```
SetDirectory["D:\ToBeSaved\MathStudies\RiskEngine"];
 Get["A_Control.m"];
******** Low level Primitives ********
******* High level Instruments ********
******* Risk and Hedge Tools **************
 InitializeData[{usd, dem, frf}]
Ref.Cur.=Currency[usd]
File read :usd.zero 15 lines
File read :usd.index 31 lines
File read :dem.zero 15 lines
File read :dem.index 31 lines
File read :frf.zero 15 lines
File read :frf.index 31 lines
File read :PrimeRate 15 lines
File read :USTreasury 15 lines
File read :Gold.index 31 lines
File read :Oil.index 31 lines
Ref.Cur.=Currency[usd]
  1 dim for the exchange rate :1
+ 1 dim for the volatility of the exchange rate :1
+ 1 dim for the index :1
+ 1 dim for the volatility of the index :1
+ NbMaturities=16
+ NbVolatilities=3
= Total NbDimPerC=23
X NbCurrencies=3
= NbDim=69
Created Tables
Reading MATH_VOL
143 lines read
```

SD Currency Currency[usd] handled
SD Currency Currency[dem] handled
SD Currency Currency[frf] handled
SD rates and currencies handled

standard deviations OK

Reading MATH\_CORR
10296 lines read

 $1.08875 \times 10^6$ 

```
1000 lines handled
2000 lines handled
3000 lines handled
4000 lines handled
5000 lines handled
6000 lines handled
7000 lines handled
8000 lines handled
9000 lines handled
10000 lines handled
Correlations handled
Multiplying SD by correlations to get covariances
Covariances Computation Ended
Checking the definiteness of the covariance matrix
Computing the square root of the covariance matrix
 EvaluationDate = "6-Mar-98";
 EvaluationDate2 = "3/06/1998";
 inst = FxOption[buy, call, 100 mm, usd,
   TT["30-Mar-98"], currencybase → dem, strike → 1.5]
forward=1.4413 k=1.5
vo=0.0546863
Inst \lceil \text{Option} \lceil \text{Call} [1.5], 1.4413 \times 10^8,
  Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
  Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
   0.0657534, 0.], 0.0657534, 0, Currency[dem]
Value[inst]
```

```
NS1[inst]
```

```
-4.8401 × 10<sup>7</sup> S1 [Index [ExchangeRate [Currency [dem], Currency [usd]]]] -
 2.3288 × 10<sup>6</sup> S1[Index[Rate[0.0657534, Currency[dem]]]] +
 2.27969 \times 10^6 \text{ S1} [Index[Rate[0.0657534, Currency[usd]]]]} + 1.01817 \times 10^7
  S1[Volatility[Index[ExchangeRate[Currency[dem], Currency[usd]]], 0.0657534]] +
 1031.86 S1[Volatility[Index[Rate[0.0194444, Currency[dem]]], 0.0657534]] -
 1624.03 S1[Volatility[Index[Rate[0.0194444, Currency[usd]]], 0.0657534]] +
 399.195 S1[Volatility[Index[Rate[0.0833333, Currency[dem]]], 0.0657534]] -
 455.48 S1[Volatility[Index[Rate[0.0833333, Currency[usd]]], 0.0657534]] +
 3.69593 \times 10^6 \, S1S[Index[ExchangeRate[Currency[dem], Currency[usd]]], 2] +
 63824.7S1S[Index[Rate[0.0194444, Currency[dem]]], 2, 2] -
 63662.9 S1S [Index [Rate [0.0194444, Currency [usd]]], 2, 1] +
 31 966.6 S1S [Index [Rate [0.0833333, Currency [dem]]], 3, 2] -
 32002.1 S1S [Index [Rate [0.0833333, Currency [usd]]], 3, 1]
z = inst[1][4]
Volatility1[
 Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]], 0.0657534, 0.]
NS1[z]
0.227212 S1[Volatility[Index[ExchangeRate[Currency[dem], Currency[usd]]], 0.0657534]] +
 0.0000230267 S1[Volatility[Index[Rate[0.0194444, Currency[dem]]], 0.0657534]] -
 0.0000362414 S1[Volatility[Index[Rate[0.0194444, Currency[usd]]], 0.0657534]] +
 8.90832\times10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.08333333,\,Currency\,[dem]\,]\,]\,,\,0.0657534]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.08333333],\,Currency\,[dem]\,]\,]\,,\,0.0657534]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.0833333],\,Currency\,[dem]\,]\,]\,,\,0.0657534]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.0833333],\,Currency\,[dem]\,]\,]\,,\,0.0657534]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.083333]],\,Currency\,[dem]\,]\,]\,,\,0.0657534]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.08333]]]\,]\,-\,10^{-6}\,S1\,[Volatility\,[Index\,[Rate\,[0.0833]]]]\,]\,
 0.0000101643 S1[Volatility[Index[Rate[0.0833333, Currency[usd]]], 0.0657534]] +
  \textbf{0.0824772} \, \texttt{S1S} \, [\, \texttt{Index} \, [\, \texttt{ExchangeRate} \, [\, \texttt{Currency} \, [\, \texttt{dem}\,] \, \, , \, \, \texttt{Currency} \, [\, \texttt{usd} \, ] \, ] \, \, ] \, \, + \, \\
 0.00142429 S1S [Index [Rate [0.0194444, Currency [dem]]], 2, 2] -
 0.00142068 S1S[Index[Rate[0.0194444, Currency[usd]]], 2, 1] +
