

TODAY'S CLASS : IMPROVING CONTROLLER'S PERFORMANCE

↳ PID : Detrimental effects of SATURATION

How To COUNTERACT ?

↳ GENERAL CASE : How To "REDUCE" THE EFFORT REQUIRED FROM $C(s)$

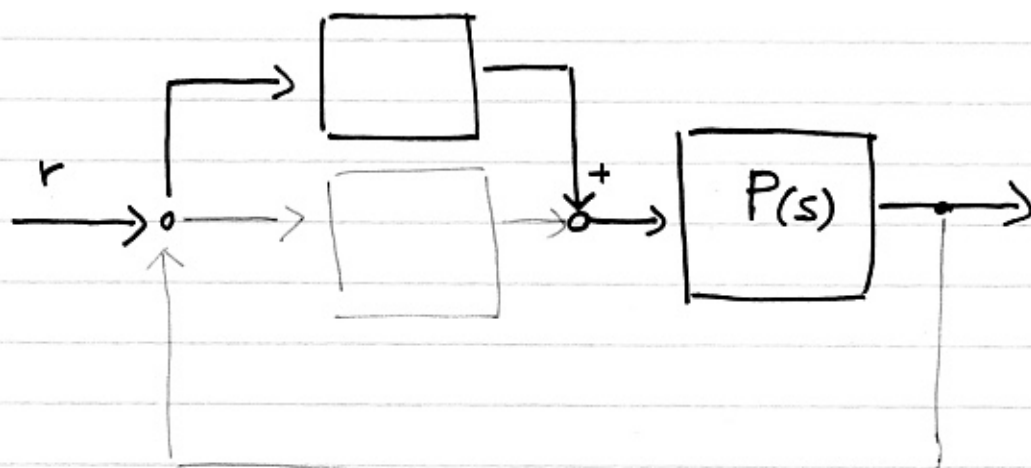
- FEED FORWARD : USE OUR KNOWLEDGE OF $P(s)$

To DESIGN "NOMINAL" CONTROL
(OPEN LOOP)

- Then FEEDBACK IS USED "ONLY" TO COMPENSATE FOR ERRORS, ROBUSTNESS

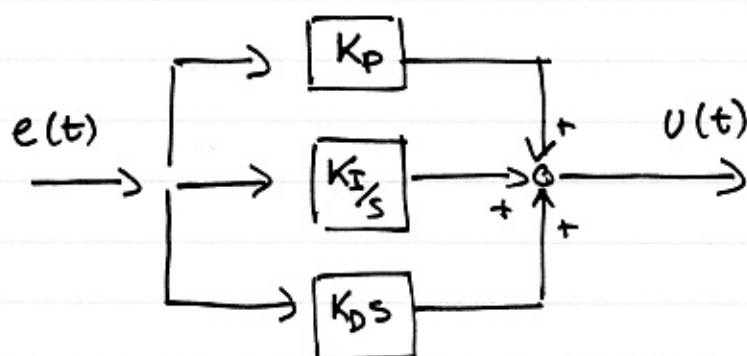
(VIDEO & NOTES)

- AT THE END : EXPLICIT APPLICATION TO OUR CASE
(Feedforward for MOTOR)



How To IMPROVE THE PID RESPONSE ?

- we considered :



- Assume $y(t) = 0$ up to $t = 0$

$$r(t) = 1(t)$$

$$\Rightarrow e(t) \approx 1(t) \quad \text{for very small } t, \text{ with } P(s) \text{ proper}$$

- $K_D s E(s) \approx K_D + \dots$

$$\downarrow \mathcal{L}^{-1}$$

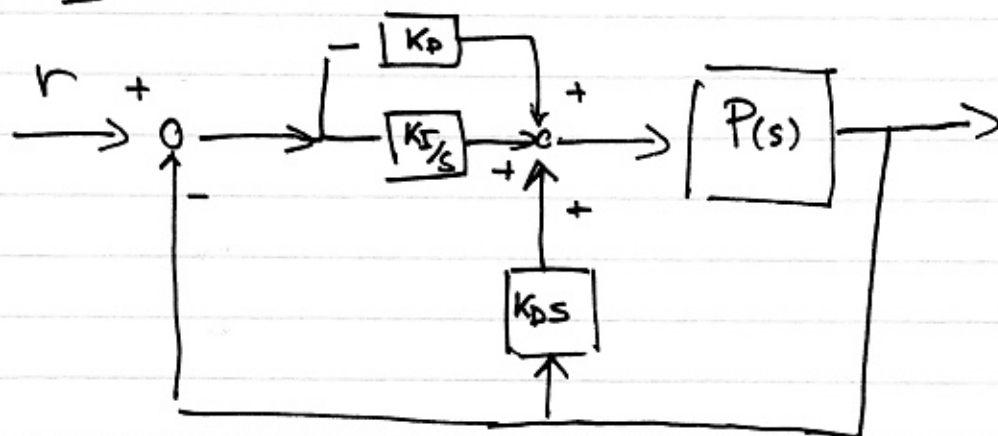
$$K_D \frac{d}{dt} e(t) \approx K_D \delta(t) \quad \leftarrow \text{PART OF } U(t)$$

▷ NON PHYSICAL : we add pole in $-\frac{1}{T_L}$

▷ IT CAN STILL BE VERY HIGH, SATURATE ...

