

R E V I E W

A row of six light-colored wooden blocks, each with a black letter, spelling out the word "REVIEW". The blocks are arranged horizontally on a dark wooden surface. In the background, several other wooden blocks are visible, some with letters like 'M', 'I', 'E', 'N', '7', and 'C'. In the foreground, there are more wooden blocks, some of which are out of focus, including one with the letter 'I' and another with the number '2'.

Overview

Review of ggplot

Quick review of material covered in the class so far

Questions to prepare for the exam

Announcements

Midterm exam is on Thursday

- Bring a pen and a pencil
- One page (double-sided) with code and equations only!
 - You will turn in this page of notes with your exam (put your name on it)
 - Recommend including equations for SEs, etc.

Office hours this week

- No TA office hours this week since there is no homework

Review of the grammar of graphics and ggplot

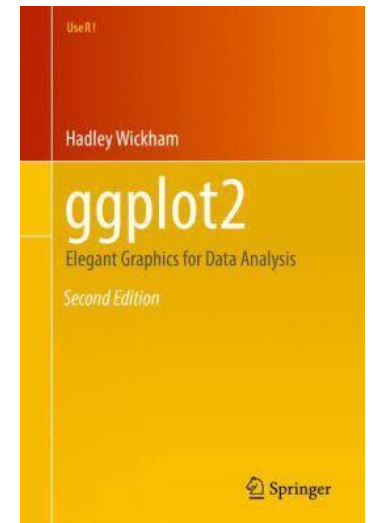
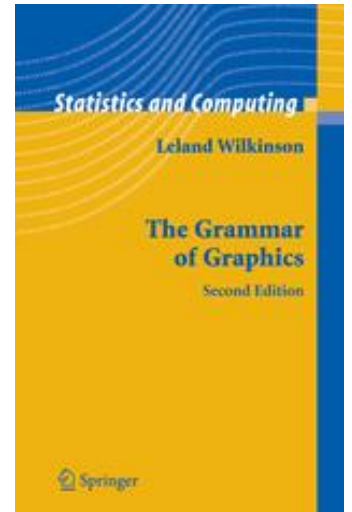


The grammar of graphics

Leland Wilkinson noticed similarities between many graphs and tried to generate a ‘grammar’ that could be used to express a graph

- i.e., a list elements that can be combined together to create a graph

Hadley Wickham implemented these ideas in R in the ggplot2 package



Graphs are composed of...

A Frame: Coordinate system on which data is placed

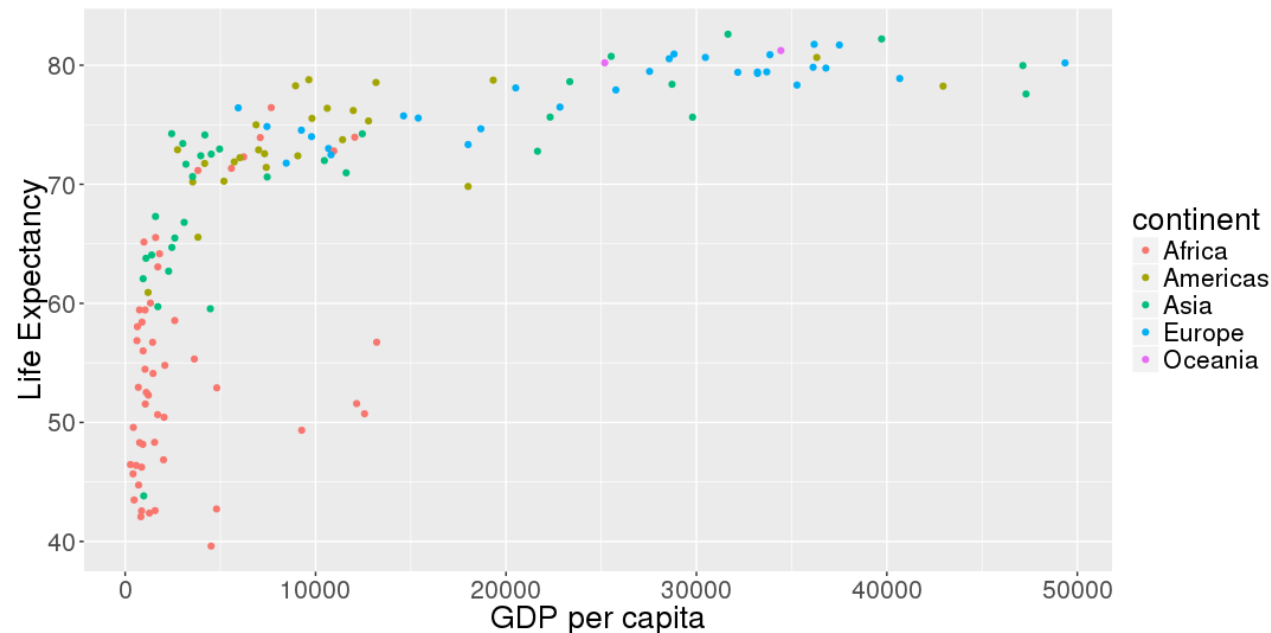
- `ggplot()` +

Glyphs: basic graphic unit representing cases or statistics

- Data is **mapped** onto these aesthetics such as: shape, color, size, etc. and/or aesthetics can be set to a fixed value
 - `geom_point(aes(x = gdpPercap, y = lifeExp, color = continent))` `geom_point(aes(x = gdpPercap, y = lifeExp), color = "red")`

Scales and guides: shows how to interpret axes and other properties of the glyphs

- `scale_x_continuous(trans = "log10")` `scale_color_brewer(type = "qua", palette = 2)`



Plots can also contain...