 0.000713356 S1S[Index[Rate[0.08333333, Currency[dem]]], 3, 2] -
 0.000714149 S1S[Index[Rate[0.0833333, Currency[usd]]], 3, 1]
NS1[z, 4/365.]
0.207415 S1[Volatility[Index[ExchangeRate[Currency[dem], Currency[usd]]], 0.0657534]] +
 0.0000210204 S1[Volatility[Index[Rate[0.0194444, Currency[dem]]], 0.0657534]] -
 0.0000330837 S1[Volatility[Index[Rate[0.0194444, Currency[usd]]], 0.0657534]] +
 8.13215 \times 10^{-6} \text{ S1}[Volatility[Index[Rate[0.08333333, Currency[dem]]], 0.0657534]]} -
 0.0752912 S1S [Index [ExchangeRate [Currency [dem], Currency [usd]]], 2] +
 0.00121491 S1S[Index[Rate[0.0194444, Currency[dem]]], 2, 2] -
 0.00121175 S1S[Index[Rate[0.0194444, Currency[usd]]], 2, 1] +
 0.000608417 S1S[Index[Rate[0.08333333, Currency[dem]]], 3, 2] -
 0.000608975 S1S[Index[Rate[0.0833333, Currency[usd]]], 3, 1]
NS1[z, 1.]
0
```

```
PS[inst, 3]
{Type, Value, Weight}
{{Exchange_Rate[dem,usd], -4.47051 \times 10^7, 2681.97},
 \{Volatility[ExchangeRate[usd,dem]], 2.61083 \times 10^6, 0.81344\},
 {Rate[usd, 0.0194444], 1.45159 \times 10<sup>6</sup>, 0.749835}}
 hedg = FxForward[100 mm, dem, TT["30-Sep-98"], soldcurrency → usd, rate → 1.43]
Seq[Inst[Fix[100000000, 0.569863, Currency[dem], 0]],
 Inst[Fix[-1.43 \times 10^8, 0.569863, Currency[usd], 0]]]
s1 = NS1[hedg]
9.77398 × 10<sup>7</sup> S1 [Index [ExchangeRate [Currency [dem], Currency [usd]]]] -
 3.89986 \times 10^7 S1[Index[Rate[0.569863, Currency[dem]]]] +
 8.0366 \times 10^7 \, S1[Index[Rate[0.569863, Currency[usd]]]]
MP[s1]
9.77398 × 10<sup>7</sup> S1S [Index [ExchangeRate [Currency [dem], Currency [usd]]], 2] -
 3.21436 \times 10^7 \text{ S1S}[Index[Rate[0.5, Currency[dem]]], 5, 2] +
 6.56813 \times 10^7 \text{ S1S}[Index[Rate[0.5, Currency[usd]]], 5, 1] -
 6.85496 \times 10^6 S1S [Index [Rate [1., Currency [dem]]], 6, 2] +
 1.46848 \times 10^7 \text{ S1S}[Index[Rate[1., Currency[usd]]], 6, 1]
s2 = NS2[hedg]
1.12417 × 10<sup>8</sup> S1 [Index [ExchangeRate [Currency [dem], Currency [usd]]]] ×
 S1[Index[Rate[0.569863, Currency[dem]]]] +
 2.24275 \times 10^7 \text{ S1} [Index[Rate[0.569863, Currency[dem]]]]}^2 -
 4.67079 \times 10^7 \text{ S1}[Index[Rate[0.569863, Currency[usd]]]}^2
cum = CM[inst]
\{1.24637 \times 10^{11}, 3.59892 \times 10^{16}, 1.39444 \times 10^{22}\}
CumulantComputation[6]
\{48743.7, 1.24637 \times 10^{11}, 3.59892 \times 10^{16}, 1.39444 \times 10^{22}, 6.77102 \times 10^{27}, 3.95046 \times 10^{33}\}
deltavector
0., -516.842, -16.3948, 0., -4.47051 \times 10^{7}, 2.61083 \times 10^{6}, 0., 0., 0., -1.48702 \times 10^{6},
 gammamatrix
```

```
0., 0., 0., -41.277, -1.30935, 0., -1.04995 \times 10^8, 208511., 0., 0., 0., -3.38296 \times 10^6,
0., 0., 0., -20.85, -0.661383, 0., -5.29695 \times 10^7, 105324., 0., 0., 0., -1.7067 \times 10^6,
```

```
0.,\,0.0580033,\,0.00367986,\,0.,\,257.99,\,-586.009,\,0.,\,0.,\,0.,\,86.1008,\,43.2027,\,0.,\,0.
0., 0., 0.00367986, 0.0000583645, 0., 8.18373, -18.5889, 0., 0., 0., 2.73121, 1.37044,
0., 0., 0., 0., 257.99, 8.18373, 0., 1.6254 \times 10^9, -1.30324 \times 10^6, 0., 0., 0., 1.09134 \times 10^8,
0., 0., -586.009, -18.5889, 0., -1.30324 \times 10^{6}, 0., 0., 0., 0., -434939., -218239.,
0., 0., 0., 86.1008, 2.73121, 0., 1.09134 \times 10^8, -434939., 0., 0., 0., 1.75827 \times 10^6,
0., 0., 0., 43.2027, 1.37044, 0., 5.47456 \times 10^7, -218239., 0., 0., 0., 1.76403 \times 10^6,
```

```
0., -0.0795161, -0.00252234, 0., -176.838, 401.677, 0., 0., 0., -59.0173, -29.613,
0., -0.00284855, -0.0000903592, 0., -6.33497, 14.3895, 0., 0., 0., -2.11421, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.06084, -1.0608
```

```
cum0 = CM[inst, 5]
\{1.24637 \times 10^{11}, 3.59892 \times 10^{16}, 1.39444 \times 10^{22}, 6.77102 \times 10^{27}\}
ratio = H1[inst, hedg]
0.453018
H2[inst, hedg]
0.452998
hedgedinst = MU[Seq[inst, ratio hedg]]
Seq[Inst[Option[Call[1.5], 1.4413 \times 10<sup>8</sup>,
 Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
 Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
  0.0657534, 0.], 0.0657534, 0, Currency [dem]],
Seq[Inst[Fix[4.53018 \times 10^7, 0.569863, Currency[dem], 0]],
 Inst[Fix[-6.47816 \times 10<sup>7</sup>, 0.569863, Currency[usd], 0]]]]
cum = CM[hedgedinst]
\{5.21463 \times 10^9, 9.30265 \times 10^{14}, 2.7244 \times 10^{20}\}
cum0[2] / cum[2]
38.687
R1 = NR[cum, 0.05]
118779.
R0 = NR[cum0, 0.05]
580699.
R0 / R1
4.88891
RQ1 = Timing[QR[cum, 0.05]]
{7.03 Second, 67620.6}
```

