Casting-out Nines

Now:

$$8263 = (8 \times 1000) + (2 \times 100) + (6 \times 10) + (3)$$

So:

$$8263 = (8 \times 999) + (2 \times 99) + (6 \times 9) + (8 + 2 + 6 + 3)$$

So:

$$8263 = (9 \times ...) + (8 + 2 + 6 + 3)$$

So:

$$8263 = 8 + 2 + 6 + 3$$
, $mod 9$

So to find N, mod 9 we just add up the digits of N

If you do an addition, subtraction or multiplication then the answer must be correct in mod 9.

Example 1

Eric says 123+35=157

mod 9:

$$LHS = 123 + 35 = (1 + 2 + 3) + (3 + 5) = 6 + 8 + 14 = 5$$

end of mod 9

So Eric's answer must be incorrect.

Example 2

Eric says $3647 \times 7298 = 26615797$

mod 9:

$$LHS = 3647 \times 7298 = (3+6+4+7) \times (7+2+9+8) = 20 \times 26 = 2 \times 8 = 16 = 7$$

end of mod 9

Be careful. We have not shown that Eric's answer must be correct.

We have shown that Eric's answer is either correct or out by a multiple of 9