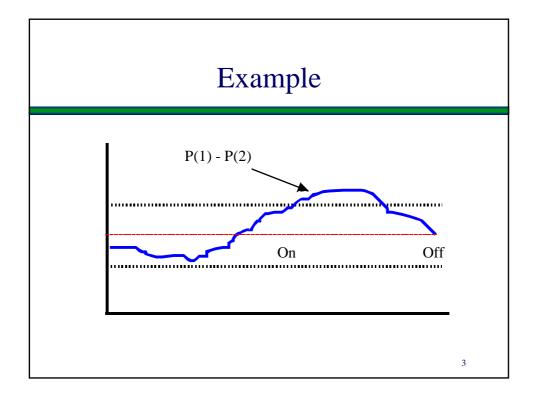
### Pairs Trading:

performance of a relative value arbitrage strategy

by
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## Statistical "Arbitrage"

- Identify a pair of stocks that move in tandem
- When they diverge:
  - □ short the higher one
  - □ buy the lower one
- Unwind upon convergence



#### **Economic Rationale**

- Tartaglia:
  - "Human beings don't like to trade against human nature, which wants to buy stocks after they go up, not down..."
- Imperfect markets?
  - Over-reaction
  - Under-reaction

### **Relative Pricing**

- Approximate APT Models
  - □ Long-short "arbitrage in expectations"
  - □ Self-financing
  - □ Eliminate relative mispricing
  - □ Silent on absolute pricing
- Mechanisms
  - □ risk-matched portfolios
  - □ risk-matched securities

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#### Methodology

- Two stages:
  - □ 1. Pairs Formation
  - □ 2. Pairs Trading
- Committed Capital
  - □ full period
  - □ when-needed
  - □ no extra leverage

#### Pairs Formation Period

- Match on stock cumulative return index
  - □ Minimize squared price error
  - □ Twelve months of daily prices
- Equivalent to matching on state-prices
  - □ Each day is a different state
  - □ Assumes stationarity
  - □ Assumes a year captures all states

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#### Pairs Formation Period

- Daily CRSP files
- Eliminate stocks that missed a day trading in a year
- Cumulative total return index for each stock
- Also restrict to same broad industry category: Utilities, Transports, Financials, Industrials

#### **Trading Period**

- Six-month periods: 1962-1997
  - □ starting a new "trader" each month
  - □ closing all positions at end of each six month
- How many pairs to use?
  - 5, 20 and 20 after first 100, then all pairs under distance metric

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#### **Trading Period**

- Open at 2 sigma (historical sigma over past one year)
- Close upon convergence, or end of sixmonth period

#### **Excess Return**

- Return on committed capital
  - □ Sum of payoffs over all pairs in period/# pairs
  - □ Allow \$1/per pair
- Return on employed capital
  - □ All \$1/pair used

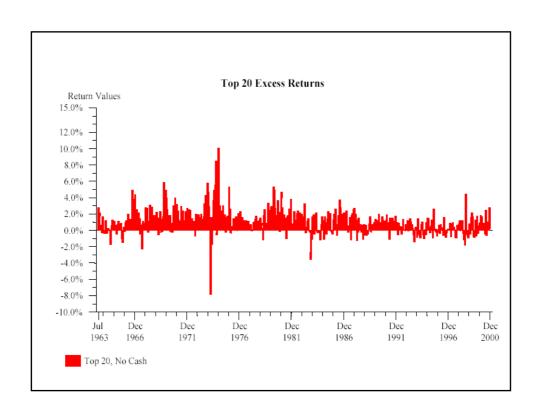
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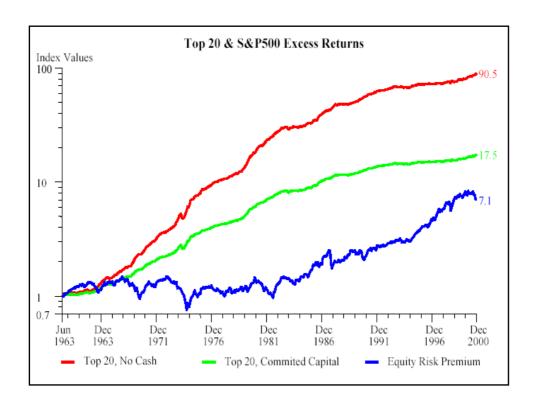
#### Results for Same Day Trading

- Portfolio of 5 and 20 best pairs earn an average of 6% per six month period.
   Average size of stocks in pairs: 3rd to 4th decile
- Utilities predominate

Trading	Performance

	Top 5	Top 20	20- 100	All
6-month Mean	5.98%	6.01%	4.51%	4.10%
Utilities	81%	82%	33%	9%
Transportation	1%	1%	2%	3%
Financial	4%	4%	16%	12%
Industrial	13%	13%	48%	76%
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# Systematic Risk Exposure

	Top 5	top 20	20 a 100	All	ERP
Intercept	0.0056	0.0061	0.0056	0.0044	0.0070
U.S. EquityPrem.	0.0102	0.0080	-0.0067	-0.0167	
Small - Big	0.0404	0.0511	0.0465	0.0688	0.2117
High B/M - Low B/M	0.0791	0.0210	0.0180	0.0689	-05847

### **Ibbotson Risk Exposures**

	Top 5	top 20	20 a 100	All	ERP
Intercept	0.0059	0.0064	0.0057	0.0047	0.0035
U.S. Equity Prem.	0296	0259	-0.0206	-0.0408	
Small Stock Prem.	0.0477	0.0494	0.0349	0.0496	0.1771
Bond Default Prem.	0.1288	0.1266	0.1344	0.1680	0.7103
Bond Horizon rem.	0.0815	0.0743	0.0440	0.0429	0.6805

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#### **Transactions Costs**

- Conservative round-trip cost estimate
  - □ Same Day vs. Wait 1 Day = 200 basis points
  - □ 2.4 round-trip per pair/6 months
  - 83 bp/round-trip and an effective spread of 42 bp
- Net 6 month excess return: 168 to 88 BP

## **Improvements**

- We may be opening pairs too soon
- We may not be picking pairs wisely
- Other sensible rules
  - □ don't open a pair on the last day of the period

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## Summary of findings

- There exists relative price reversion
- Marginally profitable
  - □ Consistent with hedge fund business
- Not simply mean reversion