

Section 1 – Parallel Computing

Question 1. MPI Programming.

- (a) Explain, and give the full prototype for the following MPI routines: `MPI_Bcast()`, `MPI_Reduce()`, `MPI_Send()`, `MPI_Recv()`, `MPI_Init()`. (10 marks)
- (b) Develop a MPI function for the compare and exchange operation. The prototype of the method can be

`int MPI_Exchange(int n, int *a, int rank1, int rank2, MPI_Comm comm)`

where the arguments are as follows:

`n` - the array size;

`a` - the array

`rank1, rank2` - the processors to exchange

`comm` - the communicator

Note: You do not have to write a routine to merge two arrays. (20 marks)

- (c) Justify why `MPI_Exchange` is an efficient solution for the compare and exchange operation. (10 marks)

Question 2. Parallel Algorithms

- (a) Give an explanation of how the odd-even sort works and write a method for it. The prototype of this method can be:

`int MPI_Sort(int n, int *a, int root, MPI_Comm comm)`

- (b) Evaluate the theoretical complexity of `MPI_Sort` and explain the communication and computation overheads of the method. (20 marks)
- (c) Prove that `MPI_Sort` finishes the sorting in $size$ repetitions, where $size$ represents the number of processors. (10 marks)