\Rightarrow We can consider a PI - D configuration

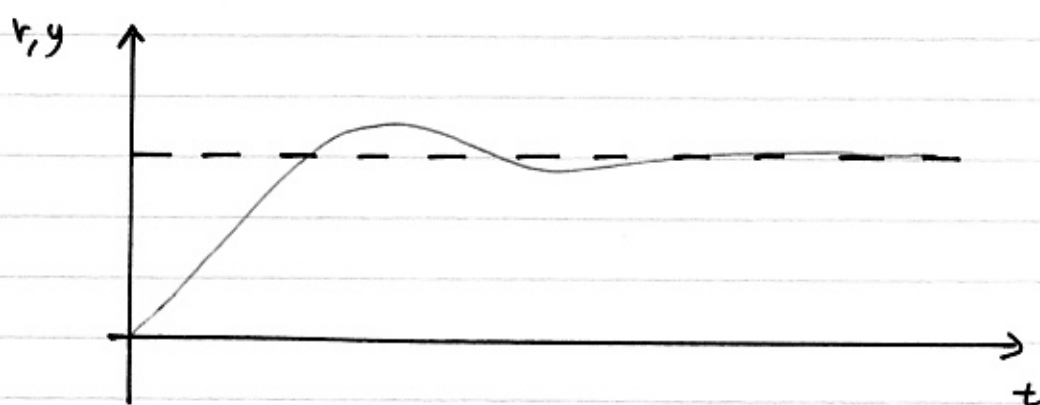
PI-D



$P(s)$ PROPER, TYPICALLY HIGH. REL. DEG. \Rightarrow SMOOTHS THE SIGNAL

- EVEN WITHOUT IMPULSES, HIGH GAINS \Rightarrow SATURATION

what happens?



▷ WITH RESPECT TO THE DESIGNED BEHAVIOUR

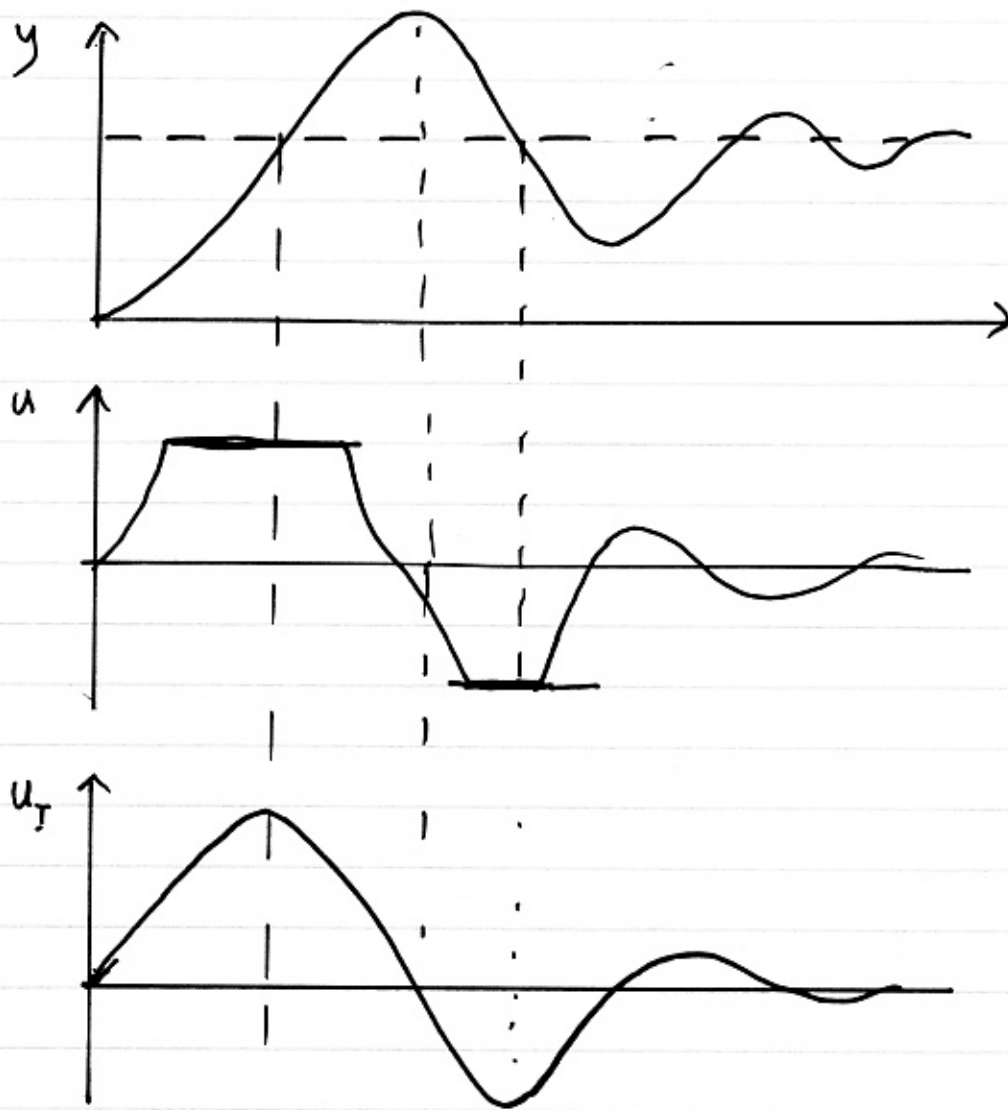
- $e(t)$ is larger, takes longer to $e(t_c) = 0$
- $e(t)$ is INTEGRATED in K_I/s : INERTIA EFFECT