Facets: allows for multiple side-by-side graphs based on a categorical variable

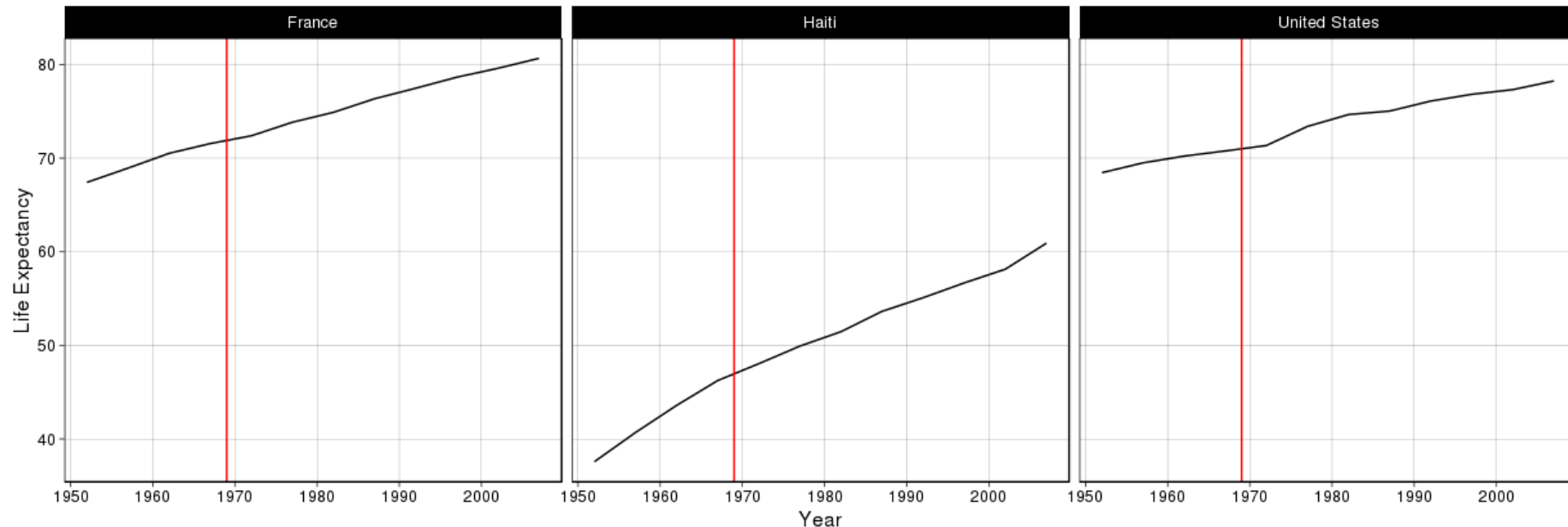
- `facet_wrap(~country)`

Layers: allows for more than one types of data to be mapped onto the same figure

- `geom_vline(xintercept = 1969, col = "red")`

Theme: contains finer points of display (e.g., font size, background color, etc.)

- `theme_wsj()`



Questions?

ggplot2 cheat sheet

Data visualization with ggplot2 :: CHEAT SHEET



Basics

ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same components: a **data** set, a **coordinate system**, and **geoms**—visual marks that represent data points.



To display values, map variables in the data to visual properties of the geom (**aesthetics**) like **size**, **color**, and **x** and **y** locations.



Complete the template below to build a graph.

```
ggplot(data = <DATA>) +  
  <GEOM_FUNCTION>(mapping = aes(<MAPPINGS>),  
    stat = <STAT>, position = <POSITION>) +  
  <COORDINATE_FUNCTION> +  
  <SCALE_FUNCTION> +  
  <THEME_FUNCTION>
```

required

Not required, sensible defaults supplied

ggplot(data = mpg, aes(x = cty, y = hwy)) Begins a plot that you finish by adding layers to. Add one geom function per layer.

last_plot() Returns the last plot.

ggsave("plot.png", width = 5, height = 5) Saves last plot as 5" x 5" file named "plot.png" in working directory. Matches file type to file extension.

Aes

Common aesthetic values.

color and **fill** - string ("red", "#RRGGBB")

linetype - integer or string (0 = "blank", 1 = "solid", 2 = "dashed", 3 = "dotted", 4 = "dotdash", 5 = "longdash", 6 = "twodash")

lineend - string ("round", "butt", or "square")

linejoin - string ("round", "mitre", or "bevel")

size - integer (line width in mm)

shape - integer/shape name or a single character ("a")

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Geoms

Use a geom function to represent data points, use the geom's aesthetic properties to represent variables. Each function returns a layer.

GRAPHICAL PRIMITIVES

a <- ggplot(economics, aes(date, unemployment))

b <- ggplot(seals, aes(x = long, y = lat))

a + geom_blank() and **a + expand_limits()**
Ensure limits include values across all plots.

b + geom_curve(aes(yend = lat + 1, xend = long + 1), curvature = 1) - x, yend, y, yend, alpha, angle, color, curvature, linetype, size

a + geom_path(lineend = "butt", linejoin = "round", linemitre = 1) - x, y, alpha, color, group, linetype, size

a + geom_polygon(aes(alpha = 50)) - x, y, alpha, color, fill, group, subgroup, linetype, size

b + geom_rect(aes(xmin = long, ymin = lat, xmax = long + 1, ymax = lat + 1)) - xmax, xmin, ymax, ymin, alpha, color, fill, linetype, size

a + geom_ribbon(aes(ymin = unemployment - 900, ymax = unemployment + 900)) - x, ymax, ymin, alpha, color, fill, group, linetype, size

LINE SEGMENTS

common aesthetics: x, y, alpha, color, linetype, size

b + geom_abline(aes(intercept = 0, slope = 1))

b + geom_hline(aes(yintercept = lat))

b + geom_vline(aes(xintercept = long))

b + geom_segment(aes(yend = lat + 1, xend = long + 1))

b + geom_spoke(aes(angle = 1:1155, radius = 1))

ONE VARIABLE continuous

c <- ggplot(mpg, aes(hwy)); **c2** <- ggplot(mpg)

c + geom_area(stat = "bin") - x, y, alpha, color, fill, linetype, size

c + geom_density(kernel = "gaussian") - x, y, alpha, color, fill, group, linetype, size, weight

c + geom_dotplot() - x, y, alpha, color, fill

c + geom_freqpoly() - x, y, alpha, color, group, linetype, size

c + geom_histogram(binwidth = 5) - x, y, alpha, color, fill, linetype, size, weight

c2 + geom_qq(aes(sample = hwy)) - x, y, alpha, color, fill, linetype, size, weight

c + geom_raster(aes(fill = z), hjust = 0.5, vjust = 0.5, interpolate = FALSE) - x, y, alpha, fill

c + geom_tile(aes(fill = z)) - x, y, alpha, color, fill, linetype, size, width

c + geom_violin(scale = "area") - x, y, alpha, color, fill, group, linetype, size, weight

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c + geom_violin(scale = "area") - x, y, alpha, color, fill, group, linetype, size, weight

TWO VARIABLES both continuous

e <- ggplot(mpg, aes(cty, hwy))

e + geom_label(aes(label = cty), nudge_x = 1, nudge_y = 1) - x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust

e + geom_point() - x, y, alpha, color, fill, shape, size, stroke

e + geom_quantile() - x, y, alpha, color, group, linetype, size, weight

e + geom_rug(sides = "bl") - x, y, alpha, color, linetype, size

e + geom_smooth(method = lm) - x, y, alpha, color, fill, group, linetype, size, weight

e + geom_text(aes(label = cty), nudge_x = 1, nudge_y = 1) - x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust

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continuous bivariate distribution

h <- ggplot(diamonds, aes(carat, price))

h + geom_bin2d(binwidth = c(0.25, 500)) - x, y, alpha, color, fill, linetype, size, weight

h + geom_density_2d() - x, y, alpha, color, group, linetype, size

h + geom_hex() - x, y, alpha, color, fill, size

continuous function

i <- ggplot(economics, aes(date, unemployment))

i + geom_area() - x, y, alpha, color, fill, linetype, size

i + geom_line() - x, y, alpha, color, group, linetype, size

i + geom_step(direction = "hv") - x, y, alpha, color, group, linetype, size

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i + geom_step(direction = "hv") - x, y, alpha, color, group, linetype, size

i + geom_step(direction = "hv") - x, y, alpha, color, group, linetype, size

i + geom_step(direction = "hv") - x, y, alpha



What we have covered so far...

