$\begin{array}{ll} & \text{Inlegrate}\left[E^{\wedge}\left(-Abs\left[x+y\right]/u\right), \left\{x,-w,w\right\},\\ & \text{Assumptions} \rightarrow Element\left[w,Reals\right] \&\& Element\left[y,Reals\right] \&\& w > 0 \end{array}$

$$\text{Out}[22] = \begin{cases} e^{-\frac{w}{u} - \frac{y}{u}} \left(-1 + e^{\frac{2w}{u}} \right) u & w - y < 0 \&\& w > 0 \&\& w + y > 0 \\ -e^{-\frac{w}{u} - \frac{y}{u}} \left(1 + e^{\frac{2y}{u}} - 2 e^{\frac{w}{u} + \frac{y}{u}} \right) u & w - y > 0 \&\& w > 0 \&\& w + y > 0 \end{cases}$$

$$e^{-\frac{w}{u} - \frac{y}{u}} \left(-1 + e^{\frac{w}{u} + \frac{y}{u}} \right) u & w - y = 0 \&\& w > 0 \&\& w + y > 0$$

$$2 e^{\frac{y}{u}} u \, \text{Sinh} \left[\frac{w}{u} \right] & \text{True}$$

$$\ln[23] = \mathbf{f}[\mathbf{y}, \mathbf{u}, \mathbf{w}] := \begin{cases} e^{-\frac{\mathbf{w}}{\mathbf{u}} - \frac{\mathbf{y}}{\mathbf{u}}} \left(-1 + e^{\frac{2\mathbf{w}}{\mathbf{u}}} \right) \mathbf{u} & \mathbf{w} - \mathbf{y} < 0 & & \mathbf{w} > 0 & & \mathbf{w} + \mathbf{y} > 0 \\ -e^{-\frac{\mathbf{w}}{\mathbf{u}} - \frac{\mathbf{y}}{\mathbf{u}}} \left(1 + e^{\frac{2\mathbf{y}}{\mathbf{u}}} - 2 e^{\frac{\mathbf{w}}{\mathbf{u}} + \frac{\mathbf{y}}{\mathbf{u}}} \right) \mathbf{u} & \mathbf{w} - \mathbf{y} > 0 & & \mathbf{w} > 0 & & \mathbf{w} + \mathbf{y} > 0 \\ e^{-\frac{\mathbf{w}}{\mathbf{u}} - \frac{\mathbf{y}}{\mathbf{u}}} \left(-1 + e^{\frac{\mathbf{w}}{\mathbf{u}} + \frac{\mathbf{y}}{\mathbf{u}}} \right) \mathbf{u} & \mathbf{w} - \mathbf{y} = 0 & & \mathbf{w} > 0 & & \mathbf{w} + \mathbf{y} > 0 \\ 2 e^{\frac{\mathbf{y}}{\mathbf{u}}} \mathbf{u} \sinh\left[\frac{\mathbf{w}}{\mathbf{u}}\right] & \text{True} \end{cases}$$

 $ln[26]:= LogPlot[f[x, 10, 1], {x, 0, 100}]$

