Group 3: Data Analysis

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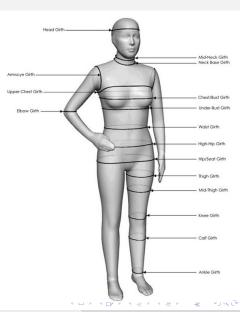
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Introduction

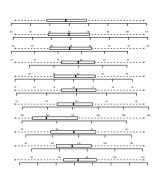
- The dataset, "Exploring Relationships in Body Dimensions", contains 25 variables: 21 body dimension measurements as well as age, weight, height, and gender for 507 physically active, young individuals.
- Of the body dimension measurements, 9 were skeletal/diameter measurements and 12 were girth/circumference measurements.
- Of the 507 individual observations, there are 247 men and 260 women.
- No missing values. Measurements made with metric scale.



Description of Variables

Summary table(left) Boxplot(right)

		. 1 (0 -/	
variable	Min.	Median	Mean	Max.
weight	42.00	68.20	69.15	116.40
chest.diam	22.20	27.80	27.97	35.60
chest.dep	14.30	19.00	19.23	27.50
bitro.diam	24.70	32.00	31.98	38.00
wrist.min	13.00	16.10	16.10	19.60
ankle.min	16.40	22.00	22.16	29.30
height	147.20	170.30	171.10	198.10
age	18.00	27.00	30.18	67.00
shoulder	85.90	108.20	108.20	134.80
navel	64.00	84.60	85.65	121.10
hip	78.80	96.00	96.68	128.30

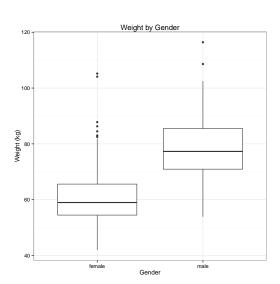


Outcome of Interest: Weight

Applications of Data:

- investigate correspondence of frame size, girths, and weight of young, athletic people
- estimate ideal weight
- inform predictions of lean/fat body compositions
- identify gender in forensic science
- design appropriate clothing (law enforcement/military)

Note: Outliers in the distribution of weight may be present because some of the individuals had unusually high muscle mass due to their high level of physical fitness.



Multiple Linear Regression Model

Initial Model

weight_i =
$$\beta_0 + \beta_1$$
chest.diam_i + β_2 chest.dep_i + β_3 bitro.diam_i
+ β_4 wrist.min_i + β_5 ankle.min_i + β_6 height_i

R Output:

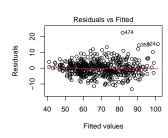
(Intercept)	chest.diam	chest.dep	bitro.diam	wrist.min	ankle.min	height
-109.89	1.34	1.54	1.20	1.11	1.15	0.18

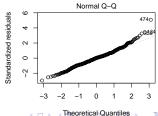
- This model was chosen by the authors of the dataset based on the idea that these
 measurements remain constant after physical maturation.
- It seems that, in our model, chest depth has the largest impact on weight.
- COMMENTS ABOUT GOODNESS OF FIT???



Model Diagnostics (Nick)

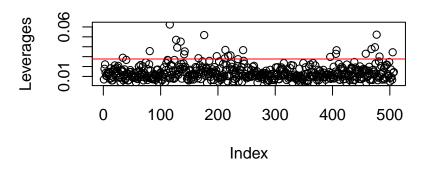
- Model diagnostics are extremely important to fitting an appropriate model.
- Assumption violations can lead to biased or faulty results.
- These plots show us that observations 124, 359, and 474 may be problematic.





Leverage

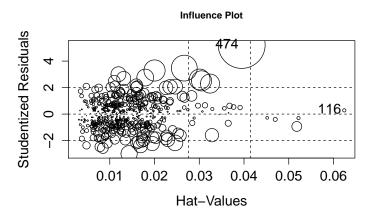
Index Plot of Leverages



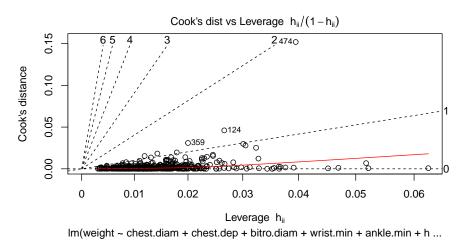
A "rule of thumb" is that leverages of more than 2p/n (p= of predictors) should be looked at more closely. Points of concern are located above the

Influence

An **influential point** is one whose removal from the dataset causes a drastic change in the fit. An influential point will either be an outlier in the data, will have high leverage, or will have both. Cook's Distance is a popular method of identifying influential points.



