Emanuele Costantino ASEN 5519 Algorithmic Motion Planning September 9, 2021

Homework 2 Solutions

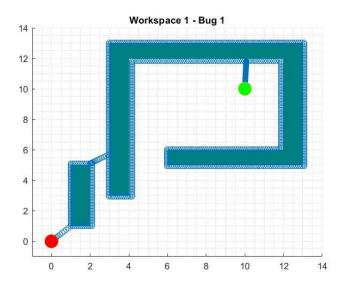
Exercise 1

Handwritten and attached below.

Exercise 2

a) Plot the paths generated by Bug 1 and Bug 2 algorithm.

Below in Figure 1 and Figure 2, the red circle is the start, and the green is the goal. I used blue circles to indicate points on the path. The turquoise rectangles represent the obstacles.



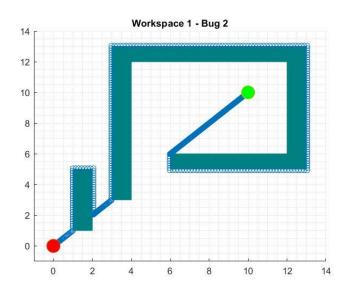
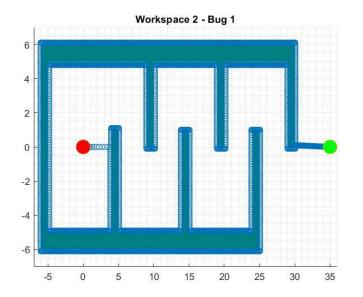


Figure 1: Left turning Bug 1 and Bug 2 algorithms in Workspace 1



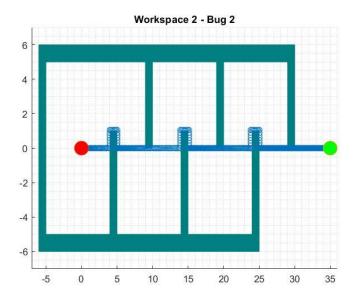


Figure 2: Left turning Bug 1 and Bug 2 algorithms in Workspace 2

b) What are the lengths of the paths generated by Bug 1 and Bug 2 algorithms?

Workspace	Bug	Travel Distance
1	1	133.168
1	2	52.805
2	1	368.633
2	2	41.624

c) Would you expect the same path lengths if the robot were right turning?

Sometime this may be the case for a given workspace but not always. Consider the case below in Figure 3. Using Bug 2 we see that the right turning robot (in red) takes a much shorter path than the left turning robot (in yellow).

