# qTesla

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## 1 Implementação qTesla

Abaixo temos a implementação do esquema de assinaturas pós-quantico qTesla conforme as especificações da segunda submissão para o concurso do NIST.

```
[24]: import os import random from cryptography.hazmat.primitives import hashes
```

Parâmetros do qTesla Abaixo temos um dos conjuntos pré definidos de parâmetros para o qTesla.

```
[34]: '''
      Lambda = 95
      kappa = 256
      n = 1024
      k = 4
      q = 343576577
      sigma = 8.5
      LE = 554, 2.61
      LS = 554, 2.61
      E = 554
      S = 554
      B = 2^19 - 1
      d = 22
      h = 25
      bGenA = 108
      rateXOF = 168
      {\it CDTParams}
      beta = 64
      precision 63
      t = 78
      size = 624
```

```
[34]: '\nLambda = 95\nkappa = 256\nn = 1024\nk = 4\nq = 343576577\nsigma = 8.5\nLE = 554, 2.61\nLS = 554, 2.61\nE = 554\nS = 554\nB = 2^19 - 1\nd = 22\nh = 25\nbGenA = 108\nrateXOF = 168\nCDTParams \nn: 64 \ncdt_v: 63 beta: 78 624\n'
```

## 1.0.1 Geração do Par de Chaves

```
[17]: def gen():
          # 1
          counter = 1
          # 2
          pre_seed = os.urandom(32)
          # 3
          seed = PRF1(pre_seed)
          seeda = seed[len(seed) - 2]
          seedy = seed[len(seed) - 1]
          # 4
          a = GenA(seeda)
          # 6
          s = GaussSampler(seed[0], counter)
          # 7
          counter += 1
          # 5
          while checkS(s) != 0:
              s = GaussSampler(seed[0], counter)
              # 7
              counter += 1
          # 8
          e = []
          t = []
          # 9
          for i in range(1, 4+1):
              # 11
              e.append(GaussSampler(seed[i], counter))
              # 12
              counter += 1
              # 13
              while checkE(e[i]) != 0:
                  # 11
                  e[i] = GaussSampler(seed[i], counter)
                  # 12
                  counter += 1
              t.append((a[i - 1]*s + e[i]) \% 343576577)
```

```
g = G(t)
sk = (s, e, seeda, seedy, g)
pk = (t, seeda)
return sk, pk
```

### 1.0.2 Assinatura

```
[3]: def sign(m, sk):
         (s, e, seeda, seedy, g) = sk
         # 1
         counter = 1
         # 2
         r = os.urandom(32)
         # 3
        rand = PRF2(seedy, r, G(m))
         stop = 0
         while stop != 1:
             # 4
             y = ySampler(rand, counter)
             # 5
             a = GenA(seeda)
             # 6
             v = []
             for i in range(4):
                 # 7
                 v.append((a[i] * y) % 343576577)
                 v[i] = v[i] - (343576577//2)
             # 9
             cl = H(v, G(m), g)
             # 10
             c = Enc(c1)
             # 11
             z = y + s*c
             stop = 1
             # 12 TODO condition1
             if condition1 :
                 counter += 1
                 stop = 0
             # 16
             w = []
```

```
stop = 1
for i in range(4):
    # 17
    w.append((v[i] - (e[i]*c)) % 343576577)
    w[i] = w[i] - (343576577//2)
    # 18 TODO condition2, condition3
    if condition2 | condition3:
        # 19
        counter += 1
        # 20
        stop = 0
return (z, cl)
```

## 1.0.3 Verificação

```
[4]: def verify(m, signature, pk):
         (z, cl) = signature
         (t, seeda) = pk
         # 1
         c = Enc(c1)
         # 2
         a = GenA(seeda)
         w = []
         # 3
         for i in range(k):
            # 4
             w.append((((a[i]*z) - (t[i]*c)) \% 343576577))
             w[i] = w[i] - (343576577//2)
         # 6 TODO condition1
         if condition1 | cl != H(w, G(m), G(t)):
             return -1
         return 0
```

## 1.0.4 Execução de um Teste

```
[]: pk, sk = Gen()

M = os.urandom(32)

signature = Sign(M, sk)

done = Verify(M, signature, pk)
```

```
if done == 0:
    print('True')
else:
    print('False')
```

#### 1.0.5 PRF1

```
[32]: def PRF1(pre_seed):
    n = 4+3
    digest = hashes.Hash(hashes.SHAKE128(int((256*n)//8)))
    digest.update(pre_seed)
    buffer = digest.finalize()

    n = 32

    return [buffer[x: x+n] for x in range(0, len(buffer), n)]
```

## 1.0.6 G

```
[25]: def G(string):
    digest = hashes.Hash(hashes.SHAKE128(int(40))
    digest.update(string)
    return digest.finalize()
```