			<u>Analysis</u>	<u>R</u>
1	Aug 29	Course overview, introduction to R, descriptive statistics		Base R
2	Sep 3-6	Review of central statistical concepts and exploratory analysis using R		
3	Sep 10-12	Confidence Intervals and the bootstrap	Resampling and parametric methods	
4	Sep 17-19	Review of hypothesis tests and permutation tests in R		Data wrangling visualization
5	Sep 24-26	Parametric tests and theories of hypothesis testing		
6	Oct 1-3	Data manipulation and visualization		
7	Oct 8-10	Review and midterm exam		
8	Oct 15-17	Functions, misc, and October break		

What we have covered so far...

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|---|---------|--|
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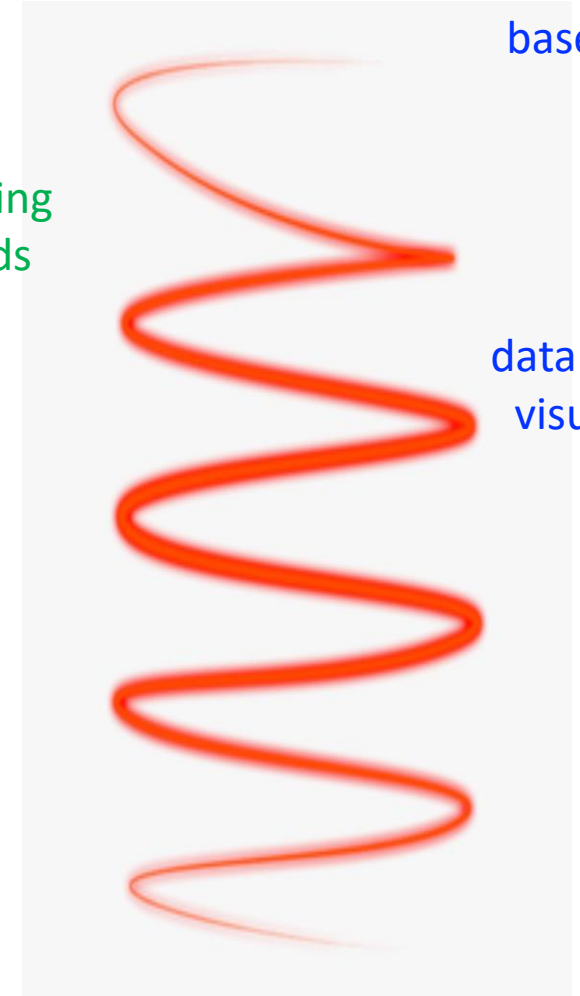
Analysis

R

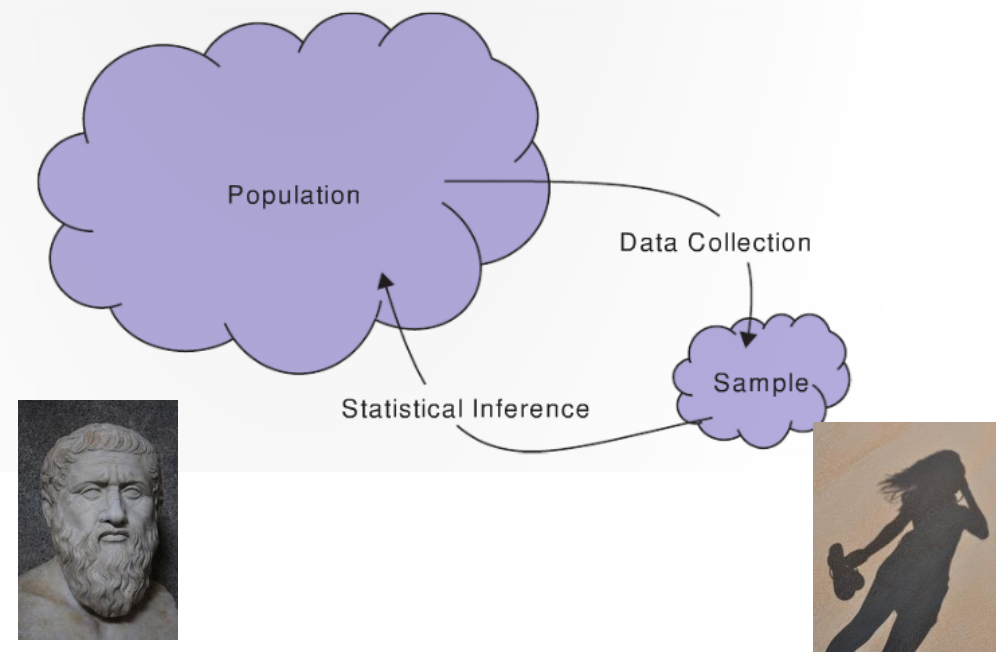
resampling
methods

base R

data wrangling
visualization



Parameters and statistics commonly used symbols



$$\bar{x} = \frac{\sum_i^n x_i}{n}$$

	Population parameter (Plato)	Sample statistic (shadow)
Mean	μ	\bar{x}
Standard deviation	σ	s
Proportion	π	\hat{p}
Correlation	ρ	r
Regression slope	β	b

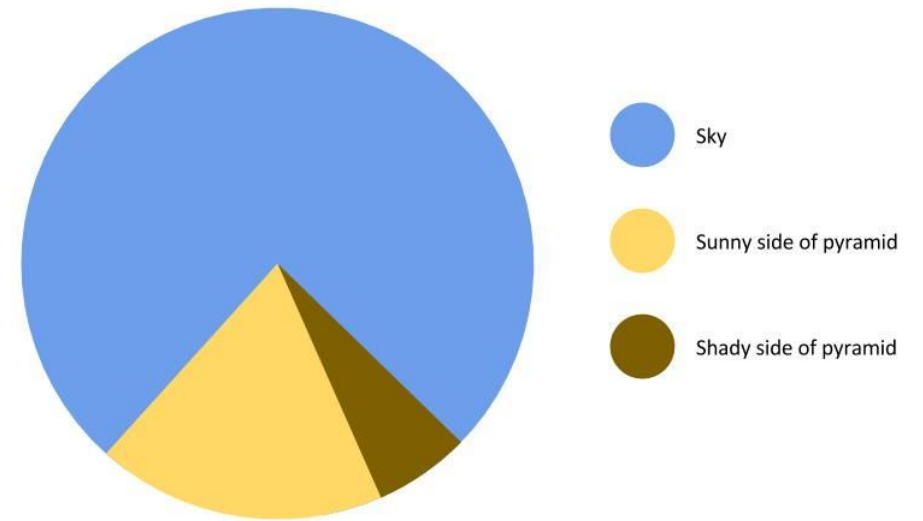
Base R

Basics of R

```
> my_vec <- c(5, 28, 19)
> inds_less_than_10 <- my_vec < 10
```

How to plot data in base R

```
> drinks_table <- table(profiles$drinks)
> barplot(drinks_table)
> pie(drinks_table)
> hist(profiles$height)
```



For loops

```
my_results <- NULL
for (i in 1:100) {
  my_results[i] <- i^2
}
```


What we have covered so far...