Cook's Distance



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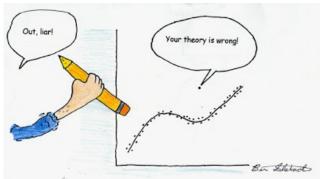
Better Fit?

Initial Model:

	 iitiai iviouc	/l.					
100.80 1.34 1.54 1.20 1.11 1.15 0.1	(Intercept)	chest.diam	chest.dep	bitro.diam	wrist.min	ankle.min	height
-109.09 1.54 1.54 1.20 1.11 1.15 0.1	-109.89	1.34	1.54	1.20	1.11	1.15	0.18

New model with influential points removed:

(Intercept)	chest.diam	chest.dep	bitro.diam	wrist.min	ankle.min	height
-109.11	1.38	1.55	1.10	0.97	1.17	0.19



Model Selection Criteria and Methods (Emily)

Goal: Find the "best" method for model selection.

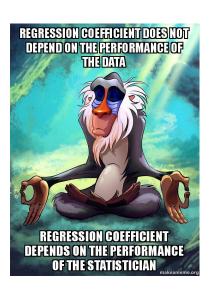
The methods used to create ten different models were:

- include all variables (1)
- suggested by paper (2)
- my selection (1)
- stepAIC (1)
- leaps (2)
- combinations of R functions and human intuition (3).

These models were compared using:

- AIC/ BIC: measure goodness-of-fit through residual sum of squares and penalizes for adding more predictors; the smaller the better.
- Adjusted R²: adjusts R² so that the model is penalized for adding more predictors; the larger the better.
- PRESS is a summary measure focused on prediction; the smaller the better.

My Selection (Emily)



- Predictors needed: age, height and gender (since these contribute significantly to weight)
- Predictors we will allow: the predictors used in the inital model (chest diameter, chest depth and bitro diameter), pelvic bredth, shoulder, chest, waist, hip and thigh (since these are directly associated with weight)
- The model I decided was the "best" includes the predictors chest.dep, chest.diam, shoulder, waist, hip, thight and height², based on AIC and BIC.

R function: stepAIC() (Emily)

To demonstrate these two R functions, we will begin with a simple model:

```
MLRex <- lm(weight height + wrist.min + ankle.min + chest, data = body)
```

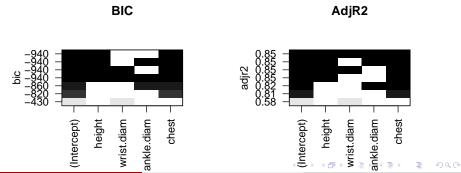
The R function found in the package "MASS" called "stepAIC()" performs stepwise model selection by AIC. This function allows you to indicate the direction of the search: forward, backward or both.

```
step <- stepAIC(MLRex, direction = "both")
head(stepanova)</pre>
```

```
Initial Model: weight
                       height + wrist.diam + ankle.diam + chest
Final Model: weight height + ankle.diam + chest
                                                              ATC
            Step
                  Df
                      Deviance Resid. Df
                                            Resid. Dev
                                       502
                                                13294.14
                                                         1666, 150
    - wrist.diam 1
                      47.90427
                                       503
                                                13342.05
                                                         1665.974
```

R function: leaps() (Emily)

```
leaps <- regsubsets(weight height + wrist.diam + ankle.diam + chest, nbest = 2,
data = body)
par(mfrow = c(1, 2))
plot(leaps, main = "BIC")
plot(leaps, scale = "adjr2", main = "AdjR2")</pre>
```



Summary (Emily)

Table 2: Criteria Summary for each model

Method	Adjusted R ²	PRESS	BIC	AIC	MLR#
all variables from dataset used	0.9753	2384	2326	2216	all
suggested by paper	0.8869	10405	3004	2970	i
suggested by paper	0.9727	2560	2319	2256	1
my model	0.9632	3408	2441	2402	2
stepAIC	0.9754	2329	2282	2206	3
stepAIC and adjustments	0.9759	2281	2271	2195	4
leaps (adj R²)	0.9755	2335	2292	2207	5
leaps(adj R²)and adjustments	0.9764	2255	2278	2189	6
leaps(BIC)	0.9749	2353	2272	2213	7
leaps(BIC) and adjustments	0.9753	2316	2264	2205	8
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Red corresponds to the best value for that criteria, blue is the second best.

