

We want to determine the odds of not capturing a single unit with regular impulses, assuming a 4 week banner.

First of all, note that we have 1 initial display and  $x$  display resets, where  $0 \leq x \leq 9$ . That's  $1 + x$  full display rolls. For those, we will need to first quantify the odds of getting no  $1^*$  on these display rolls. Let  $A(n)$  be the probability that you will get  $n$  of these displays with  $3^*$  and  $2^*$ s, with the rest being fully  $2^*$ , where  $0 \leq n \leq 1 + x$ . That would quantify as

$$A(n, x) = \binom{x+1}{n} \left( \frac{28}{100} \times \frac{27}{99} \times \frac{1}{98} \right)^n \left( \frac{28}{100} \times \frac{27}{99} \times \frac{26}{98} \right)^{x+1-n}$$

Then, for these rolls, we know that we will either try to capture the ringleader and fail if it is there, or capture a  $2^*$  and fail. Thus, the odds of failure on these  $x + 1$  captures are:

$$\begin{aligned} B(n, x) &= \binom{x+1}{n} \left( \frac{28}{100} \times \frac{27}{99} \times \frac{1}{98} \right)^n \left( \frac{28}{100} \times \frac{27}{99} \times \frac{26}{98} \right)^{x+1-n} \left( \frac{3}{4} \right)^n \left( \frac{1}{2} \right)^{x+1-n} \\ &= \binom{x+1}{n} \left( \frac{9}{15400} \right)^n \left( \frac{39}{3850} \right)^{x+1-n} \end{aligned}$$

Let's assume you start with 14 impulses and 0 extra impulses. You earn 55 impulses and 16 extra impulses throughout the banner. This totals up to 85 captures. Everytime you do a capture, you need to reroll. The final reroll does not matter in our probability calculation, so we need to take into account the 84 rerolls. We know that  $x$  rerolls are a  $2^*$ , which lead to resets, which gives probability

$$C(x) = \left( \frac{26}{98} \right)^x$$

Then, for the remaining  $85 - 1 - x = 84 - x$  captures not taken into account from the full display resets, we will have  $84 - x$  rerolls too. Let's suppose we have  $m$  ringleader appearances in these  $84 - x$  rerolls. Thus, the probability of failure here is

$$\begin{aligned} D(m, x) &= \binom{84-x}{m} \left( \frac{1}{98} \right)^m \left( \frac{26}{98} \right)^{84-x-m} \left( \frac{3}{4} \right)^m \left( \frac{1}{2} \right)^{84-x-m} \\ &= \binom{84-x}{m} \left( \frac{3}{392} \right)^m \left( \frac{13}{98} \right)^{84-x-m} \end{aligned}$$

Thus, the probability of failing to capture any unit across the entire banner is

$$\begin{aligned}
P(\text{fail}) &= \sum_{x=0}^9 \sum_{n=0}^{x+1} \sum_{m=0}^{84-x} B(n, x) C(x) D(m, x) \\
&= \sum_{x=0}^9 \sum_{n=0}^{x+1} \sum_{m=0}^{84-x} \binom{x+1}{n} \left(\frac{9}{15400}\right)^n \left(\frac{39}{3850}\right)^{x+1-n} \left(\frac{26}{98}\right)^x \binom{84-x}{m} \left(\frac{3}{392}\right)^m \left(\frac{13}{98}\right)^{84-x-m}
\end{aligned}$$

This is a lower bound, since the above sum assumes that the resets are in a fixed position in the sequence. It is hard to quantify the total amount of possible positions for the  $x$  resets, since there is a requirement that they have to at least 3 days apart, but we can upper bound this by assuming this requirement does not exist. This gives an additional  $\binom{84}{x}$  factor.

Thus, we have

$$\sum_{x=0}^9 \sum_{n=0}^{x+1} \sum_{m=0}^{84-x} B(n, x) C(x) D(m, x) \leq P(\text{fail}) \leq \sum_{x=0}^9 \sum_{n=0}^{x+1} \sum_{m=0}^{84-x} \binom{84}{x} B(n, x) C(x) D(m, x)$$