#### 1.0.7 PRF2

```
[7]: def PRF2(seedy, r, m):
    string = seedy + r + m
    digest = hashes.Hash(hashes.SHAKE128(int(32))
    digest.update(string)
    return digest.finalize()
```

## 1.0.8 GenA

```
[8]: def GenA(seeda):
    D = 0

    b = logb(q,2) / 8
    b = b.ceil()
    bl = 108

    c = cSHAKE128(seeda, 168*bl, D)

    i = 0
    pos = 0
    while(i < 4096):</pre>
```

```
x = (168*bl) // b
if pos > x - 1:
    D += 1
    pos = 0
    bl = 1
    c = cSHAKE128(seeda, 168*bl, D)

x = logb(q,2)
x = x.ceil()
x = 2^x
x = c[pos] % x
if x < 343576577:
    # TODO linha 10
    i += 1
pos += 1</pre>
return a
```

## 1.0.9 GaussSampler

```
[9]: def GaussSampler(seed, D):
         D1 = D * (2^8)
         z = []
         for i in range(1024 * 512):
             z.append(0)
         for i in range(1024):
             # TODO / ?
             r = XOF(seed, (624*64)//8, D1)
             D1 += 1
             # TODO chunk size????
             for j in range(512):
                 # TODO / ?
                 sign = r[j]//(2^{(78-1)})
                 # TODO remove bits
                 val = r[j]
                 for k in range(78):
                     # TODO condition4
                     if condition4:
                         z[i+j] += 1
                 if sign == 1:
                     z[i+j] = -z[i+j]
```

```
i += c
return z
```

## 1.0.10 Enc

```
[10]: def Enc(cl):
          D = 0
          cnt = 0
          r = cSHAKE128(cl, 168, D)
          c = []
          pos_list = []
          sign_list = []
          for i in range(25):
             c.append(0)
              pos_list.append(0)
              sign_list.append(0)
          i = 0
          while i < 25:
              if cnt > 168 - 3:
                  D += 1
                  cnt = 0
                  r = cSHAKE128(cl, 168, D)
              pos = ((r[cnt] * (2^8)) + (r[cnt+1])) % 1024
              if c[pos] == 0:
                  if (r[cnt + 2] \% 2) == 1:
                      c[pos] = -1
                  else:
                      c[pos] = 1
                  pos_list[i] = pos
                  sign_list[i] = c[pos]
                  i += 1
              cnt += 3
          return pos_list, sign_list
```

## 1.0.11 ySampler

```
[11]: def ySampler(rand, counter):
          pos = 0
          nl = 1024
          D1 = D * (2^8)
          b = logb(q,2) / 8
          b = b.ceil()
          c = XOF(rand, b*n1, D1)
          i = 0
          y = []
          for i in range(1024):
              y[i] = 0
          while i < n:
              if pos >= nl:
                  D1 += 1
                  pos = 0
                  nl = 168//b
                  c = XOF(rand, 168, D1)
              x = logb(2^19 - 1,2)
              x = x.ceil()
              x = 2^(x + 1) - (2^19 - 1)
              x = c[pos] \% x
              y[i] = x
              if y[i] != (2^19):
                  i += 1
              pos += 1
          return y
```

## 1.0.12 H

```
[]: def H(v, m, t):
    w = []

    for i in range((4 * 1024) + 79):
        w.append(0)

    for i in range(1, 5):
        for j in range(n):
            val = v[i][j] % (2^22)
```

```
if val > (2^22) - 1:
    val = val - (2^22)

w[(i - 1)*n+j] = (v[i][j] - val)/(2^22)

w1 = G(m)
w2 = G(t)
w = w1 + w2
c1 = SHAKE(w, 32)

return cl
```

#### 1.0.13 checkE

```
[13]: def checkE(e):
    b = maxi(e[0])
    for i in range(1, k):
        b += maxi(e[i])

    if b > 554:
        return 1
    return 0
```

### 1.0.14 checkS

```
[15]: def checkS(s):
    b = maxi(s[0])
    for i in range(1, k):
        b += maxi(s[i])

    if b > 554:
        return 1
    return 0
```

## 1.0.15 maxi

Função para ser usada nos dois checks

```
[]: def maxi(e): return 0
```

## 1.0.16 XOF's

Provavelmente não é bem isto o que é pedido.

```
[]: def cSHAKE128(seed, x, D):
    digest = hashes.Hash(hashes.SHAKE128(int(x))
    digest.update(seed)
    return digest.finalize()

[33]: def XOF(seed, x, D1):
    digest = hashes.Hash(hashes.SHAKE128(int(x))
    digest.update(seed)
    return digest.finalize()
```