- | | | |
|---|-----------|---|
| 3 | Sep 10-12 | Confidence Intervals and the bootstrap |
| 4 | Sep 17-19 | Review of hypothesis tests and permutation tests in R |
| 5 | Sep 24-26 | Parametric, non-parametric and theories of hypothesis testing |

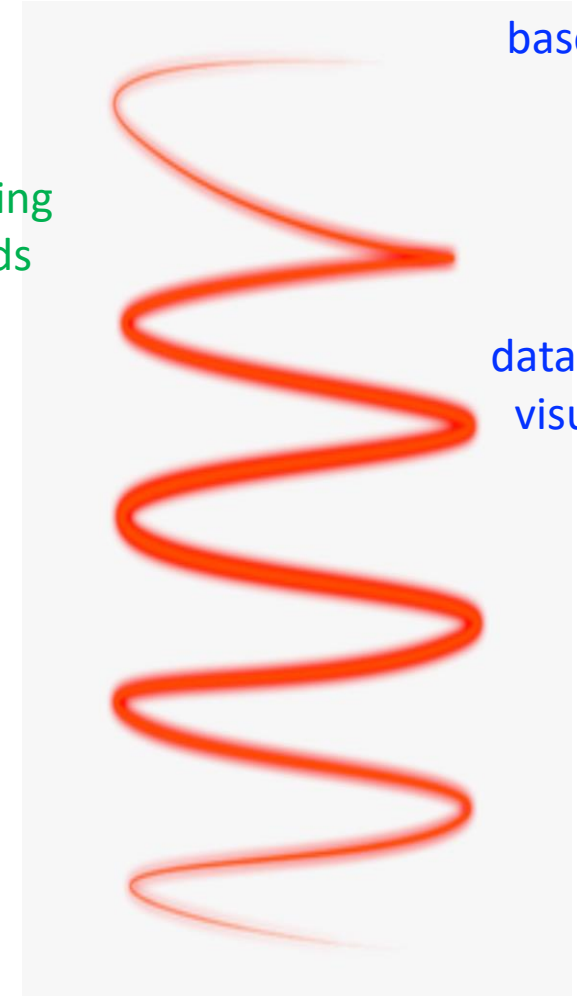
Analysis

R

resampling
methods

base R

data wrangling
visualization

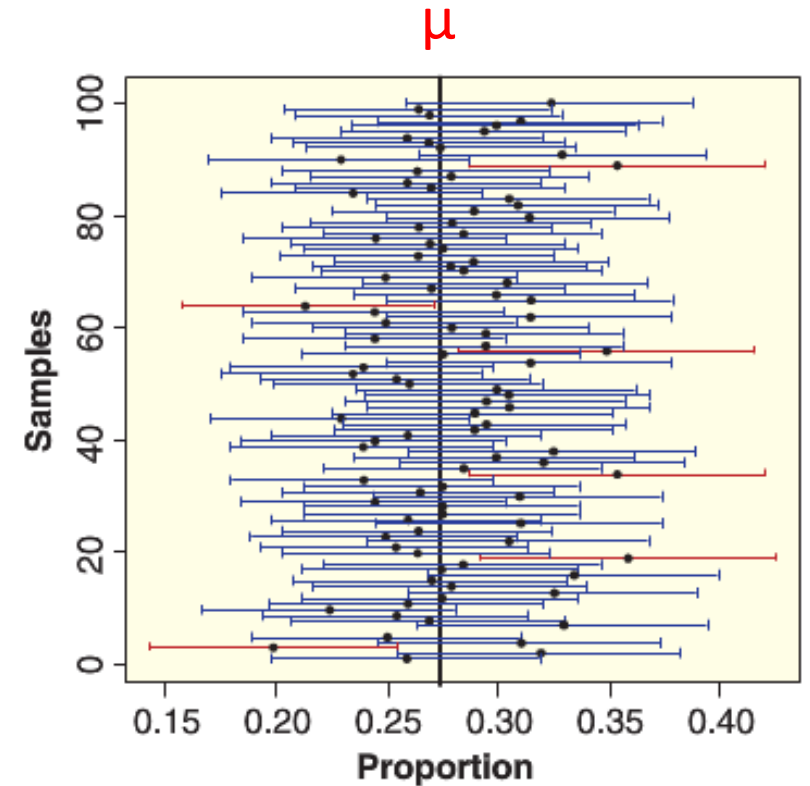
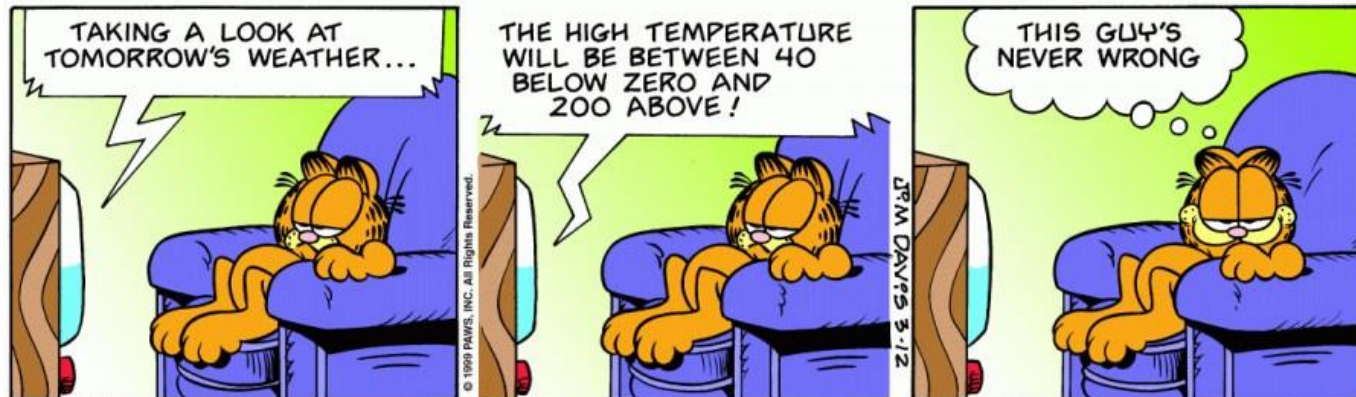


