Q# 0.15 Language Quick Reference

Primitive Types

64-bit integers	`Int`
Double-precision floats	`Double`
Booleans	`Bool` e.g.: `true` or `false`
Qubits	`Qubit`
Pauli basis	`Pauli` e.g.: `PauliI`, `PauliX`, `PauliY`, or `PauliZ`
Measurement results	`Result` e.g.: `Zero` or `One`
Sequences of integers	`Range` e.g.: `1..10` or `5..-1..0`
Strings	`String` e.g.: `"Hello Quantum!"`
"Return no information" type	`Unit` e.g.: `()`

Derived Types

Arrays	`elementType[]`
Tuples	`(type0, type1, ...)` e.g.: `(Int, Qubit)`
Functions	`input -> output` e.g.: `ArcCos : (Double) -> Double`
Operations	`input => output is variants` e.g.: `H : (Qubit => Unit is Adj)`

User-Defined Types

Declare UDT with anonymous items	`newtype Name = (Type, Type);` e.g.: `newtype Pair = (Int, Int);`
Define UDT literal	`Name(baseTupleLiteral)` e.g.: `let origin = Pair(0, 0);`

Unwrap operator ! (convert UDT to underlying type)	`VarName!`
	e.g.: `let originTuple = origin!;`
	    `(now originTuple = (0, 0))`

Declare UDT with named items	`newtype Name =`
	    `(Name1: Type, Name2: Type);`
	e.g.: `newtype Complex =`
	    `(Re : Double, Im : Double);`

Accessing named items of UDTs	`VarName::ItemName` e.g.: `complexVariable::Re`

Update-and-reassign for named UDT items	`set VarName w/= ItemName <- val;`
	e.g.: `mutable p = Complex(0., 0.);`
	    `set p w/= Re <- 1.0;`

Symbols and Variables

Declare immutable symbol	`let varName = value`
Declare mutable symbol (variable)	`mutable varName = initialValue`
Update mutable symbol (variable)	`set varName = newValue`
Apply-and-reassign	`set varName operator= expression` e.g.: `set counter += 1;`

Functions and Operations

Define function (classical routine)	`function Name(in0 : type0, ...)`
	`: returnType {`
	    `// function body`
	`}`

Call function	`Name(parameters)` e.g.: `let two = Sqrt(4.0);`

Define operation (quantum routine) with explicitly specified body, controlled and adjoint variants	`operation Name(in0 : type0, ...)`
	`: returnType {`
	    `body { ... }`
	    `adjoint { ... }`
	    `controlled { ... }`
	    `adjoint controlled { ... }`
	`}`

Define operation with automatically generated adjoint and controlled variants	`operation Name(in0 : type0, ...)`
	`: returnType is Adj + Ctl {`
	    `...`
	`}`

Call operation	`Name(parameters)` e.g.: `Ry(0.5 * PI(), q);`
Call adjoint operation	`Adjoint Name(parameters)` e.g.: `Adjoint Ry(0.5 * PI(), q);`

Call controlled operation	`Controlled Name(controlQubits, parameters)`
	e.g.: `Controlled Ry(controls,`
	    `(0.5 * PI(), target));`

Control Flow

Iterate over a range of numbers	`for index in range {`
	    `// Use integer index`
	    `...`
	`}`
	e.g.: `for i in 0..N-1 { ... }`

While loop (within functions)	`while (condition) {`
	    `...`
	`}`

Iterate over an array	`for val in array {`
	    `// Use value val`
	    `...`
	`}`
	e.g.: `for q in register { ... }`

Repeat-until-success loop	`repeat { ... }`
	`until condition`
	`fixup { ... }`

Conditional statement	`if cond1 { ... }`
	`elif cond2 { ... }`
	`else { ... }`

Ternary operator	`condition ? caseTrue	caseFalse`
Return a value	`return value`
Stop with an error	`fail "Error message"`
Conjugations ($ABA^\dagger$ pattern)	`within { ... }` `apply { ... }`

