

Demultiplexor (DeMux)

Takes 1 input, n select lines, and has 2^n outputs. Used to select which output the input is routed to.

Challenge: Draw the circuit diagram for a 1-4 demux

Multiplexors and demultiplexors can work together to transmit information over a single data line and n control lines.

So 2^n inputs are transmitted over $n+1$ long distance lines instead of 2^n . This number can be reduced to ≈ 1 line under certain circumstances, regardless of the size of n .

(Note long distance may mean just a metre, or some distance on a circuit board.)

USB

A USB keyboard, for example, will have five wires connecting to the computer. Two for data, one for ground, one for power, and one for a clock.

Here, the select lines of the mux and demux change together. By changing the combination of inputs on the select lines from $0\dots 0$ to $1\dots 1$, each input of the mux will in turn be sent to the corresponding output of the demux.

Terminology

Black Box

A black box is a device whose output depends only on its inputs. You don't need to know how it works or what is inside.

With a black box, we abstract away detail and consider only functionality. We've seen this already when building a multibit adder from many full adders.

We can take it further by representing the multibit (4-bit in this case) adder as a black box itself, with 8 inputs, 4 outputs, a carry-in, and a carry-out.

Carry-In in Multibit Adders

For just addition of two numbers you don't actually need a carry-in (you'll be setting it to 0), but it's useful for other things (e.g. you can subtract numbers using adders by manipulating the carry-ins).

Limitations

Let's look at the limitations of using a fixed number of bits to represent information (numbers in this example).

With 32 bits, we can represent 2^{32} different 32-bit patterns, where each pattern can represent a unique thing:

000.....000	0
000.....001	1
...	
111.....111	4,294,967,295

If we add 1 to this last number, since we don't have a 33rd bit, we get 0 again.

Typically there is a 33rd bit, which is used to tell if we have overflowed the limit of the 32-bit number. If it's 1, there is overflow, if it's 0, there isn't.