Probability and confidence intervals

Probability functions; e.g., `rnorm`, `pnorm`, `dnorm`, `qnorm`

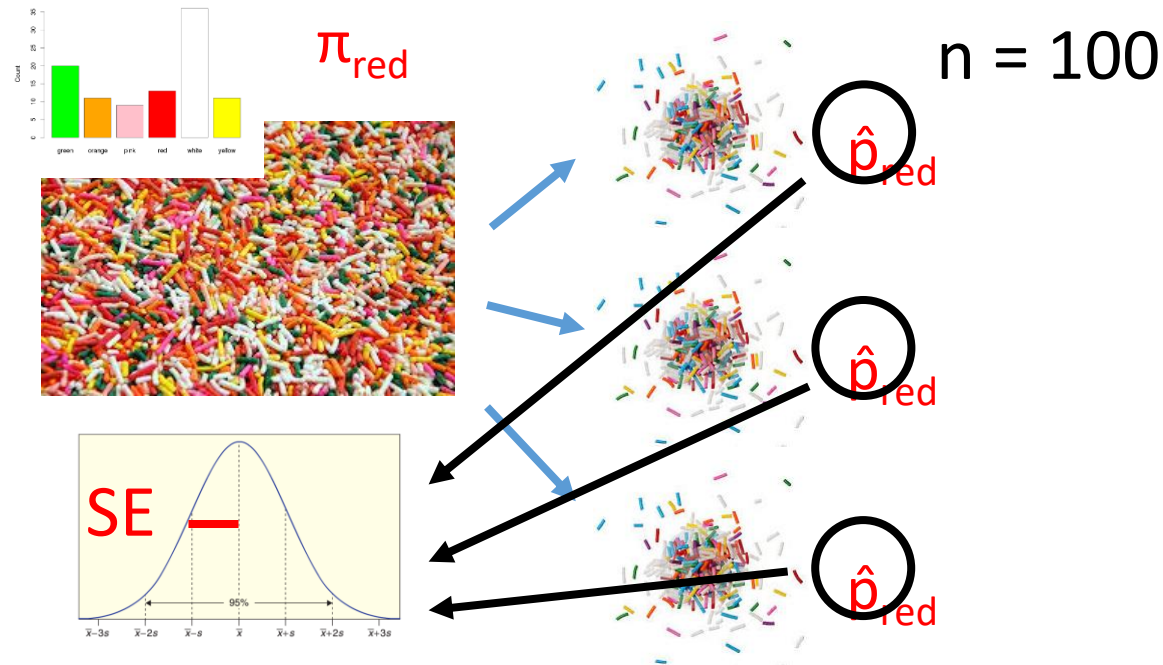
Confidence intervals:

$$CI_{95} = \text{stat} \pm 2 \cdot SE$$



Sampling and bootstrap distributions

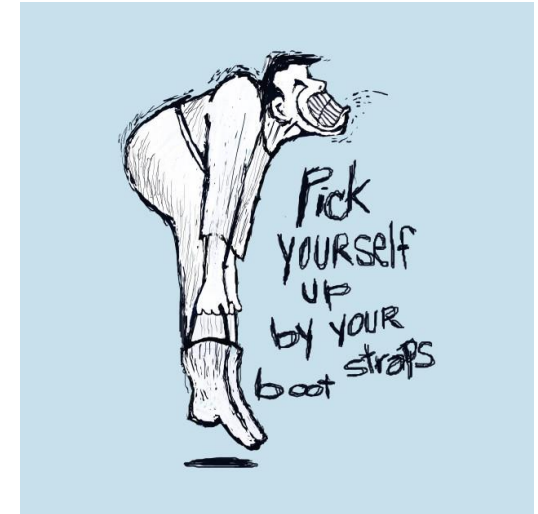
Sampling distribution



Sampling distribution!

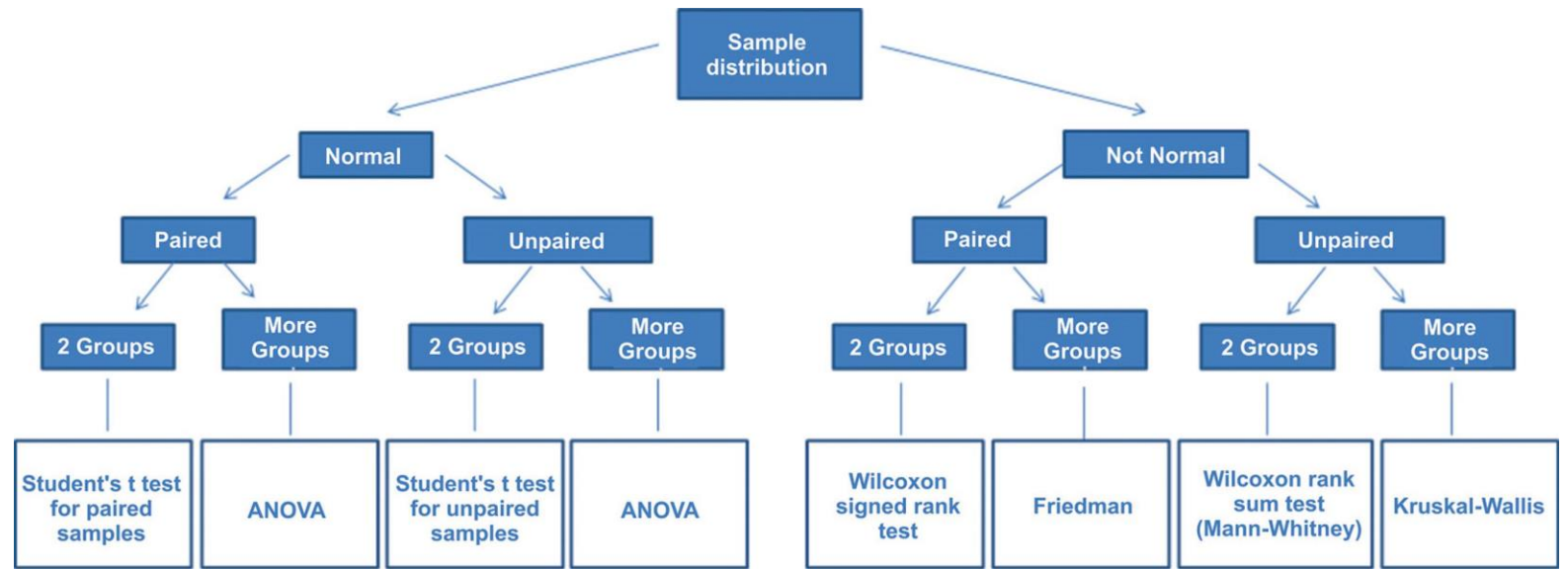
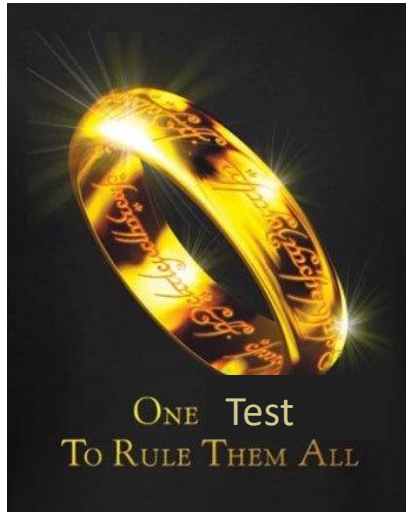
$$CI_{95} = \text{stat} \pm 2 \cdot SE^*$$

