

# The Path Towards 5G: Massive MIMO



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# Outline

- Introduction
- How to Achieve Higher Spectral Efficiency
- Basic Properties of Massive MIMO
- Massive MIMO Transmission Protocol
- 4 Myths and Misconceptions
- Research Trends and Open Questions
- Summary

# INTRODUCTION

# Incredible Success of Wireless Communications

## ***Martin Cooper's law***

*The number of voice/data connections has doubled every 2.5 years (+32% per year) since the beginning of wireless*

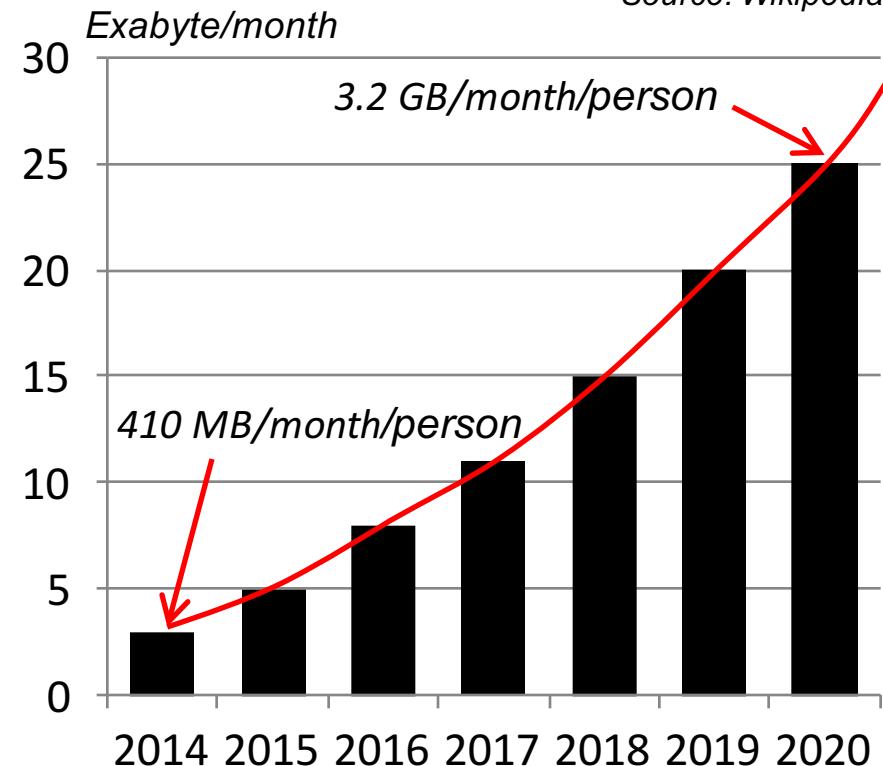
Last 45 years: 1 Million Increase in Wireless Traffic

*Two-way radio, FM/AM radio, satellites, cellular, WiFi, etc.*



Source: Wikipedia

- Future Network Traffic Growth
  - 38% annual data traffic growth
  - Slightly faster than in the past!
  - Exponential increase
  - Extrapolation: 5x in 5 years  
25x in 10 years  
125x in 15 years

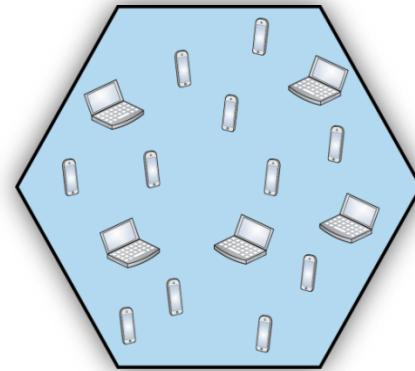


Source: Ericsson (November 2014)

# Evolving Networks for Higher Traffic

- Increase Network Throughput [bit/s/km<sup>2</sup>]

- Consider a given area



- Simple Formula for Network Throughput:

$$\frac{\text{Throughput}}{\text{bit/s/km}^2} = \frac{\text{Available spectrum}}{\text{Hz}} \cdot \frac{\text{Cell density}}{\text{Cell/km}^2} \cdot \frac{\text{Spectral efficiency}}{\text{bit/s/Hz/Cell}}$$

- Ways to Achieve 1000x Improvement:

	More spectrum	Higher cell density	Higher spectral efficiency
Nokia (2011)	10x	10x	10x
SK Telecom (2012)	3x	56x	6x

New regulations,  
cognitive radio,  
mmWave bands

Ultra dense,  
heterogeneous  
deployments

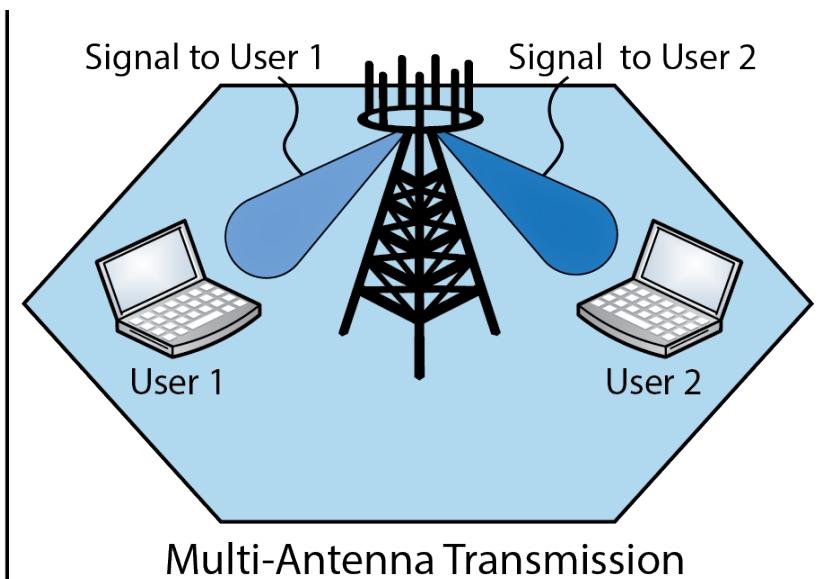
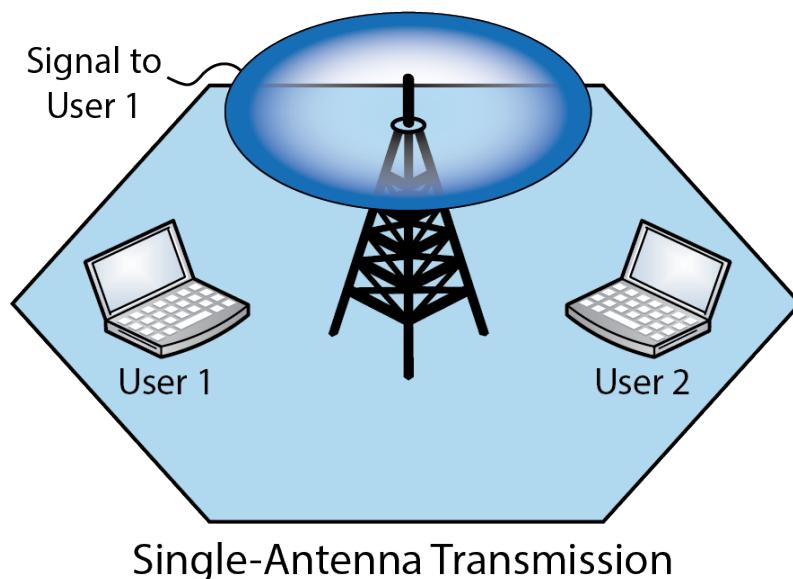
**Massive MIMO**  
*(Topic of this talk)*  
?x