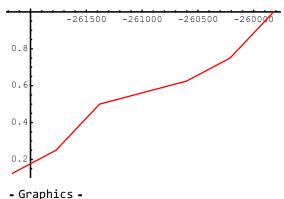
```
RQ0 = Timing[QR[cum0, 0.05]]
{14.34 Second, 486 384.}
RQ0[2] / R0
0.837583
RQ0[2] / RQ1[2]
7.19283
inst
(*----*)
SSValue[inst, Rate[dem] → +0.01] - Value[inst]
-513.076
SSValue[inst, ExchangeRate[dem] → +0.0001] - Value[inst]
SSValue[hedgedinst, ExchangeRate[dem] → +0.0001] - Value[hedgedinst]
-756.311
SSValue[inst,
                          RateAfter[usd, 1.5] \rightarrow +0.01,
                          RateBetween [dem, 0.001, 4] \rightarrow -0.01,
                          RateVolatilityBetween[dem, 1, 5] \rightarrow -0.05,
                          ExchangeRateVolatility[dem] → 0.1
        ]
\textbf{1.08926} \times \textbf{10}^6
SFValue[inst, 5 / 365.,
                          RateAfter[usd, 1.5] \rightarrow +0.01,
                          RateBetween [dem, 0.001, 4] \rightarrow -0.01,
                          RateVolatilityBetween[dem, 1, 5] \rightarrow -0.05,
                          ExchangeRateVolatility[dem] \rightarrow 0.1
        ]
828148.
```

```
SFNS1[inst, 5 / 365.,
                              RateAfter[usd, 1.5] \rightarrow +0.01,
                              RateBetween [dem, 0.001, 4] \rightarrow -0.01,
                              RateVolatilityBetween [dem, 1, 5] \rightarrow -0.05,
                              ExchangeRateVolatility[dem] → 0.1
          1
-4.2988 \times 10^7 \, S1 \, [Index \, [ExchangeRate \, [Currency \, [dem] \, , \, Currency \, [usd] \, ] \, ] \, ]
 7774.53 S1[Index[Rate[0.0136986, Currency[dem]]]] -
 2.05292 \times 10^6 \text{ S1}[Index[Rate[0.0657534, Currency[dem]]]]} +
 2.0156 \times 10^6 \text{ S1} [Index[Rate[0.0657534, Currency[usd]]]]} + 8.45515 \times 10^6
  S1[Volatility[Index[ExchangeRate[Currency[dem], Currency[usd]]], 0.0657534]] +
 856.884 S1[Volatility[Index[Rate[0.0194444, Currency[dem]]], 0.0657534]] -
 1348.64 S1[Volatility[Index[Rate[0.0194444, Currency[usd]]], 0.0657534]] +
 331.502 S1[Volatility[Index[Rate[0.0833333, Currency[dem]]], 0.0657534]] -
 378.242 S1[Volatility[Index[Rate[0.0833333, Currency[usd]]], 0.0657534]] +
 3.0692 × 10<sup>6</sup> S1S [Index [ExchangeRate [Currency [dem], Currency [usd]]], 2] +
 48 469. S1S [Index [Rate [0.0194444, Currency [dem]]], 2, 2] -
 48 341.8 S1S [Index [Rate [0.0194444, Currency [usd]]], 2, 1] +
 24 271.9 S1S [Index [Rate [0.0833333, Currency [dem]]], 3, 2] -
 24 292.6 S1S [Index [Rate [0.0833333, Currency [usd]]], 3, 1]
CM[inst]
\left\{1.24637 \times 10^{11}, 3.59892 \times 10^{16}, 1.39444 \times 10^{22}\right\}
cmf = SFCM[inst, 4, 5/365.,
                              RateAfter[usd, 1.5] \rightarrow +0.01,
                              RateBetween [dem, 0.001, 4] \rightarrow -0.01,
                              RateVolatilityBetween [dem, 1, 5] \rightarrow -0.05,
                              ExchangeRateVolatility [dem] → 0.1
\left\{1.00892 \times 10^{11}, \ 3.06338 \times 10^{16}, \ 1.25109 \times 10^{22}\right\}
NR[cmf, 0.05]
```