Arrays

Allocate array	`mutable name = new Type[length]` e.g.: `mutable b = new Bool[2];`
Get array length	`Length(name)`
Access k-th element	`name[k]` NB: indices are 0-based
Assign k-th element (copy-and-update)	`set name w/= k <- value` e.g.: `set b w/= 0 <- true;`
Array literal	`[value0, value1, ...]` e.g.: `let b = [true, false, true];`
Array concatenation	`array1 + array2` e.g.: `let t = [1, 2, 3] + [4, 5];`

Slicing (subarray)	`name[sliceRange]`
	e.g.: if `t = [1, 2, 3, 4, 5]`, then
	    `t[1 .. 3]` is `[2, 3, 4]`
	    `t[3 ...]` is `[4, 5]`
	    `t[... 1]` is `[1, 2]`
	    `t[0 .. 2 ...]` is `[1, 3, 5]`
	    `t[...-1...]` is `[5, 4, 3, 2, 1]`

Debugging (classical)

Print a string	`Message("Hello Quantum!")`
Print an interpolated string	`Message($"Value = {val}")`

Resources

Documentation

Quantum Development Kit	https://docs.microsoft.com/azure/quantum
QDK user guides	https://docs.microsoft.com/azure/quantum/user-guide
Q# Libraries Reference	https://docs.microsoft.com/qsharp/api

Q# Code Repositories

QDK Samples	https://github.com/microsoft/quantum
QDK Libraries	https://github.com/microsoft/QuantumLibraries
Quantum Katas (tutorials)	https://github.com/microsoft/QuantumKatas
Q# compiler and extensions	https://github.com/microsoft/qsharp-compiler
Simulation framework	https://github.com/microsoft/qsharp-runtime
Jupyter kernel and Python host	https://github.com/microsoft/iqsharp
Source code for the documentation	https://github.com/MicrosoftDocs/quantum-docs

Qubit Allocation

Allocate a register of N qubits	`use reg = Qubit[N];`
	`// Qubits in reg start in ` $|0\rangle$.
	`...`
	`// Qubits must be returned to ` $|0\rangle$.

Allocate one qubit	`use one = Qubit();` `...`

Allocate a mix of qubit registers and individual qubits	`use (x, y, ... ) =`
	`    (Qubit[N], Qubit(), ... );`
	`...`

Debugging (quantum)

Print amplitudes of wave function	`DumpMachine("dump.txt")`
Assert that a qubit is in $|0\rangle$ or $|1\rangle$ state	`AssertQubit(Zero, zeroQubit)` `AssertQubit(One, oneQubit)`

Measurements

Measure qubit in Pauli Z basis	`M(oneQubit)` yields a `Result` (Zero or One)
Reset qubit to $|0\rangle$	`Reset(oneQubit)`
Reset an array of qubits to $|0..0\rangle$	`ResetAll(register)`

Working with Q# from command line

Command Line Basics

Change directory	`cd dirname`
Go to home	`cd ~`
Go up one directory	`cd ..`
Make new directory	`mkdir dirname`
Open current directory in VS Code	`code .`

Working with Q# Projects

Create new project	`dotnet new console -lang Q#` `--output project-dir`
Change directory to project directory	`cd project-dir`
Build project	`dotnet build`
Run all unit tests	`dotnet test`