How to achieve

**HIGHER SPECTRAL EFFICIENCY**

# Higher Spectral Efficiency

- Point-to-Point Spectral Efficiency:  $\Uparrow \rightarrow \Uparrow$ 
  - Governed by Shannon's capacity limit:
$$\log_2 \left( 1 + \frac{\text{Received Signal Power}}{\text{Interference Power} + \text{Noise Power}} \right) \text{ [bit/s/Hz/user]}$$
  - Cannot do much: 4 bit/s/Hz  $\rightarrow$  8 bit/s/Hz requires 17 times more power!
- Many Parallel Transmissions: *Spatially focused to each desired user*



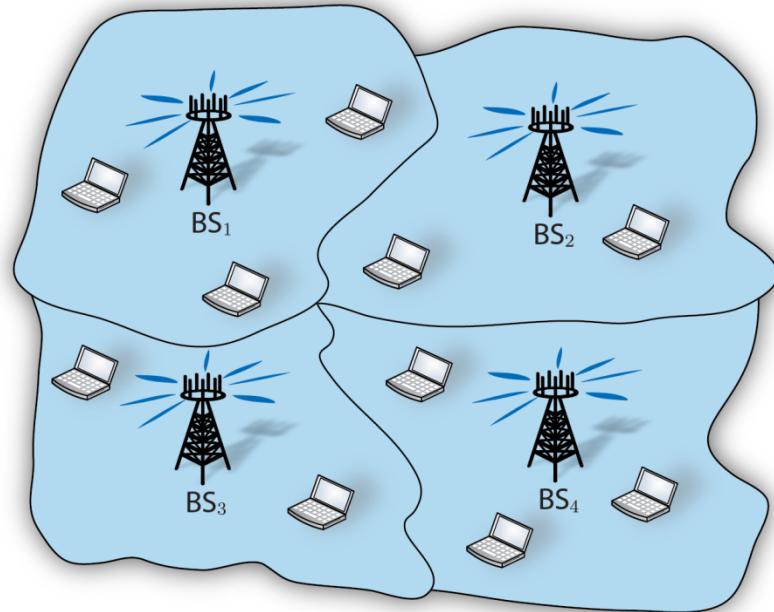
# Multi-User MIMO (Multiple-input Multiple-output)

- Multi-Cell Multi-User MIMO
  - Base stations (BSs) with  $M$  antennas
  - Parallel uplink/downlink for  $K$  users
  - Channel coherence block:  $S$  symbols
- Theory: Hardware is Limiting
  - Spectral efficiency roughly prop. to

$$\min\left(M, K, \frac{S}{2}\right)$$

- 2x improvement = 2x antennas and users (since  $S \in [100, 10000]$ )

- Practice: Interference is Limiting
  - Multi-user MIMO in LTE-A: Up to 8 antennas
  - Small gains since:
    - Hard to learn users' channels
    - Hard to coordinate BSs



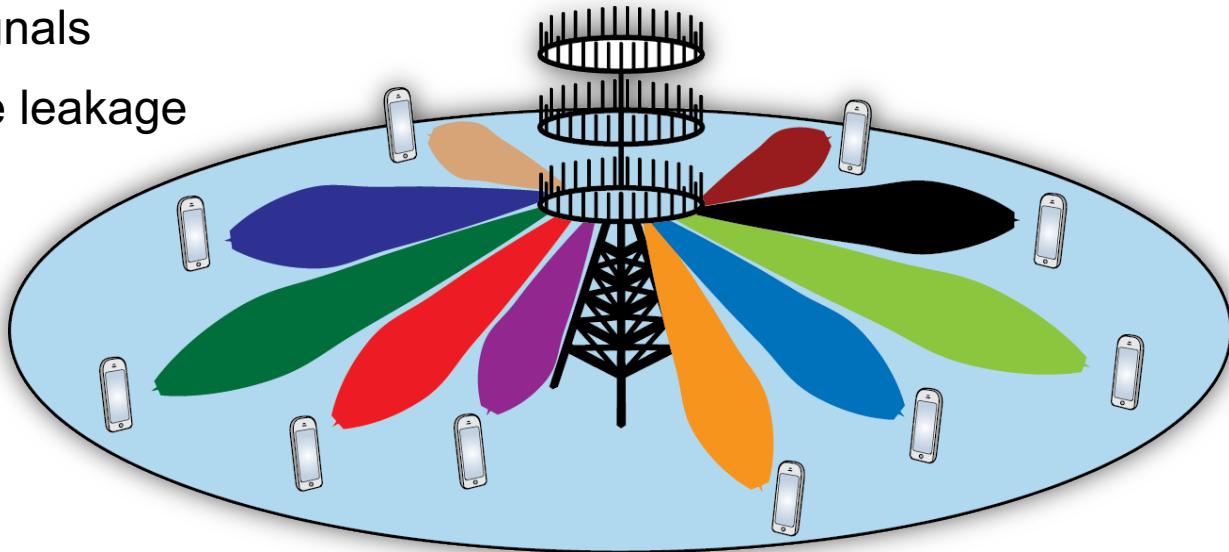
**End of the MIMO road?**  
*No reason to add more antennas/users?*

# Taking Multi-User MIMO to the Next Level

- Network Architecture: Massive MIMO
  - BS with many antennas; e.g.,  $M \approx 200$  antennas,  $K \approx 40$  users
  - Key: Excessive number of antennas,  $M \gg K$
  - Very directive signals
  - Little interference leakage

*Spectral efficiency prop.  
to number of users!*

$$\min\left(M, K, \frac{S}{2}\right) \approx K$$



- 2013 IEEE Marconi Prize Paper Award  
Thomas Marzetta, “Noncooperative Cellular Wireless with Unlimited Numbers of Base Station Antennas,” IEEE Trans. Wireless Communications, 2010.
  - Analysis based on  $M \rightarrow \infty$ , but concept applicable at any  $M$
  - Intended for conventional cellular frequencies (< 6 GHz)

# What is the Key Difference from Today?

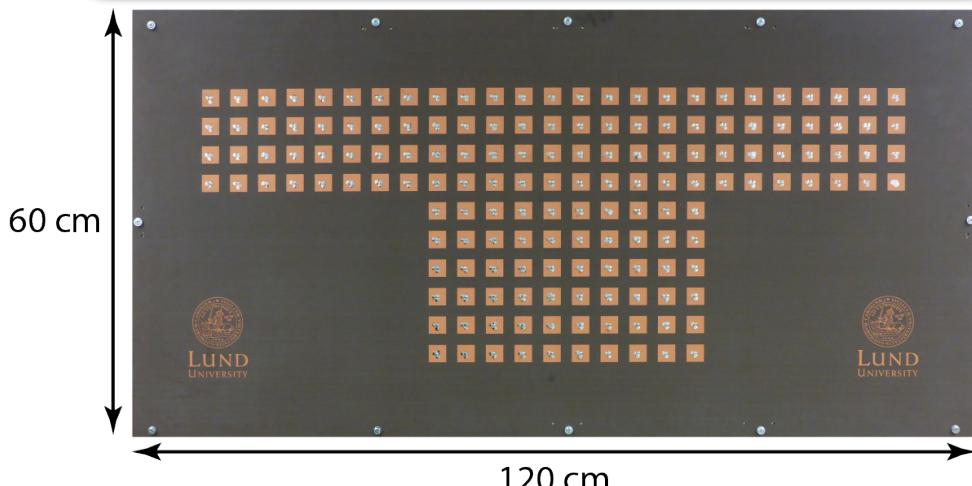
- Number of Antennas? **No, we already have many antennas!**
  - 3G/UMTS: 3 sectors x 20 element-arrays = 60 antennas
  - 4G/LTE-A: 4-MIMO x 60 = 240 antennas