Bootstrap distribution

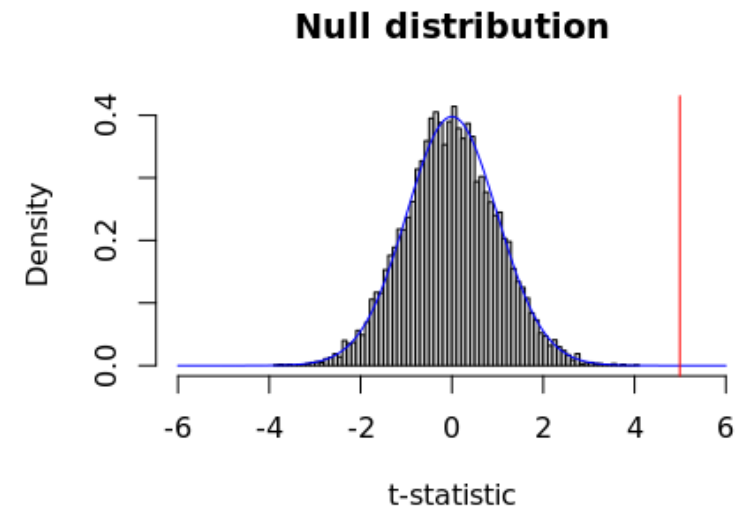
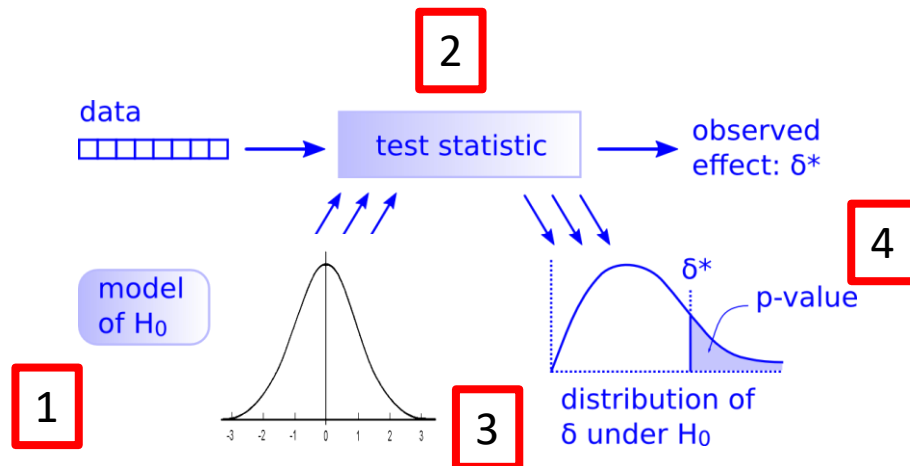


Sample with replacement from our original sample to mimic a sampling distribution

Hypothesis tests



Just need to follow 5 steps!



Randomization/permutation tests

Create a null distribution through computational simulations/shuffling

- `rbinom()`, `sample()`, etc.

$$H_0: \pi = 0.5$$

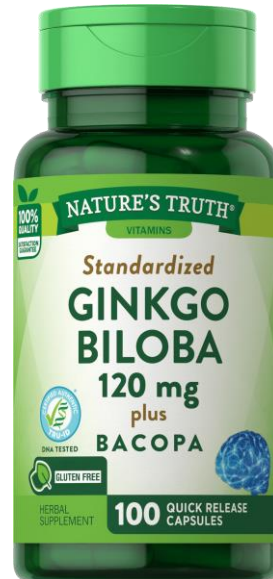
$$H_A: \pi > 0.5$$

$$H_0: \mu_T - \mu_C = 0$$

$$H_A: \mu_T - \mu_C > 0$$

$$H_0: \mu_i = \mu_j = \dots = \mu_k$$

$$H_A: \mu_i \neq \mu_j \text{ for some } i, j$$



Data	1 Sample	2 Samples	> 2 Samples
Categorical data	$H_0: \pi = p_0$ $H_A: \pi \neq p_0$ <u>Flip "coins"</u> <code>rbinom()</code>	$H_0: \pi_1 = \pi_2$ $H_A: \pi_1 \neq \pi_2$ <u>Flip "coins"</u> <code>rbinom()</code>	$H_0: \pi_1 = p_1, \pi_2 = p_2, \dots, \pi_k = p_k$ $H_A: \text{At least one } p_i \text{ is different than specified}$ <u>Flip coins</u> <code>rmultinom()</code>
Quantitative data	$H_0: \mu = v_0$ $H_A: \mu \neq v_0$ <u>resample</u> <code>sample(... , replace = TRUE)</code>	$H_0: \mu_1 = \mu_2$ $H_A: \mu_1 \neq \mu_2$ <u>Shuffle data</u> <code>sample()</code>	$H_0: \mu_1 = \mu_2 = \dots = \mu_k$ $H_A: \text{At least one } \mu_i \text{ is different}$ <u>Shuffle data</u> <code>sample()</code>

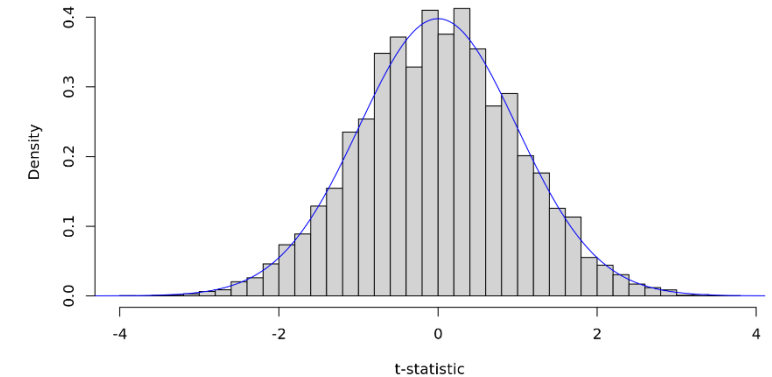
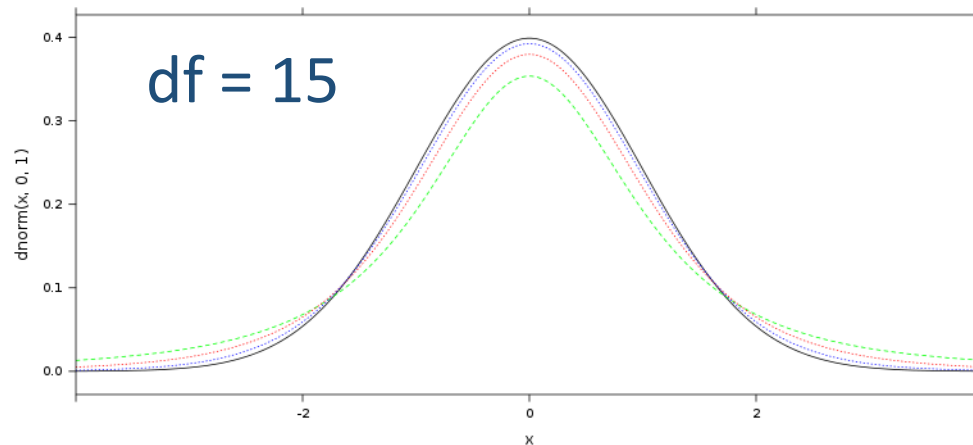
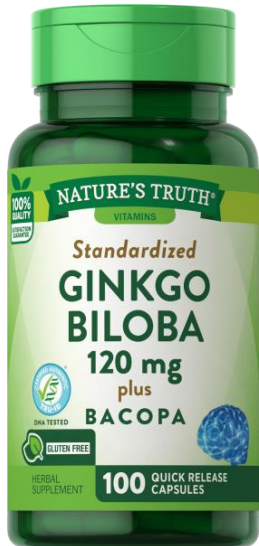
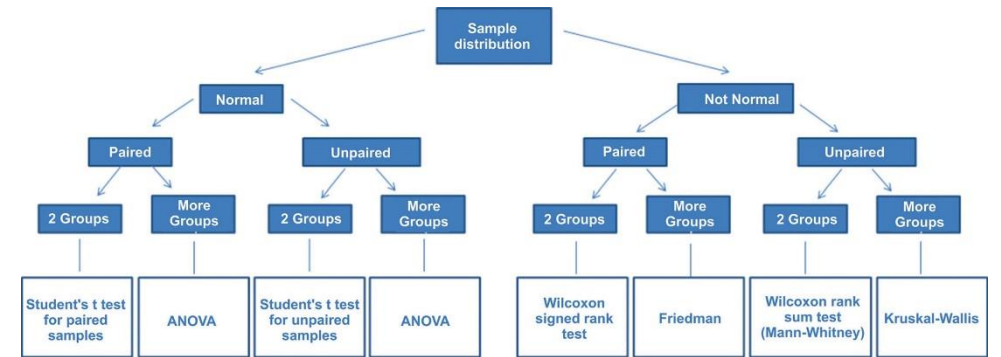
Parametric tests