Math reference

Complex Arithmetic

i^2	-1
$(a+bi)+(c+di)$	$(a+c)+(b+d)i$
$(a+bi)(c+di)$	$a \cdot c + a \cdot di + b \cdot ci + (b \cdot d)i^2 =$ $= (a \cdot c - b \cdot d) + (a \cdot d + b \cdot c)i$
Complex conjugate	$\overline{a+bi} = a - bi$
Division $\frac{a+bi}{c+di}$	$\frac{a+bi}{c+di} \cdot 1 = \frac{a+bi}{c+di} \cdot \frac{c-di}{c-di} = \frac{(a+bi)(c+di)}{c^2+d^2}$
Modulus $\lvert a+bi \rvert$	$\sqrt{a^2+b^2}$
$e^{i\theta}$	$\cos\theta + i\sin\theta$
e^{a+bi}	$e^a \cdot e^{bi} = e^a \cos b + ie^a \sin b$
r^{a+bi}	$r^a \cdot r^{bi} = r^a \cdot e^{bi \ln r} =$ $= r^a \cos(b \ln r) + i \cdot r^a \sin(b \ln r)$
Polar form $re^{i\theta}$ to Cartesian form $a+bi$	$a = r\cos\theta$ $b = r\sin\theta$
Cartesian form $a+bi$ to polar form $re^{i\theta}$	$r = \sqrt{a^2+b^2}$ $\theta = \arctan(\frac{b}{a})$

Linear Algebra

$m \times n$ matrix	$\overbrace{\begin{bmatrix} a_{0,0} & \cdots & a_{0,n-1} \\ \vdots & \ddots & \vdots \\ a_{m-1,0} & \cdots & a_{m-1,n-1} \end{bmatrix}}^{n \text{ columns}} \left.\vphantom{\begin{bmatrix}a\\b\\c\end{bmatrix}}\right\} m \text{ rows}$
Vector of size n	$\begin{bmatrix} a_0 \\ \vdots \\ a_{n-1} \end{bmatrix}$
Addition	$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} e & f \\ g & h \end{bmatrix}$ $\begin{bmatrix} a+e & b+f \\ c+g & d+h \end{bmatrix}$
Scalar product	$a \cdot \begin{bmatrix} b & c \\ d & e \end{bmatrix}$ $\begin{bmatrix} a \cdot b & a \cdot c \\ a \cdot d & a \cdot e \end{bmatrix}$
Matrix product	$\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ $\begin{bmatrix} a \cdot x + b \cdot y + c \cdot z \\ d \cdot x + e \cdot y + f \cdot z \end{bmatrix}$
Transpose	$\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix}^T$ $\begin{bmatrix} a & d \\ b & e \\ c & f \end{bmatrix}$
Adjoint	$\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix}^\dagger$ $\begin{bmatrix} \overline{a} & \overline{e} \\ \overline{b} & \overline{d} \\ \overline{c} & \overline{f} \end{bmatrix}$
Inner product	$\left\langle \begin{bmatrix} a \\ b \end{bmatrix}, \begin{bmatrix} c \\ d \end{bmatrix} \right\rangle$ $\begin{bmatrix} a \\ b \end{bmatrix}^\dagger \begin{bmatrix} c \\ d \end{bmatrix} = \begin{bmatrix} \overline{a} & \overline{b} \end{bmatrix} \begin{bmatrix} c \\ d \end{bmatrix} = \overline{a}c + \overline{b}d$
Outer product	$\begin{bmatrix} a \\ b \end{bmatrix}$ and $\begin{bmatrix} x \\ y \\ z \end{bmatrix}$ $\begin{bmatrix} a \\ b \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}^\dagger = \begin{bmatrix} a \\ b \end{bmatrix} \begin{bmatrix} \overline{x} & \overline{y} & \overline{z} \end{bmatrix} =$ $= \begin{bmatrix} a \cdot \overline{x} & a \cdot \overline{y} & a \cdot \overline{z} \\ b \cdot \overline{x} & b \cdot \overline{y} & b \cdot \overline{z} \end{bmatrix}$