## Massive MIMO Characteristics

*Many small dipoles with transceiver chains*

*Spatial multiplexing of tens of users*

*Massive in numbers – not massive in size*



160 antenna elements, LuMaMi testbed, Lund University

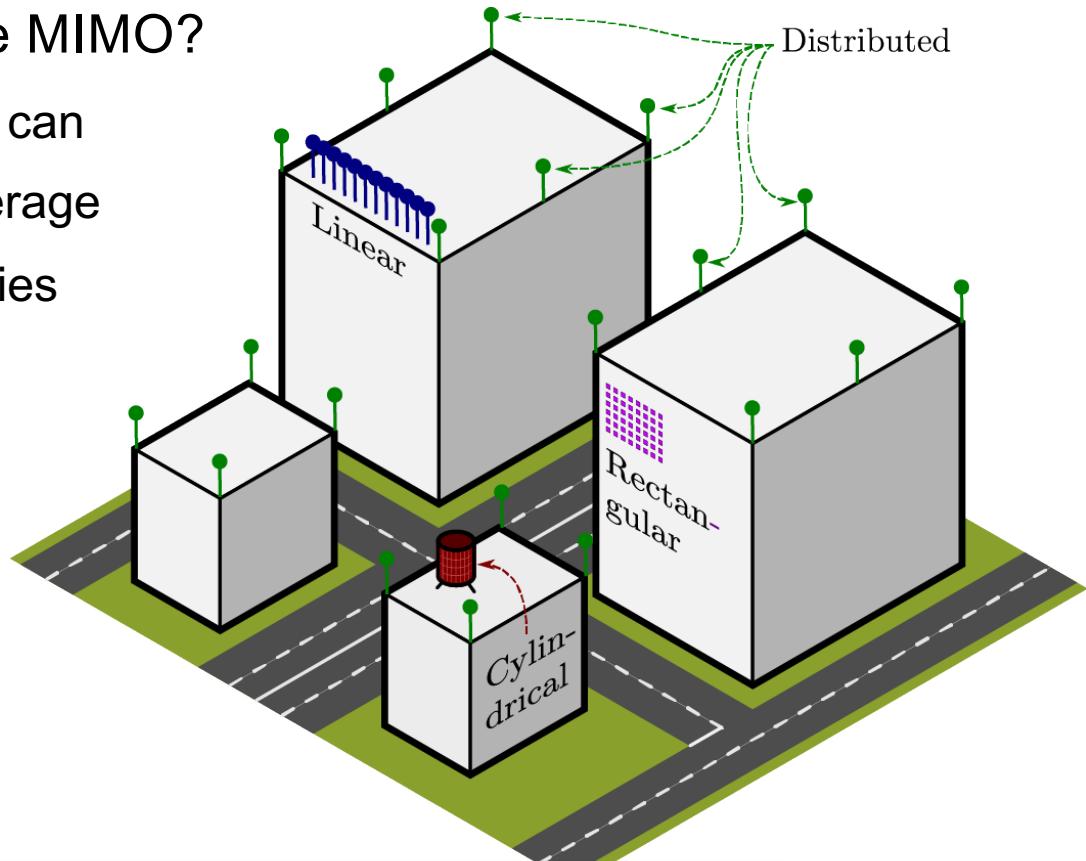
*Typical vertical array:  
10 antennas x 2 polarizations  
Only 1-2 antenna ports*



3 sectors, 4 vertical arrays per sector  
Image source: gigaom.com

# Massive MIMO Deployment

- When to Deploy Massive MIMO?
  - The future will tell, but it can
    1. Improve wide-area coverage
    2. Handle high user densities
- Co-located Deployment
  - 1D, 2D, or 3D arrays
- Distributed Deployment
  - Remote radio heads



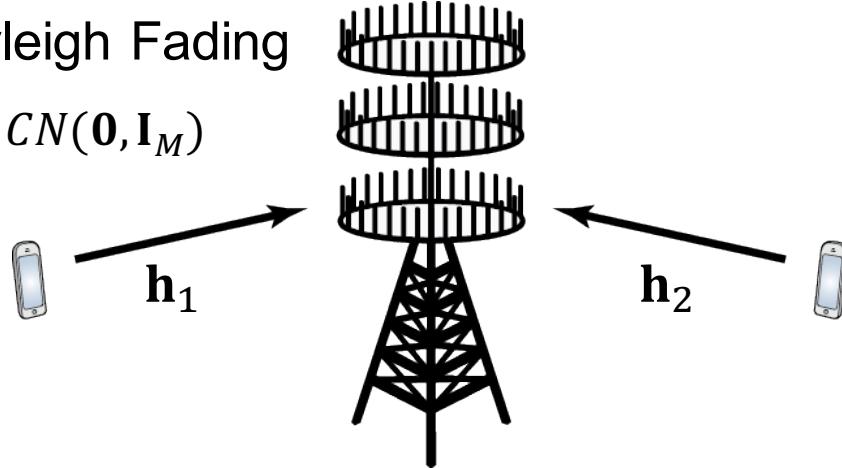
## Benefits with Massive MIMO

- Outdoor users: Handle mobility and provide coverage
- Indoor users: No need to put BSs inside buildings

Basic Properties of  
**MASSIVE MIMO**

# Asymptotic Channel Orthogonality

- Example: Uplink with Isotropic/Rayleigh Fading
  - Two users, i.i.d. channels:  $\mathbf{h}_1, \mathbf{h}_2 \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_M)$
  - Signals:  $s_1, s_2$  with power  $P$
  - Noise:  $\mathbf{n} \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_M)$
  - Received:  $\mathbf{y} = \mathbf{h}_1 s_1 + \mathbf{h}_2 s_2 + \mathbf{n}$
- Linear Processing for User 1:  $\tilde{y}_1 = \mathbf{w}_1^H \mathbf{y} = \boxed{\mathbf{w}_1^H \mathbf{h}_1 s_1} + \boxed{\mathbf{w}_1^H \mathbf{h}_2 s_2} + \boxed{\mathbf{w}_1^H \mathbf{n}}$ 
  - Maximum ratio filter:  $\mathbf{w}_1 = \frac{1}{M} \mathbf{h}_1$
  - Signal remains:  $\mathbf{w}_1^H \mathbf{h}_1 = \frac{1}{M} ||\mathbf{h}_1||^2 \xrightarrow{M \rightarrow \infty} \mathbb{E}[|h_{11}|^2] = 1$
  - Interference vanishes:  $\mathbf{w}_1^H \mathbf{h}_2 = \frac{1}{M} \mathbf{h}_1^H \mathbf{h}_2 \xrightarrow{M \rightarrow \infty} \mathbb{E}[h_{11}^H h_{21}] = 0$
  - Noise vanishes:  $\mathbf{w}_1^H \mathbf{n} = \frac{1}{M} \mathbf{h}_1^H \mathbf{n} \xrightarrow{M \rightarrow \infty} \mathbb{E}[h_{11}^H n_1] = 0$