Use mathematical density functions for the null distribution

$$H_0: \mu_T - \mu_C = 0$$

$$H_A: \mu_T - \mu_C > 0$$

$$t = \frac{\bar{x}_t - \bar{x}_c}{\sqrt{\frac{s_t^2}{n_t} + \frac{s_c^2}{n_c}}}$$



Data	1 Sample	2 Samples	> 2 Samples
Categorical data	$H_0: \pi = p_0$ $H_A: \pi \neq p_0$ <u>z-test</u> $z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$	$H_0: \pi_1 = \pi_2$ $H_A: \pi_1 \neq \pi_2$ <u>z-test or a chi-square</u> $z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}}$	$H_0: \pi_1 = p_1, \pi_2 = p_2, \dots, \pi_k = p_k$ $H_A: \text{At least one } p_i \text{ is different than specified}$ <u>chi-square test</u> $\chi^2 = \sum_{i=1}^k \frac{(\text{Observed}_i - \text{Expected}_i)^2}{\text{Expected}_i}$ $\text{df} = k - 1$
Quantitative data	$H_0: \mu = v_0$ $H_A: \mu \neq v_0$ <u>One sample t-test</u> $t = \frac{\bar{x} - v_0}{s/\sqrt{n}}$ $\text{df} = n - 1$	$H_0: \mu_1 = \mu_2$ $H_A: \mu_1 \neq \mu_2$ <u>Two sample t-test</u> $t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ $\text{df} = \min n_1 - 1, n_2 - 1$	$H_0: \mu_1 = \mu_2 = \dots = \mu_k$ $H_A: \text{At least one } \mu_i \text{ is different}$ <u>Analysis of Variance</u> $F = \frac{\frac{1}{K-1} \sum_{i=1}^K n_i (\bar{x}_i - \bar{x}_{tot})^2}{\frac{1}{N-K} \sum_{i=1}^K \sum_{j=1}^{n_i} (x_{ij} - \bar{x}_i)^2}$ $\text{df}_1 = k, \text{df}_2 = n - k$

Data	1 Sample	2 Samples
Categorical Data	$SE = \sqrt{\frac{\pi(1-\pi)}{n}}$ $\hat{p} \pm z^* \cdot \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$	$SE = \sqrt{\frac{\pi_1(1-\pi_1)}{n_1} + \frac{\pi_2(1-\pi_2)}{n_2}}$ $\hat{p}_1 - \hat{p}_2 \pm z^* \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$
Quantitative Data	$SE = \frac{s}{\sqrt{n}}$ $\bar{x} \pm t^* \frac{s}{\sqrt{n}}$	$SE = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ $(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$

Theories of hypothesis testing



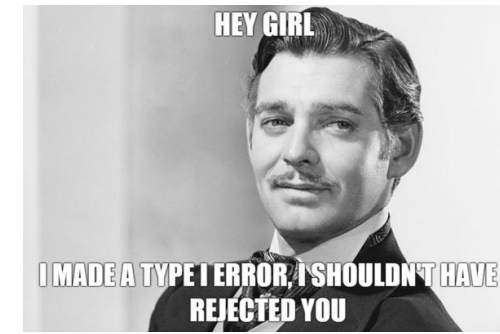
Fisher (1890-1962)



Neyman (1894-1981)

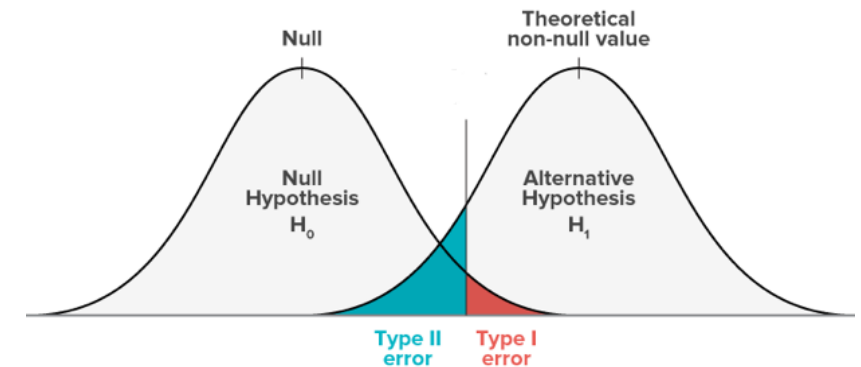
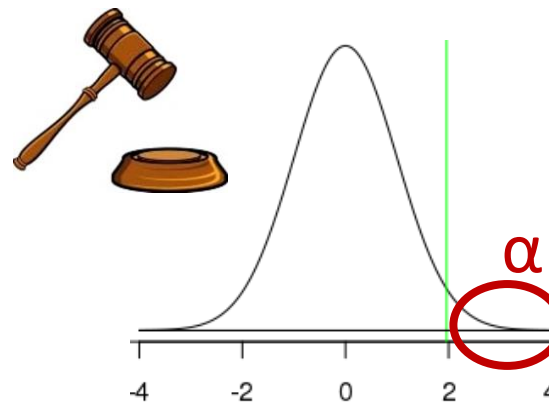
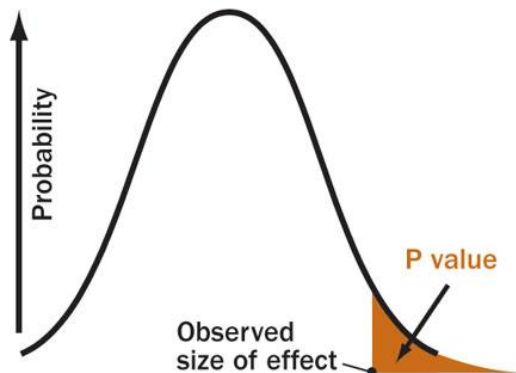
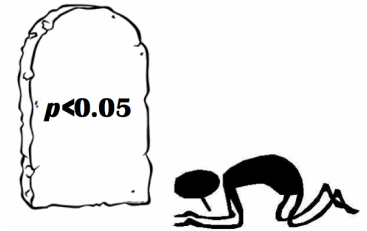


Pearson (1895-1980)