Gates reference

Single Qubit gates

Gate	Matrix representation	Ket-bra representation	Applying to $\lvert\psi\rangle = \alpha\lvert0\rangle + \beta\lvert1\rangle$	Applying to basis states:	$\lvert0\rangle, \lvert1\rangle, \lvert+\rangle, \lvert-\rangle$ and	$\lvert\pm i\rangle = \frac{1}{\sqrt{2}}(\lvert0\rangle \pm i\lvert1\rangle)$
X	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$	$\lvert0\rangle\langle1\rvert + \lvert1\rangle\langle0\rvert$	$\lvert\psi\rangle = \alpha\lvert1\rangle + \beta\lvert0\rangle$	$X\lvert0\rangle = \lvert1\rangle$ $X\lvert1\rangle = \lvert0\rangle$	$X\lvert+\rangle = \lvert+\rangle$ $X\lvert-\rangle = -\lvert-\rangle$	$X\lvert i\rangle = i\lvert-i\rangle$ $X\lvert-i\rangle = -i\lvert i\rangle$
Y	$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$	$i(\lvert1\rangle\langle0\rvert - \lvert0\rangle\langle1\rvert)$	$Y\lvert\psi\rangle = i(\alpha\lvert1\rangle - \beta\lvert0\rangle)$	$Y\lvert0\rangle = i\lvert1\rangle$ $Y\lvert1\rangle = -i\lvert0\rangle$	$Y\lvert+\rangle = -i\lvert-\rangle$ $Y\lvert-\rangle = i\lvert+\rangle$	$Y\lvert i\rangle = \lvert i\rangle$ $Y\lvert-i\rangle = -\lvert-i\rangle$
Z	$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$	$\lvert0\rangle\langle0\rvert - \lvert1\rangle\langle1\rvert$	$Z\lvert\psi\rangle = \alpha\lvert0\rangle - \beta\lvert1\rangle$	$Z\lvert0\rangle = \lvert0\rangle$ $Z\lvert1\rangle = -\lvert1\rangle$	$Z\lvert+\rangle = \lvert-\rangle$ $Z\lvert-\rangle = \lvert+\rangle$	$Z\lvert i\rangle = \lvert-i\rangle$ $Z\lvert-i\rangle = \lvert i\rangle$
I	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	$\lvert0\rangle\langle0\rvert + \lvert1\rangle\langle1\rvert$	$I\lvert\psi\rangle = \lvert\psi\rangle$			
H	$\frac{1}{\sqrt{2}}\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$	$\lvert0\rangle\langle+\rvert + \lvert1\rangle\langle-\rvert$	$H\lvert\psi\rangle = \alpha\lvert+\rangle + \beta\lvert-\rangle = \frac{\alpha+\beta}{\sqrt{2}}\lvert0\rangle + \frac{\alpha-\beta}{\sqrt{2}}\lvert1\rangle$	$H\lvert0\rangle = \lvert+\rangle$ $H\lvert1\rangle = \lvert-\rangle$	$H\lvert+\rangle = \lvert0\rangle$ $H\lvert-\rangle = \lvert1\rangle$	$H\lvert i\rangle = e^{i\pi/4}\lvert-i\rangle$ $H\lvert-i\rangle = e^{-i\pi/4}\lvert i\rangle$
S	$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$	$\lvert0\rangle\langle0\rvert + i\lvert1\rangle\langle1\rvert$	$S\lvert\psi\rangle = \alpha\lvert0\rangle + i\beta\lvert1\rangle$	$S\lvert0\rangle = \lvert0\rangle$ $S\lvert1\rangle = i\lvert1\rangle$	$S\lvert+\rangle = \lvert i\rangle$ $S\lvert-\rangle = \lvert-i\rangle$	$S\lvert i\rangle = \lvert-\rangle$ $S\lvert-i\rangle = \lvert+\rangle$