*Asymptotically noise/interference-free communication:*  $\tilde{y}_1 \xrightarrow{M \rightarrow \infty} s_1$

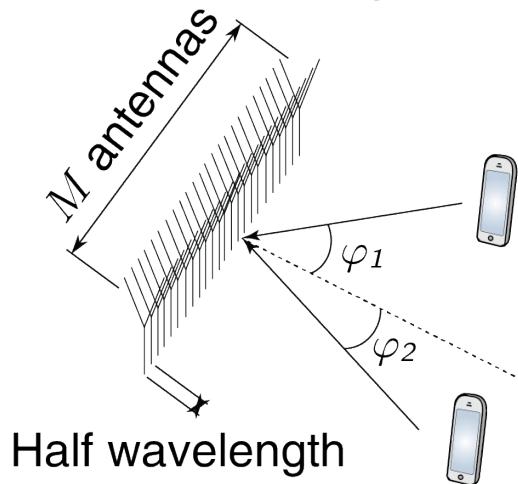
# Is this Result Limited to Isotropic Fading?

- Assumptions in i.i.d. Rayleigh Fading
  - No dominant directivity
  - Very many scattering objectives

Less true as  $M \rightarrow \infty$

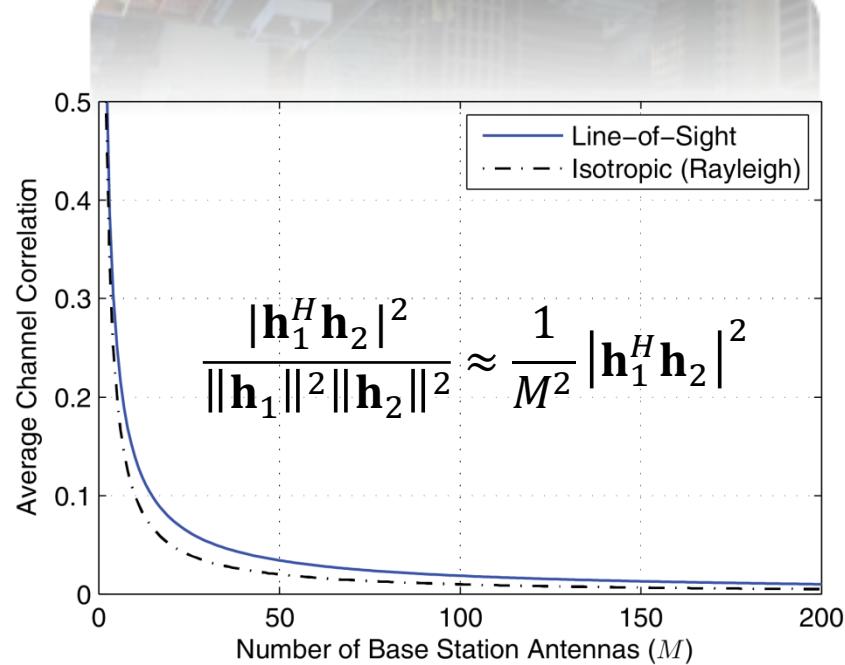


- Example: Line-of-Sight Propagation



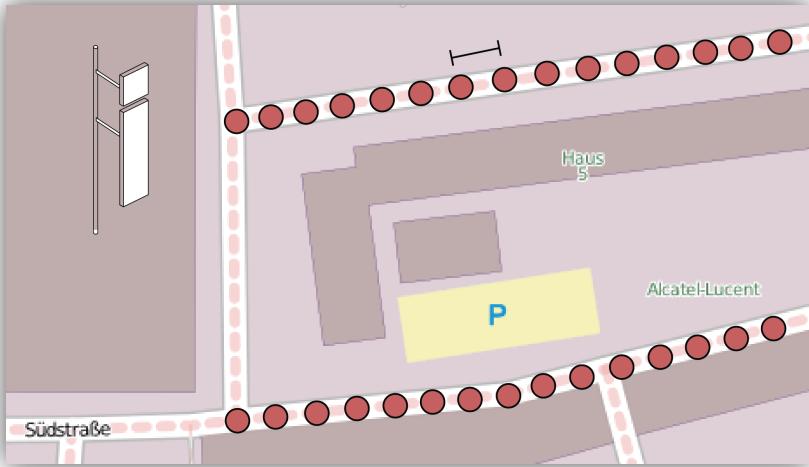
- Uniform linear array
- Random user angles
- $M$  observations:
  - Stronger signal
  - Suppressed noise
- What is  $\mathbf{h}_1^H \mathbf{h}_2 \rightarrow ?$

**Only difference:**  
How quickly interference is suppressed



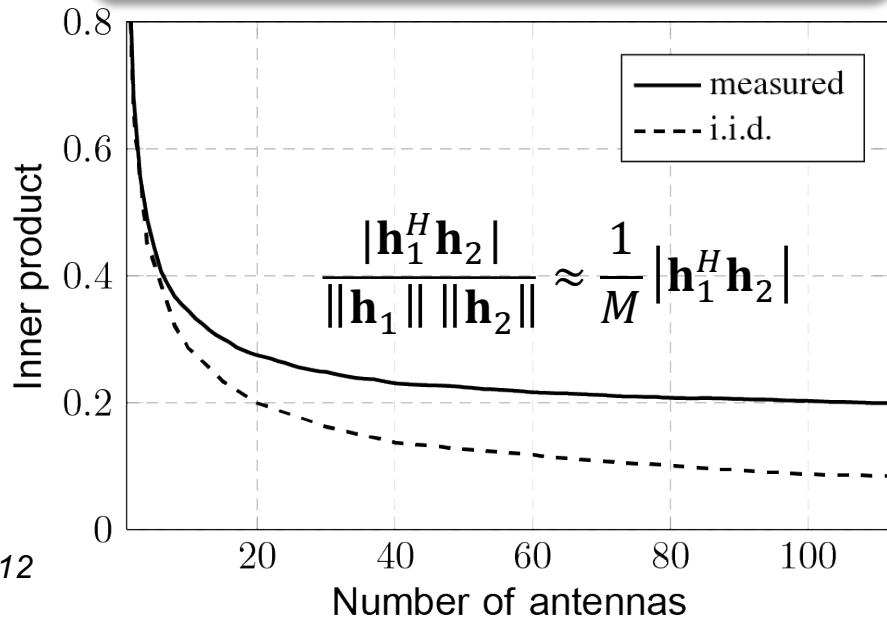
# How will Practical Channels Behave?