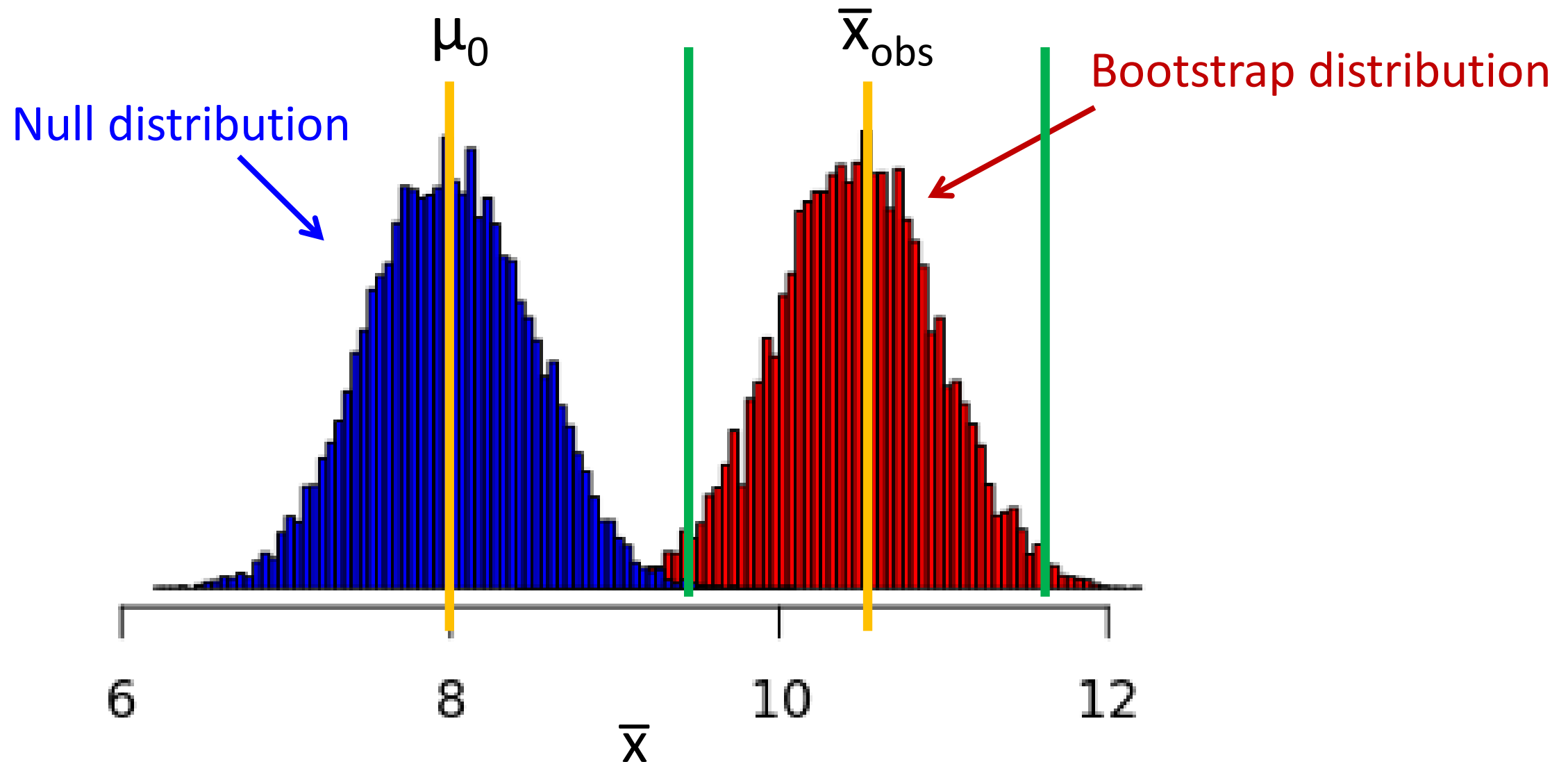


p-value a strength of evidence

Use p-value to make a decision



Relationship between null and bootstrap distributions



Data manipulation with dplyr

dplyr is a package that has a set of verbs for transformations data

- All these function **take a data frame** and other arguments and **return a data frame**

1. `filter()`
2. `select()`
3. `mutate()`
4. `arrange()`
5. `summarize()`
6. `group_by()`



```
film_results <- movies |>
  filter(title_type == "Feature Film") |>
  select(critics_score, audience_score, genre) |>
  mutate(audience_prefs =
    audience_score - critics_score) |>
  group_by(genre) |>
  summarize(mean_audience_prefs =
    mean(audience_prefs)) |>
  arrange(desc(mean_audience_prefs))

head(film_results )
```

Grammar of graphics with ggplot

A Frame: Coordinate system on which data is placed

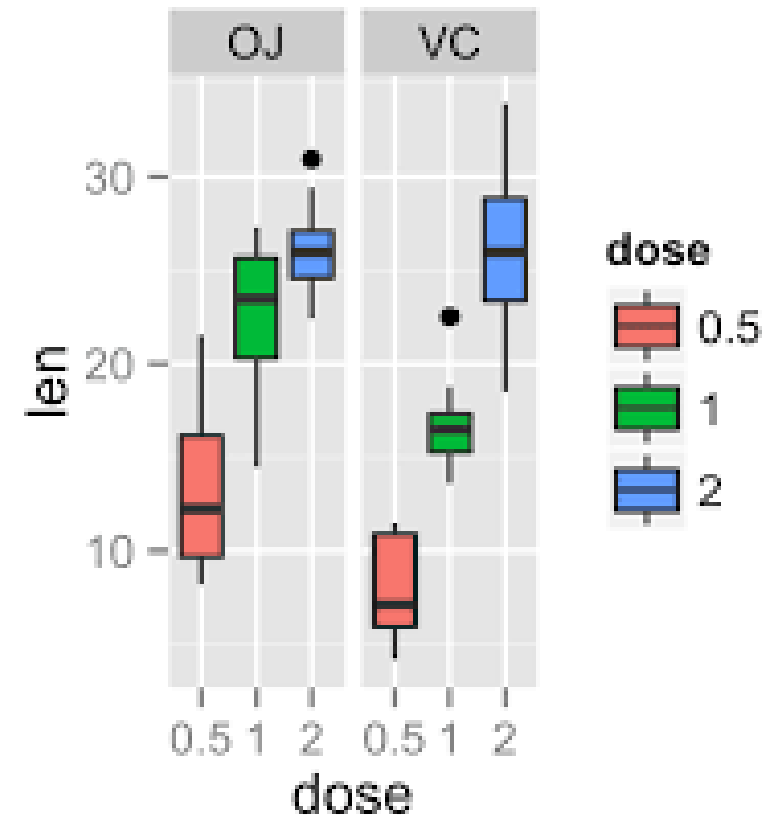
Glyphs: basic graphic unit representing cases or statistics

Scales and guides: shows how to interpret axes and other properties of the glyphs

Facets: allows for multiple side-by-side graphs based on a categorical variable

Layers: allows for more than one types of data to be mapped onto the same figure

Theme: contains finer points of display (e.g., font size, background color, etc.)



Questions

