

# DEMO/LAB: Springs & Elastics in Parallel vs Series

Overview: This lab will be using rubber bands to model springs  $k$  constant when in various configurations

Materials needed:

Meterstick version:

3 pencils

Heavy Textbook

Various rubber bands

Phone Camera with slo mo

Meterstick

Scale to find weight of pencil, or find answer in terms of “pencils”

Twist ties

Note: you need some way to measure vertically, for the displacement of the rubber and for the vertical height maximum it reaches

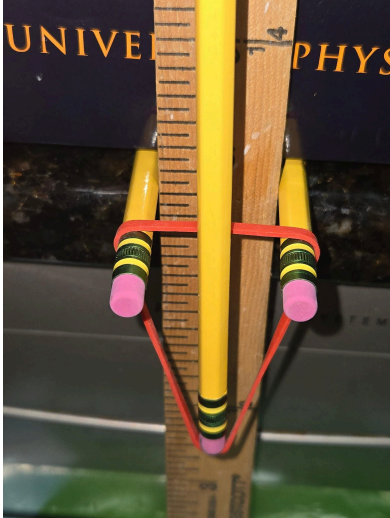
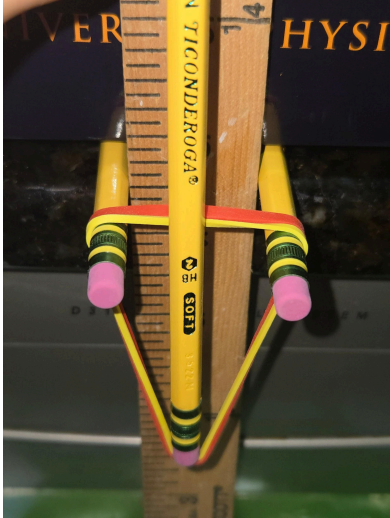

## Procedure

Finding  $K$  for one rubber band:

1. Place two pencils parallel to each other, half of the pencil off the ledge of a table, and use a textbook to hold them in place
2. Place a rubber band on the pencil and pull it down until you find its equilibrium position
3. From here, pick a vertical displacement down from the equilibrium and note it down
4. Put a pencil in the rubber band while it's displaced
5. Let go of the rubber band and be sure to find its vertical maximum when it's launched. You can use a video camera to see exactly what its vertical height is
6. If you do not have a meterstick tall enough to measure the height, you can perform kinematics to directly calculate exit velocity (fig 2) use your video recording to find the time it took to go from launch exit position to the maximum height
7. Take several videos to ensure accuracy and then average the result
8. Repeat the procedure with several different displacements to ensure accuracy

Finding  $K$  for rubber bands in parallel and in series

Refer to the diagrams on how to set up the rubber band in series and in parallel

| Single Band (equalibrium)   | Paralell (equalibrium)   | Series (stretched out)  |
|---|--|---|
|  |  |  |

proving that my series configuration works



Test question

If I put use a weight to find the relative displacements between the rubber bands by themselves and then together in series (the way i think it would work for them to be attached), I can find out whether the way I attached them is equivalent to attaching them in series

both ~ 12cm<<13

yellow ~ 7cm

red ~ 6.5cm

$$F = kx$$

$$k = \frac{F}{x}$$

$$k_b = \frac{F}{12.6}$$

$$k_y = \frac{F}{7}$$

$$k_r = \frac{F}{6.5}$$

$$\frac{1}{k_b} = \frac{1}{k_r} + \frac{1}{k_y}$$

$$12.6 \approx 7 + 6.5$$

$$7 + 6.5 = 13.5$$

Margin of error <1

Result: my method is adequate to result in series behavior

## Lab tables

Pencil Mass: (i looked it up, i have a fresh pencil) 6.5 grams or 0.0065 kg

Rubber band 1

Displacement: \_\_\_\_ 1 1/8 inch \_\_\_\_

| Trial   | Height (in) |
|---------|-------------|
| 1       | 18.875      |
| 2       | 14.125      |
| 3       | 22.75       |
| 4       | 14.125      |
| 5       | 17.125      |
| average | 17.4        |

Feel free to do more trials for accuracy

Rubber band 2

Displacement: \_\_ 1 1/8 inch \_\_\_\_

| Trial | Height (in) |
|-------|-------------|
| 1     | 4.125       |
| 2     | 7.5         |
| 3     | 22.125      |

|         |             |
|---------|-------------|
| 4       | 199.5       |
| 5       | 15.75       |
| 6       | 15.375      |
| 7       | 8.5         |
| average | 38.98214286 |

In Parallel

Displacement: 1 2/8 in

| Trial   | Height |
|---------|--------|
| 1       | 24.25  |
| 2       | 17.125 |
| 3       | 29.125 |
| 4       | 20.875 |
| 5       | 19.125 |
| average | 22.1   |

In Series

Displacement: 1 7/8 in

| Trial   | Height |
|---------|--------|
| 1       | 9.625  |
| 2       | 10.125 |
| 3       | 13.625 |
| 4       | 9      |
| 5       | 12.875 |
| average | 11.05  |

## Calculations

Using the data you collected, determine a formula for finding k. Variables should include h (height), m (mass of pencil), x (displacement of rubber band from equilibrium)

$$k = \frac{384.16mh^2}{x_{disp}^2}$$

Using your derivation above, calculate the experimental value for K in each of your tables.

I converted everything to m

$$k_{r1} = \frac{384.16(0.0065)(0.44196)^2}{0.028575^2} = 597.226$$

$$k_{r2} = \frac{384.16(0.0065)(0.990146429)^2}{0.028575^2} = 2998.139$$

$$k_p = \frac{384.16(0.0065)(0.56134)^2}{0.03175^2} = 0.00196$$

$$k_s = \frac{384.16(0.0065)(0.28067)^2}{0.047625^2} = 0.000489$$

My calculations did not go according to plan, i believe i have made a big calculation flaw somewhere. It was strange converting to m from inches

In AP Physics C Electricity and Magnetism, it is learned that components in series are added together while components in parallel are sums of each component's inverse. Student B claims that the behavior of rubber bands should be the same. Using your calculated data, explain whether Student B's claims are correct or incorrect.

Student B is incorrect as my results show that it is the other way around. Rubber bands in parallel behave as added, while in series, sum of their inverse.

## Post Lab Questions

1. How does the behavior of rubber bands in parallel differ from those in series when a weight is applied? Describe the difference in terms of displacement and constant K  
When rubber bands are in parallel, each band shares the load, so the displacement would be less for the same applied force compared to a single band. The spring constant follows this rule  $K=K_1+K_2$

In contrast, when they are in series the load is distributed across the entire stretch of both bands, and there is more displacement for the same force, so it would have the following behavior:

$$1/k = 1/k_1 + 1/k_2$$

2. Based on your height measurements, which configuration had the highest launch height if they were to be at the same displacement? Does this match your conclusion in response to Student B?

I had calculation error but it should be the configuration in parallel

3. How does conservation of energy take place in this lab?

Conservation of energy is demonstrated in this lab as the initial spring potential energy ( $\frac{1}{2} kx^2$ ) is directly responsible for the exit velocity ( $\frac{1}{2}mv^2$ ) and the final height.

4. If you were to double the number of rubber bands in parallel, what would happen to the height?

It would just be  $2k$