522462.

```
ScenarioSet1 = {
                 {RateAfter[usd, 1.5] \rightarrow +0.01,
                                 RateBetween [dem, 0.001, 4] \rightarrow -0.01,
                                 RateVolatilityBetween[dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] → 0.1},
           {RateAfter[usd, 1.5] \rightarrow +0.02,
                                 RateBetween [dem, 0.001, 4] \rightarrow -0.02,
                                 RateVolatilityBetween [dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] → 0.1},
           {RateAfter[usd, 1.5] \rightarrow +0.03,
                                 RateBetween [dem, 0.001, 4] \rightarrow -0.03,
                                 RateVolatilityBetween[dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] \rightarrow 0.1},
           {RateAfter[usd, 1.5] \rightarrow -0.01,
                                 RateBetween [dem, 0.001, 4] \rightarrow 0.01,
                                 RateVolatilityBetween [dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] → 0.1},
           {RateAfter[usd, 1.5] \rightarrow -0.02,
                                 RateBetween [dem, 0.001, 4] \rightarrow 0.02,
                                 RateVolatilityBetween[dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] \rightarrow 0.1},
           {RateAfter[usd, 1.5] \rightarrow -0.03,
                                 RateBetween [dem, 0.001, 4] \rightarrow 0.03,
                                 RateVolatilityBetween [dem, 1, 5] \rightarrow -0.05,
                                 ExchangeRateVolatility[dem] → 0.1}
     };
SSValue[inst, 5 / 365., ScenarioSet1]
{828148., 828538., 828928., 827369., 826979., 826589.}
fss = ScenarioD[inst, 5 / 365., ScenarioSet1,
  weightlist \rightarrow \{1/8, 1/8, 1/4, 1/4, 1/8, 1/8\}
\left\{\left\{-262\,161.,\,\frac{1}{8}\right\},\,\left\{-261\,771.,\,\frac{1}{4}\right\},\,\left\{-261\,381.,\,\frac{1}{2}\right\}\right\}
 \left\{-260601., \frac{5}{8}\right\}, \left\{-260211., \frac{3}{4}\right\}, \left\{-259821., 1\right\}\right\}
```

# ListPlot[fss, PlotStyle $\rightarrow$ RGBColor[1, 0, 0], PlotJoined $\rightarrow$ True]



### MCRisk[fss, 0.25]

261966.