T	$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$	$\lvert0\rangle\langle0\rvert + e^{i\pi/4}\lvert1\rangle\langle1\rvert$	$T\lvert\psi\rangle = \alpha\lvert0\rangle + e^{i\pi/4}\beta\lvert1\rangle$	$T\lvert0\rangle = \lvert0\rangle$	$T\lvert1\rangle = e^{i\pi/4}\lvert1\rangle$	
$R_x(\theta)$	$\begin{bmatrix} \cos\frac{\theta}{2} & -i\sin\frac{\theta}{2} \\ -i\sin\frac{\theta}{2} & \cos\frac{\theta}{2} \end{bmatrix}$	$\cos\frac{\theta}{2}\lvert0\rangle\langle0\rvert - i\sin\frac{\theta}{2}\lvert1\rangle\langle0\rvert - i\sin\frac{\theta}{2}\lvert0\rangle\langle1\rvert + \cos\frac{\theta}{2}\lvert1\rangle\langle1\rvert$	$R_x(\theta)\lvert\psi\rangle = (\alpha\cos\frac{\theta}{2} - i\beta\sin\frac{\theta}{2})\lvert0\rangle + (\beta\cos\frac{\theta}{2} - i\alpha\sin\frac{\theta}{2})\lvert1\rangle$	$R_x(\theta)\lvert0\rangle = \cos\frac{\theta}{2}\lvert0\rangle - i\sin\frac{\theta}{2}\lvert1\rangle$	$R_x(\theta)\lvert1\rangle = \cos\frac{\theta}{2}\lvert1\rangle - i\sin\frac{\theta}{2}\lvert0\rangle$	
$R_y(\theta)$	$\begin{bmatrix} \cos\frac{\theta}{2} & -\sin\frac{\theta}{2} \\ \sin\frac{\theta}{2} & \cos\frac{\theta}{2} \end{bmatrix}$	$\cos\frac{\theta}{2}\lvert0\rangle\langle0\rvert + \sin\frac{\theta}{2}\lvert1\rangle\langle0\rvert - \sin\frac{\theta}{2}\lvert0\rangle\langle1\rvert + \cos\frac{\theta}{2}\lvert1\rangle\langle1\rvert$	$R_y(\theta)\lvert\psi\rangle = (\alpha\cos\frac{\theta}{2} - \beta\sin\frac{\theta}{2})\lvert0\rangle + (\beta\cos\frac{\theta}{2} + \alpha\sin\frac{\theta}{2})\lvert1\rangle$	$R_y(\theta)\lvert0\rangle = \cos\frac{\theta}{2}\lvert0\rangle + \sin\frac{\theta}{2}\lvert1\rangle$	$R_y(\theta)\lvert1\rangle = \cos\frac{\theta}{2}\lvert1\rangle - \sin\frac{\theta}{2}\lvert0\rangle$	
$R_z(\theta)$	$\begin{bmatrix} e^{-i\theta/2} & 0 \\ 0 & e^{i\theta/2} \end{bmatrix}$	$e^{-i\theta/2}\lvert0\rangle\langle0\rvert + e^{i\theta/2}\lvert1\rangle\langle1\rvert$	$R_z(\theta)\lvert\psi\rangle = \alpha e^{-i\theta/2}\lvert0\rangle + \beta e^{i\theta/2}\lvert1\rangle$	$R_z(\theta)\lvert0\rangle = e^{-i\theta/2}\lvert0\rangle$	$R_z(\theta)\lvert1\rangle = e^{i\theta/2}\lvert1\rangle$	
$R_1(\theta)$	$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\theta} \end{bmatrix}$	$\lvert0\rangle\langle0\rvert + e^{i\theta}\lvert1\rangle\langle1\rvert$	$R_1(\theta)\lvert\psi\rangle = \alpha\lvert0\rangle + \beta e^{i\theta}\lvert1\rangle$	$R_1(\theta)\lvert0\rangle = \lvert0\rangle$	$R_1(\theta)\lvert1\rangle = e^{i\theta}\lvert1\rangle$	

