Starting Equations:

$$\begin{aligned} class1: A &= [2,2]^T, B = [3,5]^T \\ class1\_bias: A &= [1,2,2]^T, B = [1,3,5]^T \\ class2: C &= [1,3]^T, D = [-1,-0.5]^T \\ class2\_bias: C &= [1,1,3]^T, D = [1,-1,-0.5]^T \\ initial_weight_vector: W0 &= [1,1,1]^T \end{aligned}$$

First Step of weight vector updating:

$$W0*A = 5(OK)$$
 
$$W0*B = 9(OK)$$
 
$$W0*C = 5(NOTOK)$$
 
$$W1 = W0 - C = [0, 0, -2]$$
 
$$W1*D = 1(NOTOK)$$
 
$$W2 = W1 - D = [-1, 1, -1.5]$$

Second Step of weight vector updating:

$$W2*A = -2(NOTOK)$$

$$W3 = W2 + A = [0, 3, 0.5]$$

$$W3*B = 11.5(OK)$$

$$W3*C = 4.5(NOTOK)$$

$$W4 = W3 - C = [-1, 2, -2.5]$$

$$W4*D = -1.75(OK)$$

Third Step of weight vector updating:

$$W4*A = -2(NOTOK)$$
 
$$W5 = W4 + A = [0, 4, -0.5]$$
 
$$W5*B = 9.5(OK)$$
 
$$W5*C = 2.5(NOTOK)$$
 
$$W6 = W5 - C = [-1, 3, -3.5]$$
 
$$W6*D = -2.25(OK)$$

Four Step of weight vector updating:

$$W6*A = -2(NOTOK)$$
 
$$W7 = W6 + A = [0, 5, -1.5]$$
 
$$W7*B = 7.5(OK)$$
 
$$W7*C = 0.5(NOTOK)$$
 
$$W8 = W7 - C = [-1, 4, -4.5]$$
 
$$W8*D = -2.75(OK)$$

Five Step of weight vector updating:

$$W8*A = -2(NOTOK)$$
 
$$W9 = W8 + A = [0, 6, -2.5]$$
 
$$W9*B = 5.5(OK)$$
 
$$W9*C = -1.5(OK)$$
 
$$W9*D = -4.75(OK)$$

Final result:

$$W9 * A = 7.000000$$
  
 $W9 * B = 5.500000$   
 $W9 * C = -1.500000$   
 $W9 * D = -4.750000$   
 $W9 = [0, 6, -2.5]$ 

ANSWER: 71.0208% majority vote accuracy

```
By Hand:
  probability <- .6</pre>
  number_of_weak_learners <- 7</pre>
  x <- ceiling(number_of_weak_learners/2)</pre>
  final_sum <- 0
  for(i in number_of_weak_learners:x) {
    binomial_coefficient <- (factorial(number_of_weak_learners) /</pre>
                                       (factorial(i) * factorial(number_of_weak_learners-i)))
    p <- probability^i</pre>
    np <- (1-probability)^(number_of_weak_learners-i)</pre>
    final_sum <- final_sum + (binomial_coefficient * p * np)</pre>
  print(final_sum)
R Packages:
  final_sum <- dbinom(7, size=7, prob=0.6) +</pre>
                dbinom(6, size=7, prob=0.6) +
                dbinom(5, size=7, prob=0.6) +
                dbinom(4, size=7, prob=0.6)
```