(\* -----\*)

# fmc = MonteCarloD[hedgedinst, 1000];

simulation time :0.05 Second

200 simulations /1000 val= $-2.78298 \times 10^{7}$ 

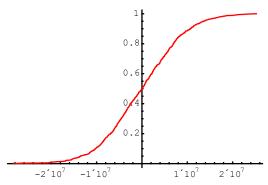
400 simulations /1000 val= $-2.55468 \times 10^7$ 

600 simulations /1000 val= $-3.01861\times10^7$ 

800 simulations /1000 val= $-2.52553 \times 10^7$ 

1000 simulations /1000 val= $-2.83646 \times 10^{7}$ 

### ListPlot[fmc, PlotStyle → RGBColor[1, 0, 0], PlotJoined → True]



- Graphics -

### MCRisk[fmc, 0.05]

 $1.35286 \times 10^{7}$ 

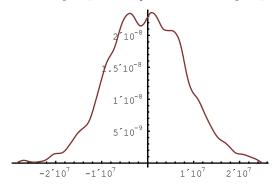
### MCCM[fmc, 4]

 $\left\{4.41516\times10^{-9},\,6.84503\times10^{13},\,1.66544\times10^{19},\,2.19987\times10^{26}\right\}$ 

ds = MCSample[fmc, 200];

# ds3 = MCSampleDerive[ds, 1000];

ListPlot[ds3, PlotStyle → RGBColor[0.5, 0.2, 0.2], PlotJoined → True]



- Graphics -

```
(* -----Credit
  Risk Computation ----- *)
 X2 = Bond[buy, 25 mm, usd, TT["15-May-07"], coupon \rightarrow 0.065, bondprice \rightarrow 97.6]
Seq[Inst[Fix[311644., 0.191781, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 1.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 2.19178, Currency[usd], 0.00352586]],
 Inst [Fix[1.625 \times 10^6, 3.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 4.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 5.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 6.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 7.19178, Currency[usd], 0.00352586]],
 Inst[Fix[1.625 \times 10^6, 8.19178, Currency[usd], 0.00352586]],
 Inst[Fix[2.6625 \times 10^7, 9.19178, Currency[usd], 0.00352586]]]
EXP0[X2, 1]
2.2527 \times 10^7
EXPO[X2, 2]
2.30166 \times 10^7
 X3 = Swap[receivefloat, 125 mm, usd,
     TT["31-Dec-05"], fixed \rightarrow 0.074, reset \rightarrow 0.07, frequency \rightarrow 0.5];
Value[X3]
-6.5543 \times 10^6
FindRoot[Value[Swap[receivefloat, 125 mm, usd, TT["31-Dec-05"],
     fixed \rightarrow fff, reset \rightarrow 0.07, frequency \rightarrow 0.5]] == 0, {fff, 0.05}]
\{\texttt{fff} \rightarrow \texttt{0.065142}\}
 X3 = Swap[receivefloat, 125 mm, usd,
     TT["31-Dec-05"], fixed \rightarrow 0.0674014, reset \rightarrow 0.07, frequency \rightarrow 0.5];
Value[X3]
-1.67179 \times 10^6
```