- Measurements show similar results



Source: J. Hoydis, C. Hoek, T. Wild, and S. ten Brink,  
"Channel Measurements for Large Antenna Arrays," ISWCS 2012

**Spectral Efficiency**  
Only 10-20% lower than i.i.d. fading



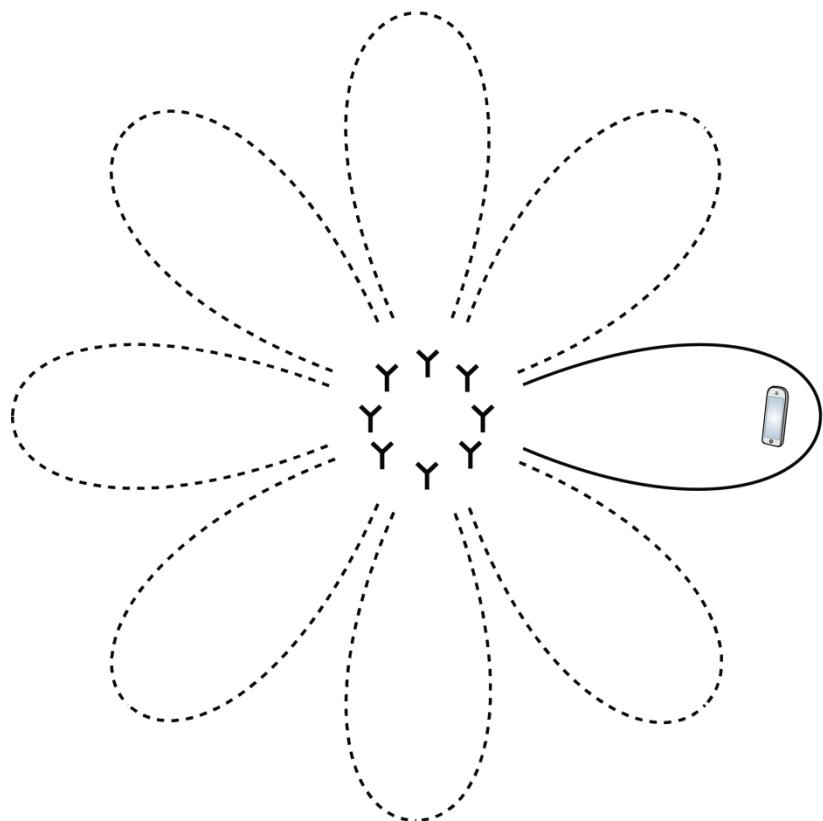
- Asymptotic Favorable Propagation:  $\frac{1}{M} \mathbf{h}_1^H \mathbf{h}_2 \rightarrow 0$  as  $M \rightarrow \infty$ 
  - Achieved in Rayleigh fading and line-of-sight – two extremes!
  - Same behavior expected and seen in practice

Massive MIMO

# **TRANSMISSION PROTOCOL**

# MIMO Precoding

Same principles for  
MIMO detection



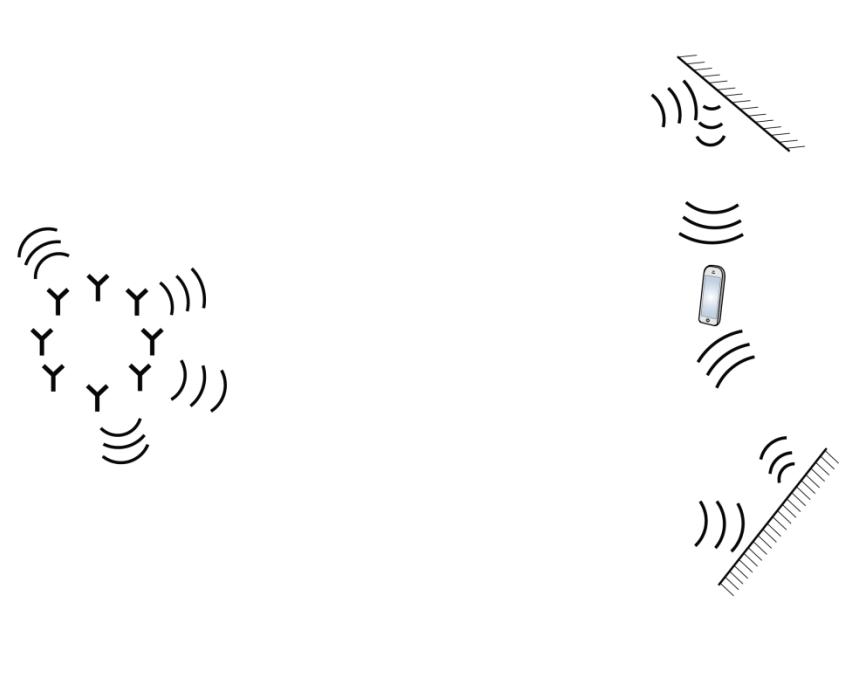
## **Line-of-Sight**

Channels determined by angles

1-2 parameters to estimate per user

Precoding = Beamforming

**Easy: Codebooks can be used**



## **Non-Line-of-Sight**

Rich multipath propagation

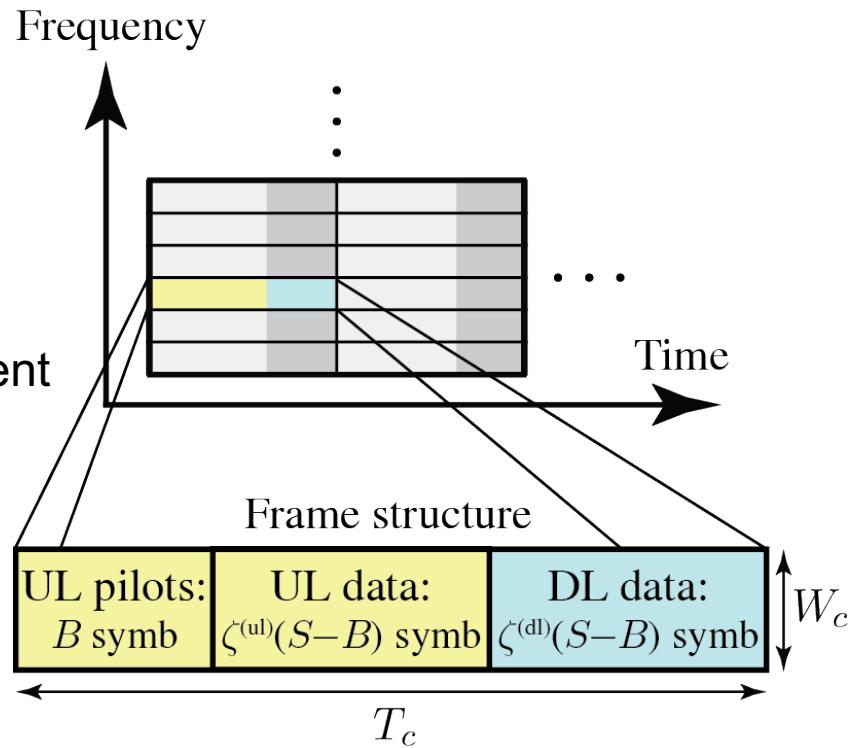
$M$  parameters to estimate per user

Precoding  $\neq$  Beamforming

**Hard: Requires pilots!**

# Transmission Protocol

- Coherence Blocks
  - Fixed channel responses
  - Coherence time:  $T_c$  s
  - Coherence bandwidth:  $W_c$  Hz
  - Depends on mobility and environment
  - Block length:  $S = T_c W_c$  symbols
  - Typically:  $S \in [100, 10000]$
- Time-Division Duplex (TDD)
  - Switch between downlink and uplink on all frequencies
  - $B$  symbols/block for uplink pilots – to estimate channel responses ( $B \geq K$ )
  - $S - B$  symbols/block for uplink and/or downlink payload data



# Linear versus Non-linear Processing

- Capacity-Achieving Non-linear Processing
  - Downlink: Dirty paper coding
  - Uplink: Successive interference cancellation

Do we need it in  
Massive MIMO?