$$U_I(t) = K_I \int_0^t e(\tau) d\tau$$

- the negative $e(t)$ after t_c must erase this accumulated error
- It Takes LONGER for $U(t) = U_p(t) + U_D(t) + U_I(t)$ to SWITCH SIGN

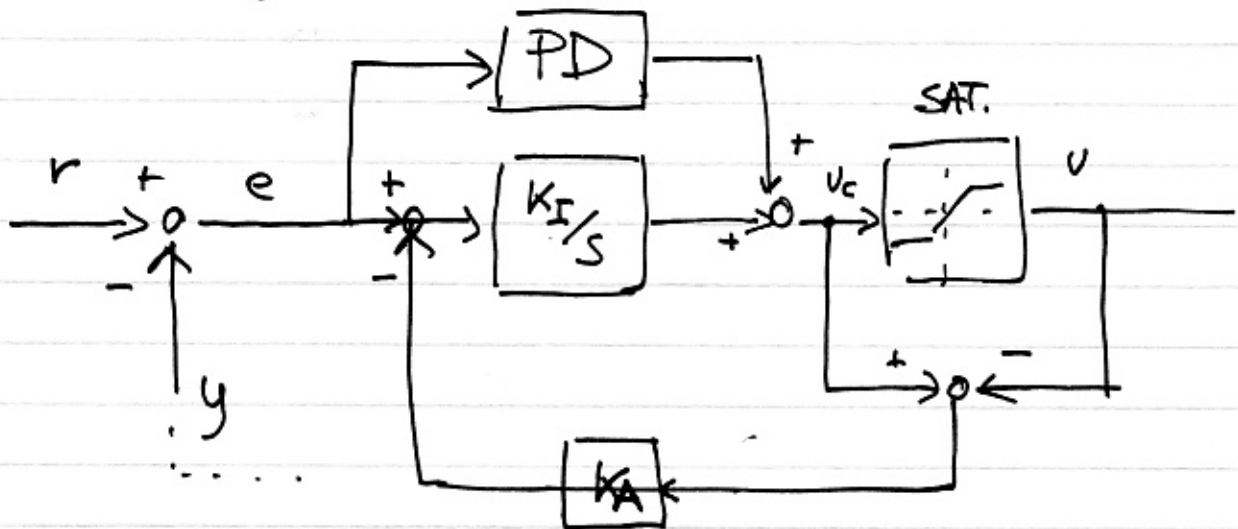
⇒ EXTRA OVERTHOOT,

POSSIBLY also saturation for negative u



⇒ ANTI-WINDUP ARCHITECTURE

- detects saturation
- mitigates effects



• If $U_c = U$, NO SATURATION , "NORMAL" PID

• IF $U_c \neq U$ THE INTEGRATOR INPUT IS

$$e(t) - K_A (U_c(t) - U(t))$$

$$\Delta \rightarrow T_a \simeq (K_A K_I)^{-1} \simeq \frac{t_s^*}{3}$$

APPROXIMATE RELATION FOR DESIGN

← PERFORMANCE SPEC.

$$\Rightarrow K_A = \frac{3}{t_s^* K_I}$$

AS A FIRST, TENTATIVE CHOICE
ADAPT BY TRIAL & ERROR.