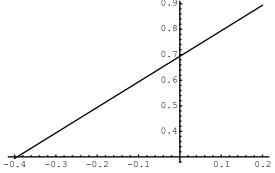
(\*----\*)

```
Plot[EXPO[X3, t], {t, 0.01, 10}]
6'10<sup>6</sup>
4'106
2′10<sup>6</sup>
- Graphics -
(* -----*)
bb = Bond[buy, 125 mm, dem, TT["20-May-01"], coupon → 0.06375]
Seq[Inst[Fix[1.63741\times10<sup>6</sup>, 0.205479, Currency[dem], 0]],
 Inst[Fix[7.96875 \times 10<sup>6</sup>, 1.20548, Currency[dem], 0]],
 Inst[Fix[7.96875 \times 10<sup>6</sup>, 2.20548, Currency[dem], 0]],
 Inst[Fix[1.32969 \times 10^8, 3.20548, Currency[dem], 0]]]
 X27 = EuropeanBondOption[buy, 10, call, usd, bb, 0.3, strike → 1.01];
Value[X27]
3.54342 \times 10^7
 X27 = EuropeanBondOption[buy, 10, call, usd, bb, 0.3, strike \rightarrow 1.01, cumulants \rightarrow 4];
v00 = Value[X27]
3.54199 \times 10^7
debugflag = 1;
Value[X27]
True Cumulants=\{1.0123 \times 10^{14}, 2.21974 \times 10^{14}, 3.00985 \times 10^{22}\}
Forward Value = 8.82165 \times 10^7 Total Forward Volatility = 0.11405
LN Cumulants=\{1.01226\times10^{14}, 3.49976\times10^{20}, 2.1587\times10^{27}\}
Final coeffs=\{3.24555 \times 10^9, -3.49976 \times 10^{20}, -2.15867 \times 10^{27}\}
LN Density Derivatives= \left\{2.15055\times10^{-8}\text{, }-3.33323\times10^{-16}\text{, }-5.39771\times10^{-23}\right\}
adjustement=-14300.4
3.54199 \times 10^7
(*----- find a volatility spread due to the non linearity -----*)
X27 = EuropeanBondOption[buy, 10, call, usd, bb, 0.3, strike \rightarrow 1.01, cumulants \rightarrow 4];
v00 = Value[X27]
```

```
True Cumulants=\{1.0123 \times 10^{14}, 2.21974 \times 10^{14}, 3.00985 \times 10^{22}\}
Forward Value = 8.82165 \times 10^7 Total Forward Volatility = 0.11405
LN Cumulants=\{1.01226 \times 10^{14}, 3.49976 \times 10^{20}, 2.1587 \times 10^{27}\}
Final coeffs=\{3.24555\times10^9, -3.49976\times10^{20}, -2.15867\times10^{27}\}
LN Density Derivatives=\{2.15055 \times 10^{-8}, -3.33323 \times 10^{-16}, -5.39771 \times 10^{-23}\}
adjustement=-14300.4
3.54199 \times 10^7
FindRoot[Value[EuropeanBondOption[buy, 10, call, usd, bb, 0.3,
     strike \rightarrow 1.01, volatilityspread \rightarrow spx] == v00, {spx, 0.00001, 0.00005}]
\{ spx \rightarrow -0.0000413695 \}
Value[EuropeanBondOption[buy, 10, call, usd,
  bb, 0.3, strike \rightarrow 1.01, volatilityspread \rightarrow -0.00004136]]
3.54199 \times 10^7
debugflag = 0;
Value[X27]
3.54199 \times 10^7
(*---- effect of non linearity on a
 highly non linear option -----Exemple 1 *)
 inst = FxOption buy, call, 95 mm, usd,
    TT["30-Mar-98"], currencybase \rightarrow dem, strike \rightarrow \frac{1}{1}
forward=1.444 k=0.666667
vo=0.0548063
Inst [Option [Call [0.666667], 1.3718 \times 10^8,
  Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
  Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
    0.0657534, 0.], 0.0657534, 0, Currency[dem]]
v1 = Value[inst, TT["15-Mar-98"]]
7.37254 \times 10^7
(*---- effect of non linearity on a
 highly non linear option -----Exemple 2 *)
```

```
xi = EuropeanOption[buy, Call, 100 mm, usd, inst, TT["15-Mar-98"], strike → 1.01]
v0=2.71332\times10^{-93} f=-3.66455×10<sup>98</sup> k=-3.7012×10<sup>98</sup>
Inst [Option [Call [-3.7012 \times 10^{98}], -2.72885 \times 10^{-91}]
  Index[FutVal[0.0246575, Currency[usd], Inst[Option[Call[0.666667],
       1.3718 × 10<sup>8</sup>, Index [ExchangeRate [0.0657534, Currency [usd], Currency [dem]]],
       Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
        0.0657534, 0.], 0.0657534, 0, Currency [dem] | | | |,
  Volatility1 Index FutVal 0.0246575, Currency [usd], Inst Option Call 0.666667],
        1.3718 × 10<sup>8</sup>, Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
        Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
         0.0657534, 0.], 0.0657534, 0, Currency[dem]]]],
   0.0246575, 0.], 0.0246575, 2, Currency[usd]]
Value[xi]
1.63662317 \times 10^{1802} + 1.34334146 \times 10^{1802} \text{ I}
xi1 = EuropeanOption[buy, Call, 100 mm,
  usd, inst, TT["15-Mar-98"], strike \rightarrow 1.01, cumulants \rightarrow 5]
v0=0.0393215 f=9.17389\times10^{98} k=9.26563\times10^{98}
Inst [Option [Call [9.26563 \times 10^{98}], 1.09005 \times 10^{-91}]
  Index[FutVal[0.0246575, Currency[usd], Inst[Option[Call[0.666667],
       1.3718 × 10<sup>8</sup>, Index [ExchangeRate [0.0657534, Currency [usd], Currency [dem]]],
       Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
        0.0657534, 0.], 0.0657534, 0, Currency[dem]]]],
  Volatility1 [Index FutVal [0.0246575, Currency [usd], Inst [Option [Call [0.666667],
        1.3718 \times 10^8, Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
        Volatility1[Index[ExchangeRate[0.0657534, Currency[usd], Currency[dem]]],
         0.0657534, 0.], 0.0657534, 0, Currency[dem]]]],
   0.0246575, 0.], 0.0246575, 5, Currency[usd]]]
Value[xi1]
-\,4.85891\times 10^{95}
Sqrt[CM1[inst, TT["15-Mar-98"]][1] x TT["15-Mar-98"] / ProvidedStatisticalTime] /
 Value[inst, TT["15-Mar-98"]]
0.13928
Value[Index[ExchangeRate[1, Currency[dem], Currency[usd]]]]
0.692411
```

```
Plot[SSValue[Index[ExchangeRate[Currency[dem], Currency[usd]]],
  ExchangeRate[dem] \rightarrow xx], {xx, -0.4, 0.2}]
```