## Linear Processing

Bad when  $M \approx K$

Good when  $M/K > 2$

Relative low complexity

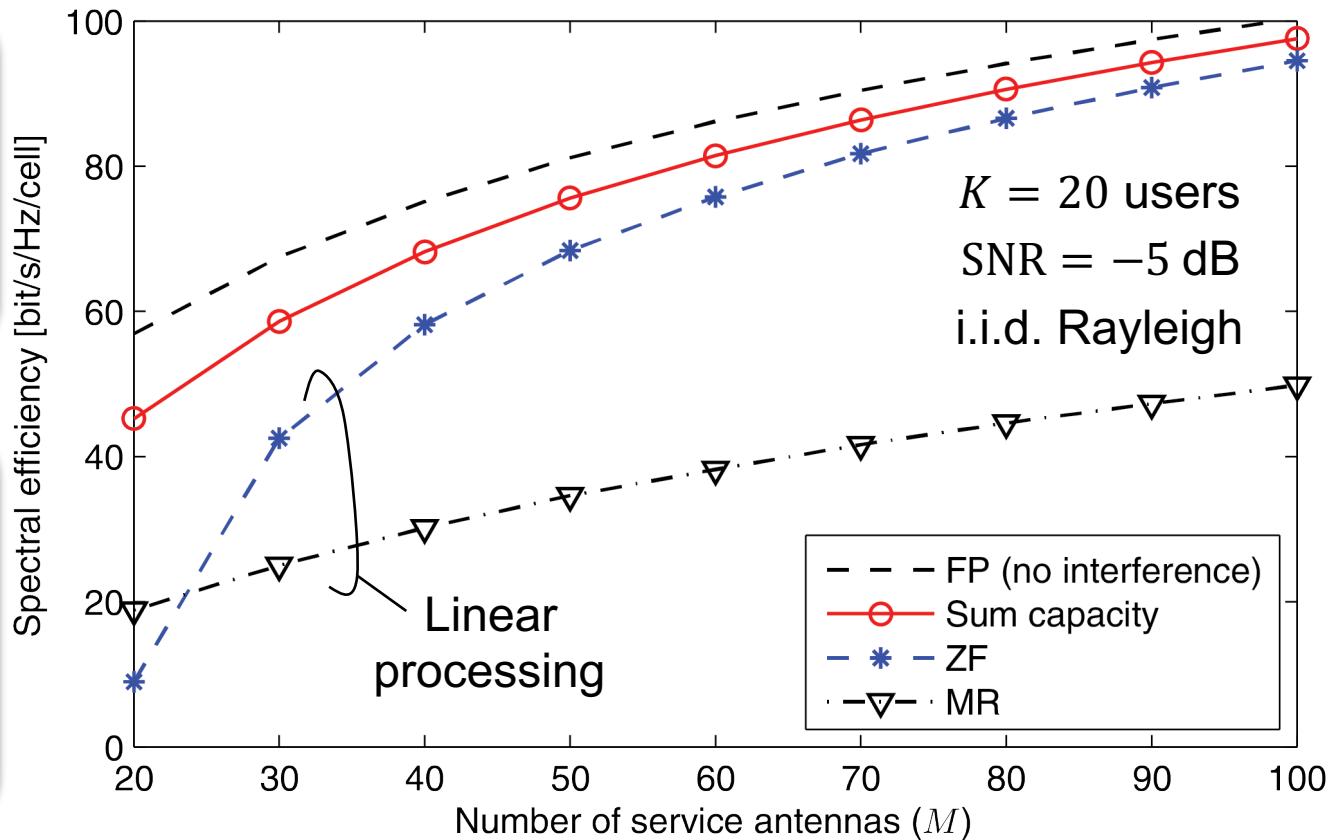
## Massive MIMO

Uses linear processing:

Maximum ratio (MR)

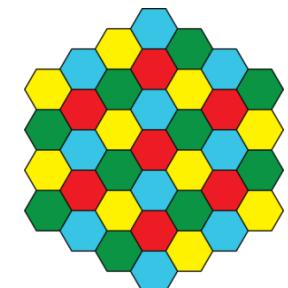
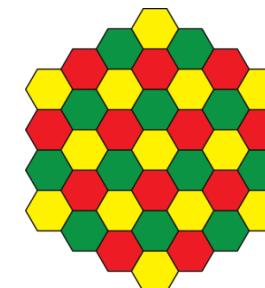
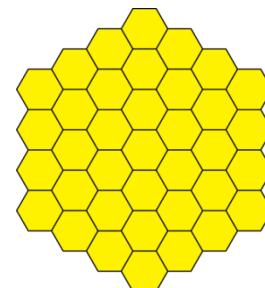
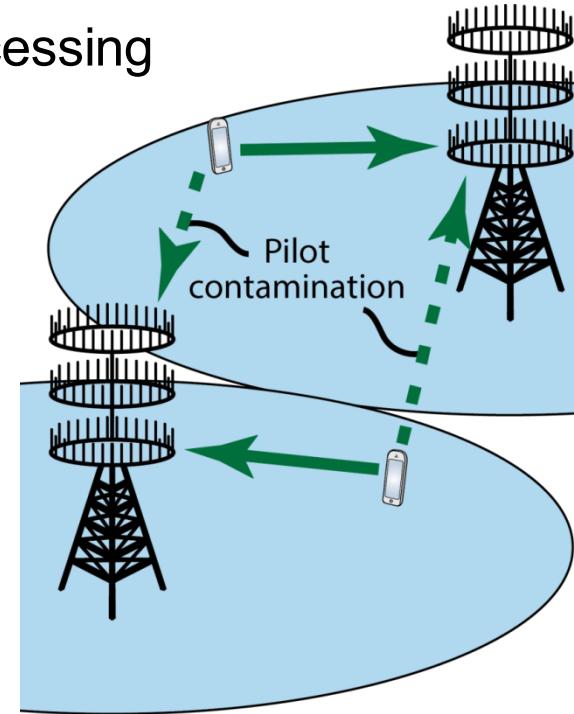
Zero-forcing (ZF)

Optimal: MMSE



# Channel Acquisition in Massive MIMO

- BS Needs Channel Responses for Linear Processing
  - Estimate using uplink pilot symbols
  - Only  $B$  pilot symbols available ( $B \leq S$ )
  - Must use same pilot symbols in different cells
  - BSs cannot tell some users apart
- Called: Pilot Contamination
  - Recall: Noise and interference vanish as  $M \rightarrow \infty$
  - Not interference between users with same pilot!
- Solution: Select how often pilots are reused
  - Pilot reuse factor  $\beta \geq 1$
  - Users per cell:  $K = \frac{B}{\beta}$
  - Higher  $\beta \rightarrow$  Fewer users per cell, but interferers further away