- Model Selection truely is an art form.
- R can mechanically run through steps, interactions, combinations, etc.
- R cannot subjectively look at the variables to determine the absolute best model.
- To acheive the model of "best" fit, it is best to utilize a combination of R functions, criteria methods, and your own adjustments/ intuition.

Model Selection (Yiding)

Logistic Model: $logit(p_i) = \beta_0 + \beta_1 X_{i1} + ... + \beta_m X_{im}$

Model selection criteria:

 AIC =nlog(RRS/n) + 2(p + 1) in R: step()

	AIC criteria model selection	
Step #	Model	AIC
1	logi(SEX)=WT+CDM+CDP+BDM+WR+ANK+HT+AGE+SHD+NAV+HIP	110.35
2	logi(SEX)=WT+CDP+BDM+WR+ANK+HT+AGE+SHD+NAV+HIP	108.36
3	logi(SEX)=WT+CDP+BDM+WR+HT+AGE+SHD+NAV+HIP	106.45
4	logi(SEX)=CDP+BDM+WR+HT+AGE+SHD+NAV+HIP	104.55
5	logi(SEX)=CDP+WR+HT+AGE+SHD+NAV+HIP	102.69
6	logi(SEX)=CDP+WR+HT+AGE+SHD+HIP	101.05

• BIC = nlog(RSS/n) + (p+1)log(n)& Posterior Probability

$$= p(\theta \mid x) = \frac{p(x|\theta)p(\theta)}{p(x)}$$

in R: BMA packages bic.glm()

	BIC criteria model selection		
Model #	Model	BIC	Posterior prob
1	logi(SEX)=WR+HT+SHD+HIP	-3033	0.453
2	logi(SEX)=WR+HT+AGE+SHD+HIP	-3031	0.157
3	logi(SEX)=CDP+WR+HT+AGE+SHD+HIP	-3031	0.151
4	logi(SEX)=WR+HT+SHD+NAV+HIP	-3031	0.142
5	logi(SEX)=WR+HT+SHD+HIP	-3029	0.047

Check the Goodness of Model (Yiding)

Linearity

Residuals vs Fitted Values

Pearson residuals:

$$r_i = \frac{y_i - \hat{\mu}_i}{\sqrt{\hat{V}(y_i)}} = \frac{y_i - n_i \hat{\pi}_i}{\sqrt{n_i \hat{\pi}_i (1 - \hat{\pi}_i)}}$$

Predictive ability

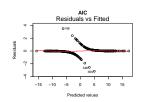
ROC curve:

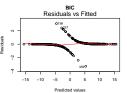
sinsitivity vs 1-specificity Somer's rank correlation:

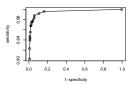
$$D_{xy}=2(c-0.5)$$

c is the area under the ROC curve.

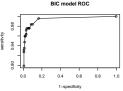
Hmisc package: somers2()







AIC model ROC



Model	Area ROC curve	Somers' D _{xy}
AIC	0.9944721	0.9889443
BIC	0.9941607	0.9883214

Ada-boosting (Yiding)

Algorithem:

Given: $(x_1, y_1), ..., (x_m, y_m)$ where

$$x_i \in X, y_i \in Y = \{-1, +1\}$$
 Initialize

$$D_1(i) = 1/m.$$

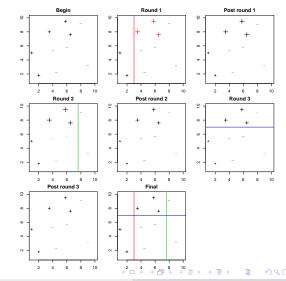
For
$$t=1,\,...,\,T$$
:

- ullet Train weak learner using distribution D_t .
- Get weak hypothesis $h_t: X \to \{-1, +1\}$ with error $\epsilon_t = Pr_{i \sim D_t} \left[h_t(x_i) \neq y_i \right]$
- error $\epsilon_t = Pr_{i \sim D_t} [h_t(x_i) \neq y_i]$
- Choose $\alpha_t = \frac{1}{2} ln \left(\frac{1 \epsilon_t}{\epsilon_t} \right)$
- Update:

$$D_{t+1}(i) = \frac{D_t(i)}{Z_t} \times \begin{cases} e^{-\alpha_t} & \text{if } h_t(x_i) = y_i \\ e^{\alpha_t} & \text{if } h_t(x_i) \neq y_i \end{cases}$$

 $= \frac{D_i(i)\exp(\alpha_t y_i h_t(x_i))}{Z_t}$

Final hypothesis: $H(x) = sign\left(\sum_{t=1}^{T} \alpha_t h_t(x)\right)$



Logistic Regression vs Ada-boosting (Yiding)

Logistic Regression

Predictive ability depends on cutoff point

Cutoff point	Sensitivity	Specificity
0.00	1.000	0.004
0.05	0.996	0.838
0.10	0.992	0.892
0.15	0.988	0.942
0.20	0.984	0.954
	***	***
0.85	0.923	0.992
0.90	0.903	0.992

Ada-boosting

Predictive ability depends on variables

Round #	Original data	AIC data	BIC data
	Sensitiviy; Specificity; Accuracy	Sensitiviy; Specificity; Accuracy	Sensitiviy; Specificity; Accuracy
1	0.975; 0.925; 0.949	0.967; 0.962; 0.965	0.967; 0.947; 0.957
2	0.953; 0.936; 0.945	0.953; 0.920; 0.937	0.961; 0.936; 0.949
3	0.949; 0.951; 0.949	0.954; 0.959; 0.957	0.954; 0.959; 0.957
4	0.983; 0.932; 0.957	0.983; 0.955; 0.961	0.983; 0.962; 0.972
5	0.983; 0.924; 0.953	0.983; 0.931; 0.957	0.983; 0.947; 0.965
Avarage	0.969; 0.934; 0.951	0.968; 0.945; 0.955	0.970; 0.950; 0.960

Inference

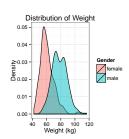
Logistic Regression $\sqrt{}$

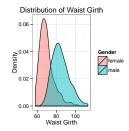
Prediction

Ada-boosting $\sqrt{}$

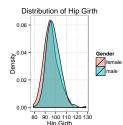
Differences between Males and Females (Liza)

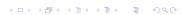
- Are there significant differences in the body measurements most useful for predicting weight in males and females?
- Is one regression formula appropriate for predicting weight for both genders?
- Can we use regression trees to help explore these questions?











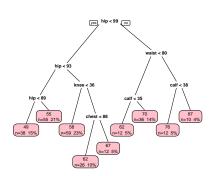
Regression Trees (Liza)

Pruned Tree, Weight (Male)

hip < 100 no hip < 107 hip < 94 shoulder < 113 97 n=19 8% 72 78 n=29 12% 72

n=29 12%

Regression Tree, Weight (Female)



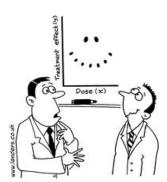
- Variables used in male tree: hip shoulder girths
- Variable used in female tree: hip, knee, chest, waist and calf girths

n=38 15%

Conclusions (Liza)

- Regression trees are useful for exploring data and provide a useful alternative to parametric regression methods, though are not intended for making predictions.
- Results here suggest that separate models for males and females might be appropriate.
- Model fitting and selection exercises could test this hypothesis.

Group Conclusions



"It's a non-linear pattern with outliers.....but for some reason I'm very happy with the data."

What have we learned?

- Always check your assumptions, even low influence outliers can change your model fit
- With model selection, a combination of selection criteria, R functions and intuition are needed to create the model of "best" fit.
- Inference choose Logistic Regression; prediction choose Ada-boosting.
- Regression trees are a powerful, yet simple, non-parametric method for exploring data.