- Graphics -

insta = FxOption[buy, call, 100 mm, dem, 1., currencybase → usd, strike → 0.7]

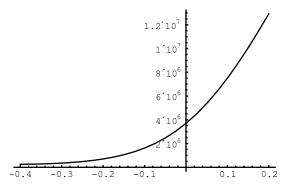
forward=0.693818 k=0.7

vo=0.215092

Inst

Option  $[Call[0.7], 6.93818 \times 10^7, Index[ExchangeRate[1., Currency[dem], Currency[usd]]],$ Volatility1[Index[ExchangeRate[1., Currency[dem], Currency[usd]]], 1., 0.], 1., 0, Currency[usd]

### Plot[SSValue[insta, ExchangeRate[dem] $\rightarrow$ xx], {xx, -0.4, 0.2}]



- Graphics -

hedg = FxForward[45 mm, dem, TT["30-Sep-98"], soldcurrency  $\rightarrow$  usd, rate  $\rightarrow$  1.43]; ratio = H1[insta, hedg]

-0.648989

```
hedgedinsta = MU[Seq[insta, ratio hedg]]
```

```
Seq[Inst[Option[Call[0.7], 6.93818 \times 10^7,
   Index[ExchangeRate[1., Currency[dem], Currency[usd]]],
   Volatility1[Index[ExchangeRate[1., Currency[dem], Currency[usd]]], 1., 0.], 1.,
   0, Currency[usd]], Seq[Inst[Fix[-2.92045 \times 10^7, 0.569863, Currency[dem], 0]],
  Inst[Fix[4.17624 \times 10^7, 0.569863, Currency[usd], 0]]]
```

### Plot[SSValue[hedgedinsta, ExchangeRate[dem] $\rightarrow$ xx] - Value[hedgedinsta], {xx, -0.4, 0.2}]

```
6'10
                                     4′10<sup>6</sup>
                                     2′10
                     -0.2
- Graphics -
```

```
(*---- Use of pseudo-
 sensitivities for hedging barrier options -----*)
instb = FxBarrierOption[buy, call, upandout,
  100 mm, dem, .1, currencybase \rightarrow usd, strike \rightarrow 0.7, barrier \rightarrow 10.9]
forward=0.693818 \text{ k}=0.7 \text{ b}=10.9
vo=0.0674585
Inst [Option | BarrierCall [1, 1, 0.7, 10.9], 1.4413 \times 10^8,
  Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]],
  Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.],
  0.1, Currency[usd]
```

### NS1a[instb]

forward=0.693818 k=0.7

```
-226743. S1[Index[Rate[0, 0.1, Currency[usd]]]] + 6.60658 \times 10<sup>7</sup>
  S1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0] + 1.24824 \times 10^{7}
  S1[Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.], 0]
```

#### insta = FxOption[buy, call, 100 mm, dem, .1, currencybase → usd, strike → 0.7]

```
vo=0.0674585
Inst [Option[Call[0.7], 6.93818 \times 10^7,
  Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]],
  Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.],
  0.1, 0, Currency [usd] ]
```

#### Value[insta]

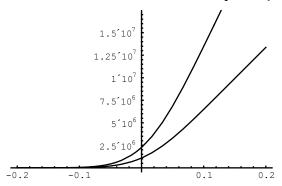
 $1.09141 \times 10^6$ 

#### NS1a[insta]

```
-109141. S1 [Index [Rate [0, 0.1, Currency [usd]]]] + 3.18028 \times 10<sup>7</sup>
  S1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0] + 1.90016 \times 10<sup>7</sup>
  S1[Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.], 0]
```

### Plot[{ SSValue[instb, ExchangeRate[dem] $\rightarrow xx$ ],

SSValue[insta, ExchangeRate[dem]  $\rightarrow$  xx]}, {xx, -0.2, 0.2}]