# Intuitive Spectral Efficiency Expressions

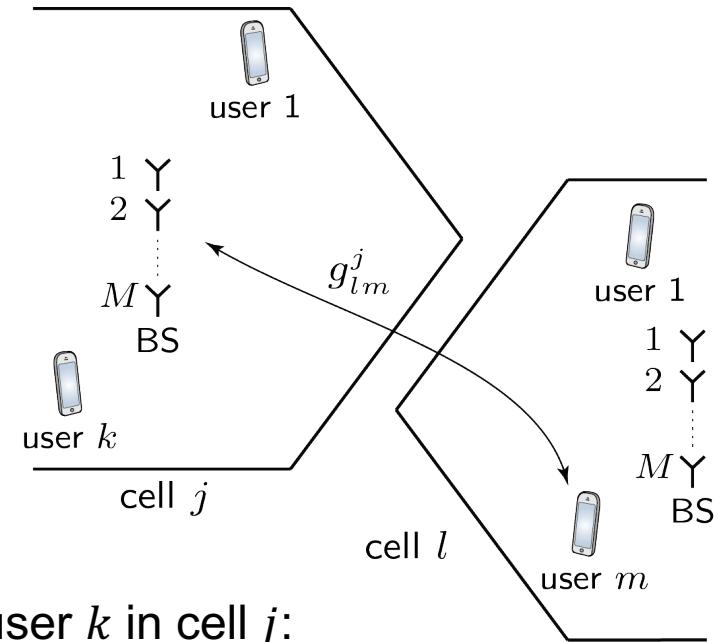
- Simple Performance Expressions

- No small-scale fading, only gain  $g_{lm}^j$
- Depends on transmit powers:  $\rho_{jk}^u, \rho_{jk}^p$
- Depends on estimation quality:

$$\gamma_{lk}^j = \frac{\rho_{lk}^p g_{lk}^j}{\sum_{l' \in \mathcal{P}_l} \rho_{l'k}^p g_{l'k}^j + 1}$$

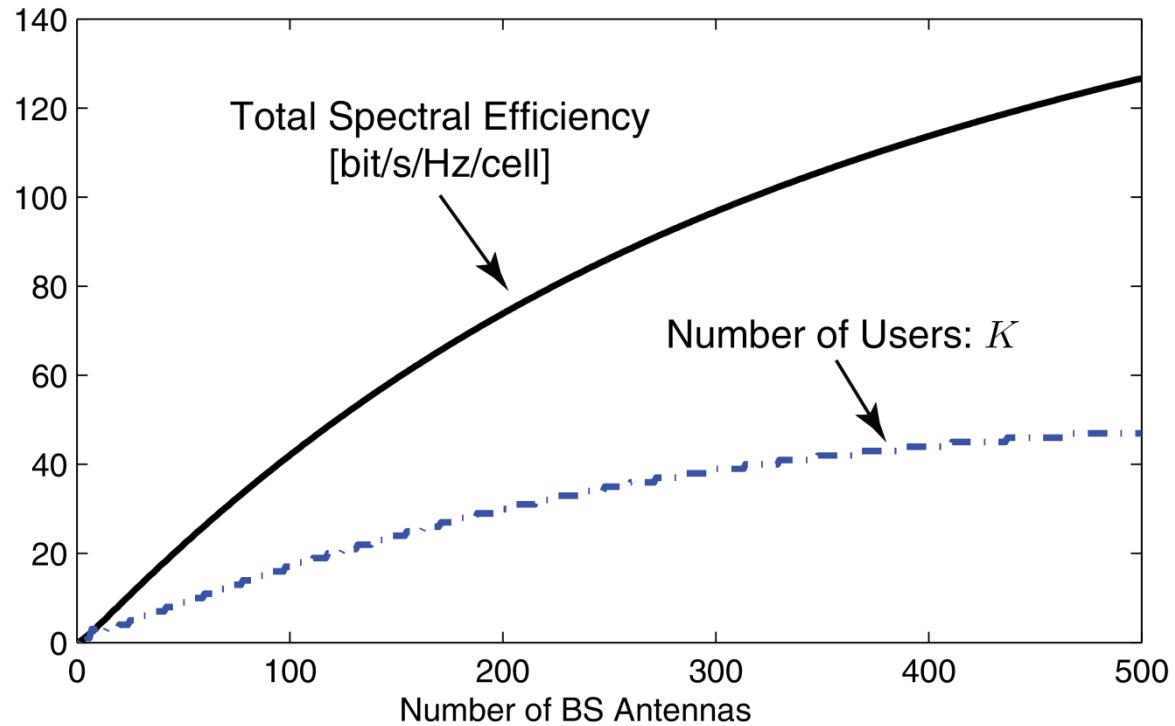
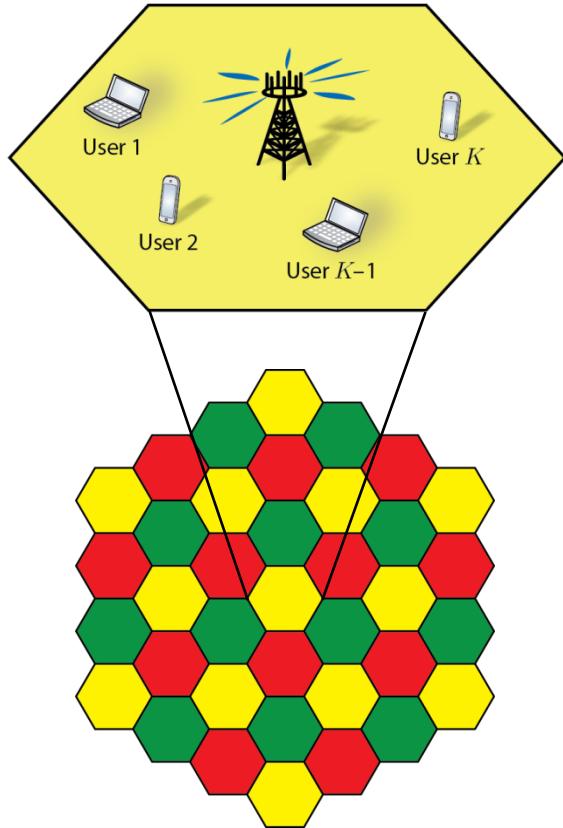
- Ergodic spectral efficiency with MR for user  $k$  in cell  $j$ :

$$R_{jk} = \underbrace{\left(1 - \frac{\beta K}{S}\right)}_{\text{Pilot overhead}} \log_2 \left( 1 + \frac{\underbrace{M \rho_{jk}^u g_{jk}^j \gamma_{jk}^j}_{\text{Desired signal}}}{\underbrace{\sum_{l,m} \rho_{lm}^u g_{lm}^j}_{\text{Conventional interference}} + \underbrace{M \sum_{l \in \mathcal{P}_j \setminus \{j\}} \rho_{lk}^u g_{lk}^j \gamma_{lk}^j}_{\text{Pilot-contaminated interference}} + 1} \right)$$



**Similar expressions for downlink and with ZF processing**

# How Much can Spectral Efficiency be Improved?



## Uplink Simulation

LTE-like system parameters

Coherence block:  $S = 500$

SNR 5 dB, i.i.d. Rayleigh

ZF and  $\beta = 3$

## Observations

- Baseline: 2.25 bit/s/Hz/cell (IMT-Advanced)
- Massive MIMO,  $M = 100$ : x20 gain ( $M/K \approx 6$ )
- Massive MIMO,  $M = 400$ : x50 gain ( $M/K \approx 9$ )
- Per scheduled user:  $\approx 2.5$  bit/s/Hz