Two-qubit gates

Gate	Matrix Representation	Ket-Bra Representation	Applying to $\lvert\psi\rangle = \alpha\lvert00\rangle + \beta\lvert01\rangle + \gamma\lvert10\rangle + \delta\lvert11\rangle$	Applying to basis states	
CNOT	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$	$\lvert00\rangle\langle00\rvert + \lvert01\rangle\langle01\rvert + \lvert11\rangle\langle10\rvert + \lvert10\rangle\langle11\rvert$ or $\lvert0\rangle\langle0\rvert \otimes I + \lvert1\rangle\langle1\rvert \otimes X$	$\text{CNOT}\lvert\psi\rangle = \alpha\lvert00\rangle + \beta\lvert01\rangle + \boldsymbol{\delta\lvert10\rangle} + \boldsymbol{\gamma\lvert11\rangle}$	$\text{CNOT}\lvert00\rangle = \lvert00\rangle$ $\text{CNOT}\lvert01\rangle = \lvert01\rangle$	$\text{CNOT}\lvert10\rangle = \lvert11\rangle$ $\text{CNOT}\lvert11\rangle = \lvert10\rangle$
SWAP	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$\lvert00\rangle\langle00\rvert + \lvert01\rangle\langle10\rvert + \lvert10\rangle\langle01\rvert + \lvert11\rangle\langle11\rvert$	$\text{SWAP}\lvert\psi\rangle = \alpha\lvert00\rangle + \boldsymbol{\gamma\lvert01\rangle} + \boldsymbol{\beta\lvert10\rangle} + \delta\lvert11\rangle$	$\text{SWAP}\lvert00\rangle = \lvert00\rangle$ $\text{SWAP}\lvert01\rangle = \lvert10\rangle$	$\text{SWAP}\lvert10\rangle = \lvert01\rangle$ $\text{SWAP}\lvert11\rangle = \lvert11\rangle$
Controlled U	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & a_{0,0} & a_{0,1} \\ 0 & 0 & a_{1,0} & a_{1,1} \end{bmatrix}$	$\lvert0\rangle\langle0\rvert \otimes I + \lvert1\rangle\langle1\rvert \otimes U$	$\text{CU}\lvert\psi\rangle = \alpha\lvert00\rangle + \beta\lvert01\rangle + (\gamma a_{0,0} + \delta a_{0,1})\lvert10\rangle + (\gamma a_{1,0} + \delta a_{1,1})\lvert11\rangle$	$\text{CU}\lvert00\rangle = \lvert00\rangle$ $\text{CU}\lvert01\rangle = \lvert01\rangle$	$\text{CU}\lvert10\rangle = a_{0,0}\lvert10\rangle + a_{1,0}\lvert11\rangle$ $\text{CU}\lvert11\rangle = a_{0,1}\lvert10\rangle + a_{1,1}\lvert11\rangle$

Toffoli (CCNOT) gate

Gate	Matrix Representation	Ket-Bra Representation	Applying to $\lvert\psi\rangle = \alpha\lvert000\rangle + \beta\lvert001\rangle + \gamma\lvert010\rangle + \delta\lvert011\rangle + \epsilon\lvert100\rangle + \lambda\lvert101\rangle + \eta\lvert110\rangle + \kappa\lvert111\rangle$	Applying to basis states	
CCNOT	$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}$	$(I_2 - \lvert11\rangle\langle11\rvert) \otimes I_1 + \lvert11\rangle\langle11\rvert \otimes X$	$\text{CCNOT}\lvert\psi\rangle = \alpha\lvert000\rangle + \beta\lvert001\rangle + \gamma\lvert010\rangle + \delta\lvert011\rangle + \epsilon\lvert100\rangle + \lambda\lvert101\rangle + \boldsymbol{\kappa\lvert110\rangle} + \boldsymbol{\eta\lvert111\rangle}$	$\text{CCNOT}\lvert000\rangle = \lvert000\rangle$ $\text{CCNOT}\lvert001\rangle = \lvert001\rangle$ $\text{CCNOT}\lvert010\rangle = \lvert010\rangle$ $\text{CCNOT}\lvert011\rangle = \lvert011\rangle$	$\text{CCNOT}\lvert100\rangle = \lvert100\rangle$ $\text{CCNOT}\lvert101\rangle = \lvert101\rangle$ $\text{CCNOT}\lvert110\rangle = \lvert111\rangle$ $\text{CCNOT}\lvert111\rangle = \lvert110\rangle$