- Graphics -

hedg = FxForward[45 mm, dem, TT["30-Sep-98"], soldcurrency → usd, rate → 1.43];

ratiob = H1[instb, hedg]

-1.46092

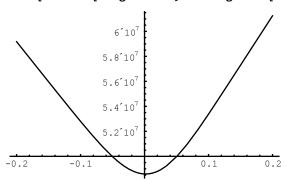
ratioa = H1[insta, hedg]

-0.675118

### hedgedinstb = MU[Seq[instb , ratiob hedg]]

```
Seq[Inst[Option[BarrierCall[1, 1, 0.7, 10.9],
   1.4413 × 10<sup>8</sup>, Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]],
   Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.],
   0.1, Currency [usd]], Seq[Inst[Fix[-6.57416 \times 10^7, 0.569863, Currency[dem], 0]],
  Inst[Fix[9.40105 \times 10<sup>7</sup>, 0.569863, Currency[usd], 0]]]]
```

# Plot[SSValue[hedgedinstb, ExchangeRate[dem] $\rightarrow$ xx], {xx, -0.2, 0.2}]



- Graphics -

### NS1a[instb]

```
-226743. S1[Index[Rate[0, 0.1, Currency[usd]]]] + 6.60658 \times 10<sup>7</sup>
  S1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0] + 1.24824 \times 10<sup>7</sup>
  S1[Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.], 0]
```

ratiob = H1[instb, hedg]

-1.46092

```
(* If we enlarge the horizon for meta sensitivities *)
MetaSensitivityFactor = 0.99;
NS1a[instb]
-405740. S1[Index[Rate[0, 0.1, Currency[usd]]]] + 6.86481 \times 10<sup>7</sup>
  S1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0] -6.59745 \times 10^{77}
  S1[Volatility1[Index[ExchangeRate[0.1, Currency[dem], Currency[usd]]], 0.1, 0.], 0]
ratiob = H1[instb, hedg]
-1.43053 \times 10^{69}
hedgedinstb = MU[Seq[instb, ratiob hedg]];
Value[Volatility[Index[ExchangeRate[Currency[usd], Currency[dem]]], 1], 0]
0.214134
StDeviation[index_, tm_, tf_] := Value[Volatility[index, tm], tf] * Value[index, tf]
sdfx = StDeviation[Index[ExchangeRate[Currency[usd], Currency[dem]]], 1, 0]
0.308631
Plot[SSValue[hedgedinstb, ExchangeRate[dem] \rightarrow xx], {xx, -sdfx, sdfx}]
                 4'10<sup>76</sup>
- Graphics -
(* -----*)
bb = Bond[buy, 125 mm, dem, TT["20-May-01"], coupon → 0.06375]
Seq[Inst[Fix[1.63741 \times 10<sup>6</sup>, 0.205479, Currency[dem], 0]],
 Inst \left[\operatorname{Fix}\left[7.96875 \times 10^{6}, 1.20548, \operatorname{Currency}\left[\operatorname{dem}\right], 0\right]\right],
 Inst[Fix[7.96875 \times 10<sup>6</sup>, 2.20548, Currency[dem], 0]],
 Inst[Fix[1.32969 \times 10<sup>8</sup>, 3.20548, Currency[dem], 0]]]
Value[EuropeanOption[buy, Call, 100\,mm, usd, bb, TT["15-Oct-98"], strike \rightarrow 1.01]]
v0=0.162701 f=8.97159\times10^7 k=9.06131\times10^7
5.81506 \times 10^6
Value[BarrierOption[buy, call, upandout, 100 mm,
  usd, bb, TT["15-Oct-98"], strike \rightarrow 1.01, barrier \rightarrow 1.2]]
```

```
vo=0.162701
forward=8.97159\times10<sup>7</sup> k=9.06131\times10<sup>7</sup> b=1.07659\times10<sup>8</sup>
\textbf{1.48487} \times \textbf{10}^{6}
xinst = BarrierOption[buy, call, upandout,
     100 mm, usd, bb, TT["15-Oct-98"], strike \rightarrow 1.01, barrier \rightarrow 1.2];
vo=0.162701
forward=8.97159 \times 10^7 \text{ k}=9.06131 \times 10^7 \text{ b}=1.07659 \times 10^8
xhedg = BarrierOption[buy, call, upandout,
     100 mm, usd, bb, TT["15-Oct-98"], strike \rightarrow 1.01, barrier \rightarrow 1.2];
vo=0.162701
forward=8.97159\times10<sup>7</sup> k=9.06131\times10<sup>7</sup> b=1.07659\times10<sup>8</sup>
xratio = H1[xinst, xhedg]
-1.
```