)$

O(*n*)

 $O(\log n)$

 $O(n \log n)$ merge sort

O(*n*)

 $O(\log n)$

 $\Omega(n \log n)$

 $\Omega(n)$

 $\Omega(\log n)$

 $\Omega(n \log n)$ merge sort

 $\Omega(n)$

 $\Omega(\log n)$

 $\Theta(n^2)$

 $\Theta(n \log n)$

 $\Theta(n)$

 $\Theta(\log n)$

Θ(1)

 $\Theta(n^2)$

 $\Theta(n \log n)$ merge sort

 $\Theta(n)$

 $\Theta(\log n)$

Θ(1)