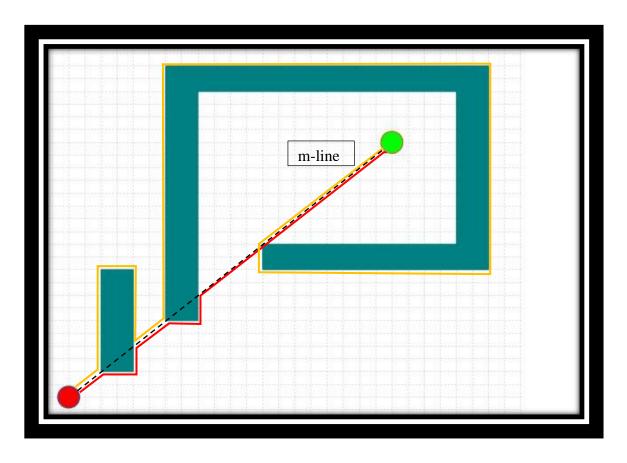
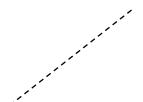
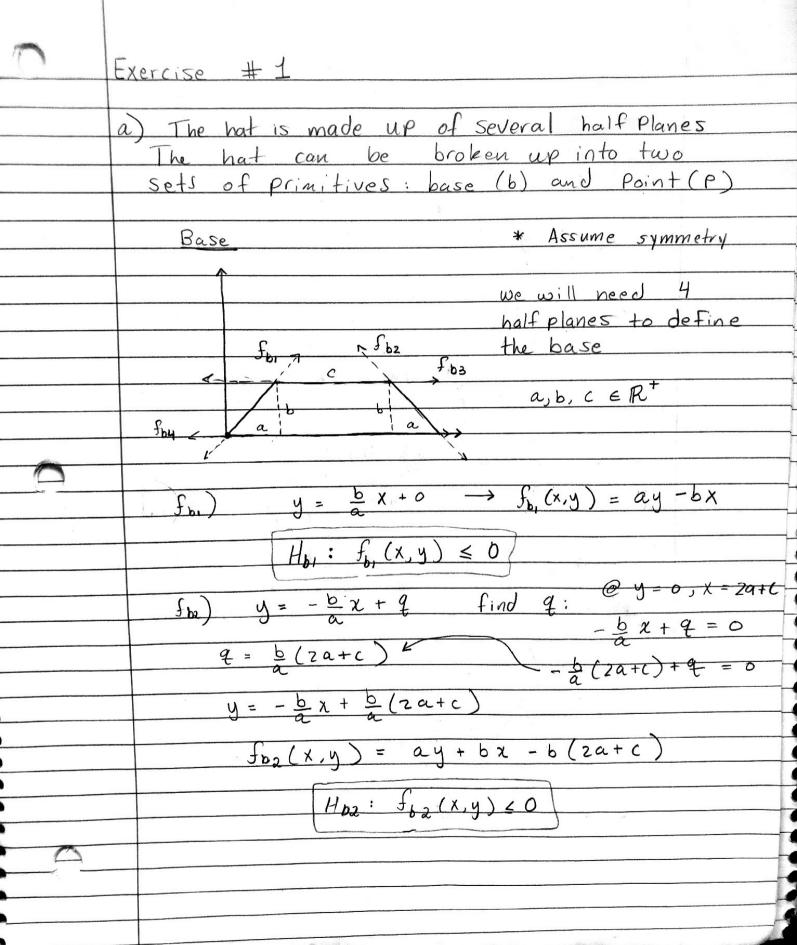
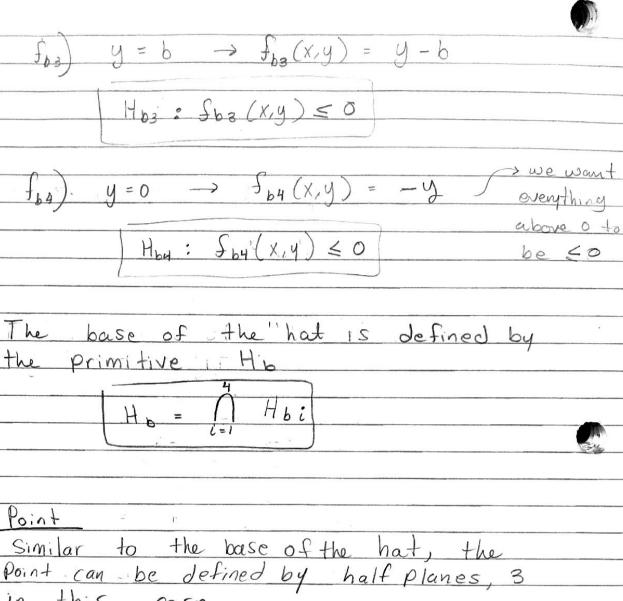


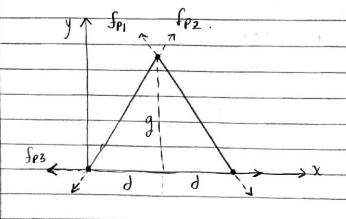
Figure 3: Left vs Right turning Bug 2 algorithm







Similar to the base of the hat, the Point can be defined by half planes, 3 in this case.





$$f_{P_1}$$
 $y = \frac{3}{3}x + 0 \rightarrow f(x,y) = dy - g x$

$$H_{P_1}: f_{P_1}(x,y) < 0$$

$$f_{P2}$$
) $y = -\frac{9}{3}\chi + q \rightarrow @y = 0, \chi = 2d$

$$q = g(2d) = 2g$$

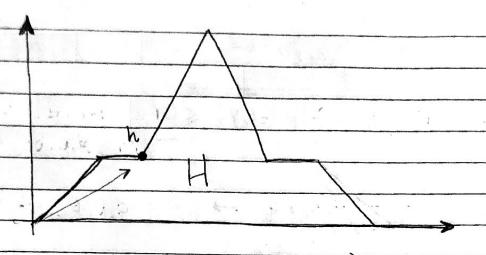
$$y = -9 \times + 29$$

$$y = -9 \times + 29$$

$$f_{p_2}(x,y) = y + \frac{9}{9} \times -29$$

alredy defined for the base

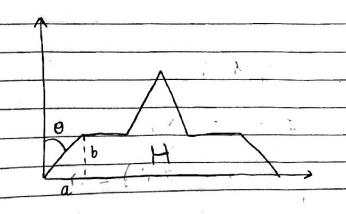
But wait! we have to move the point to the right place!



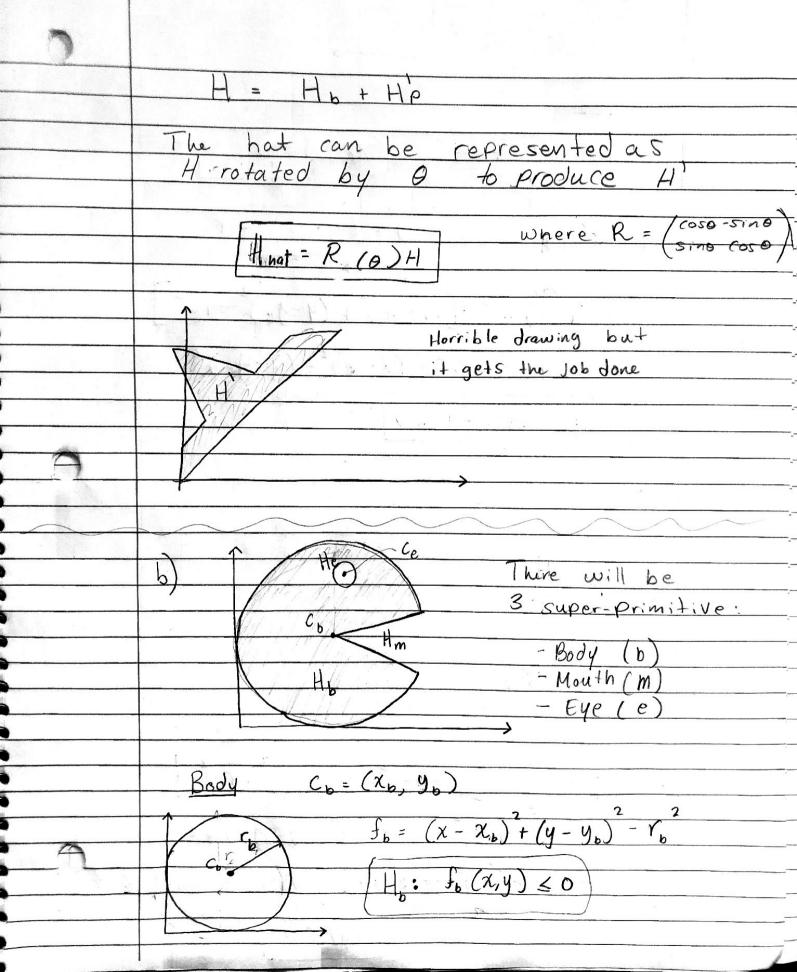
define point $h = (x_n, y_n)$ where we have to translate the point to $f_{P1} = f_{P1}(x - x_P, y - y_P), H_{P1} : f_{P1} \le 0$ $f_{P2} = f_{P2}(x - x_P, y - y_P), H_{P2} : f_{P2} \le 0$ $f_{P3} = f_{P3}(x - x_P, y - y_P), H_{P3} : f_{P3} \le 0$

$$H_{\rho} = \bigcap_{i=1}^{3} H_{\rho_i}$$

Now, we have to rotate by 0



 $\theta = a \tan \left(\frac{a}{b}\right)$

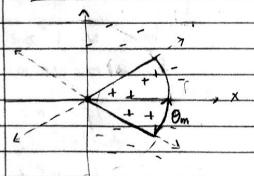


Eye

$$-f(x,y) = (x-xe)^2 + (y-ye)^2 - re^2$$

$$f_e(x,y) = -[(x-xe)^2 + (y-ye)^2 - re^2]$$

Mouth



$$f_{m}(x,y) = -[(x-x_{b})^{2} + (y-y_{b})^{2} - r_{b}^{2}]$$

$$= r_{b}^{2} - (x - x_{b})^{2} - (y - y_{b})^{2}$$

$$f_m(x,y) = \{r_0^2 - (x - x_0)^2 - (y - y_0) \mid x > 0 \land -\theta_m \leq \arctan\left(\frac{y}{x}\right) \leq \theta_m^2\}$$