# **4 MYTHS AND MISCONCEPTIONS**

# Massive MIMO Relies on Asymptotic Results

- No! Accurate theory for any  $M$

- **Example:**

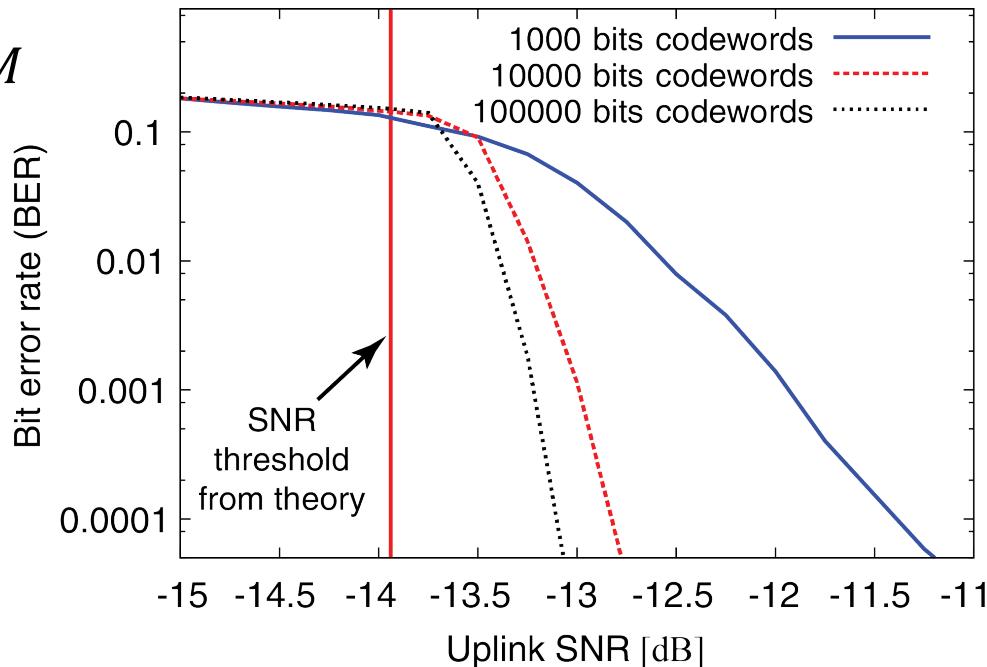
- $M = 100, K = 30$

- QPSK with  $\frac{1}{2}$ -LDPC code

- Total: 30 bit/s/Hz

- **Reality:**

- Rate expressions reached at modest codeword lengths



## Signal Processing Complexity is Overwhelming

- **Reality:** It is higher, but manageable:
  - Most processing can be parallelized per antenna (e.g., FFTs, channel estimation, precoding/detection of data)
  - Not parallelized: Computing ZF/MMSE matrix inversion, but:
    - Not the main complexity (happens only  $1/S$  of the time)
    - Good inversion approximations (diagonal-dominant matrices)

# We Need Orders of Magnitude More Antennas than Users

- No! It all depends on the goal

- **Example:**

$$M = 100, S = 200$$

SNR =  $-5$  dB from own BS

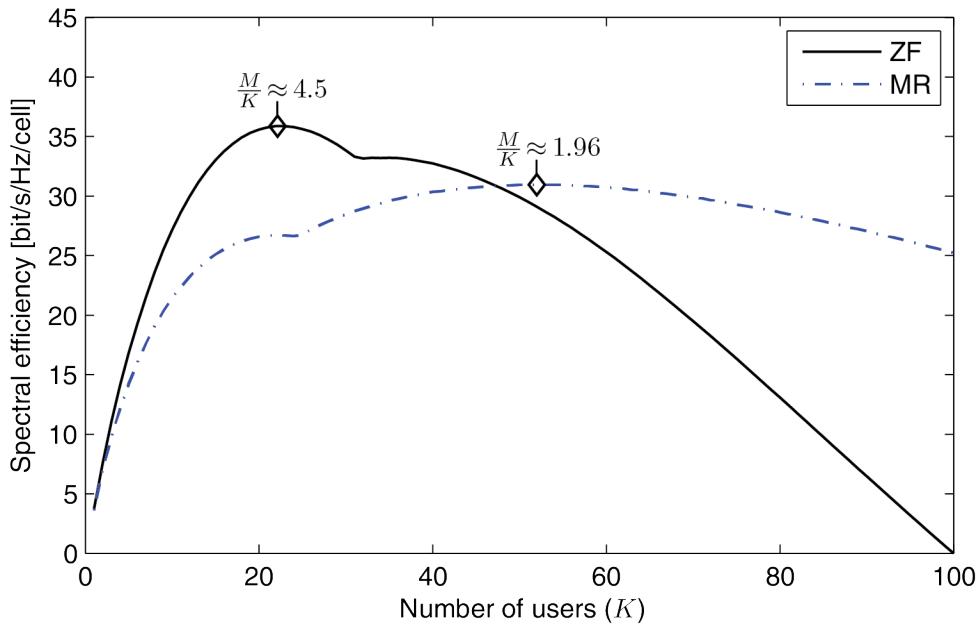
- **Reality:**

Any  $M/K > 2$  is desirable

Choose between:

Many or few users  $\rightarrow$

Low or high rates/user



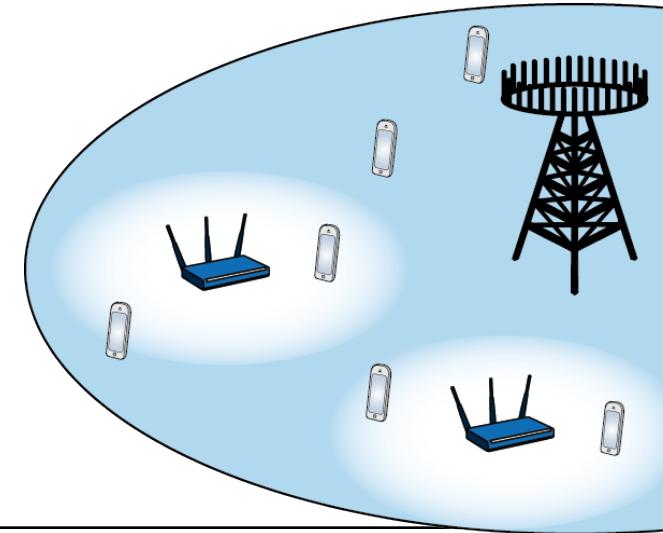
## Resource Allocation is Impossible with so Many Antennas

- **Classically:** Allocate time/frequency blocks based on current fading
- **Reality:** Not needed in Massive MIMO!
  - Small-scale fading does not impact channel quality
  - Everyone can get the whole bandwidth whenever needed!
  - Remaining issue: Power control, but can be handled as a convex problem

# **RESEARCH TRENDS AND OPEN QUESTIONS**

# Research Trends and Open Questions

- Coexistence with Other Technologies
    - How to balance traffic load over BS types?
    - Can it tolerate underlaying (e.g., D2D)?
    - Is TDD time synchronization manageable?
    - Are mmWave frequencies suitable?



- Implementation-Based Hardware and Algorithmic Design
    - Transceiver hardware is imperfect and affects the system:



- Fact: Massive MIMO tolerates larger hardware impairments
  - How to utilize this to tailor the transceiver hardware?
  - Data shuffling is a bottleneck: Develop easily implementable algorithms

# Can Massive MIMO work in FDD mode?

- Frequency-division duplex (FDD) is used in many systems
  - Different uplink/downlink frequencies → Two-way pilots & feedback needed

## TDD versus FDD

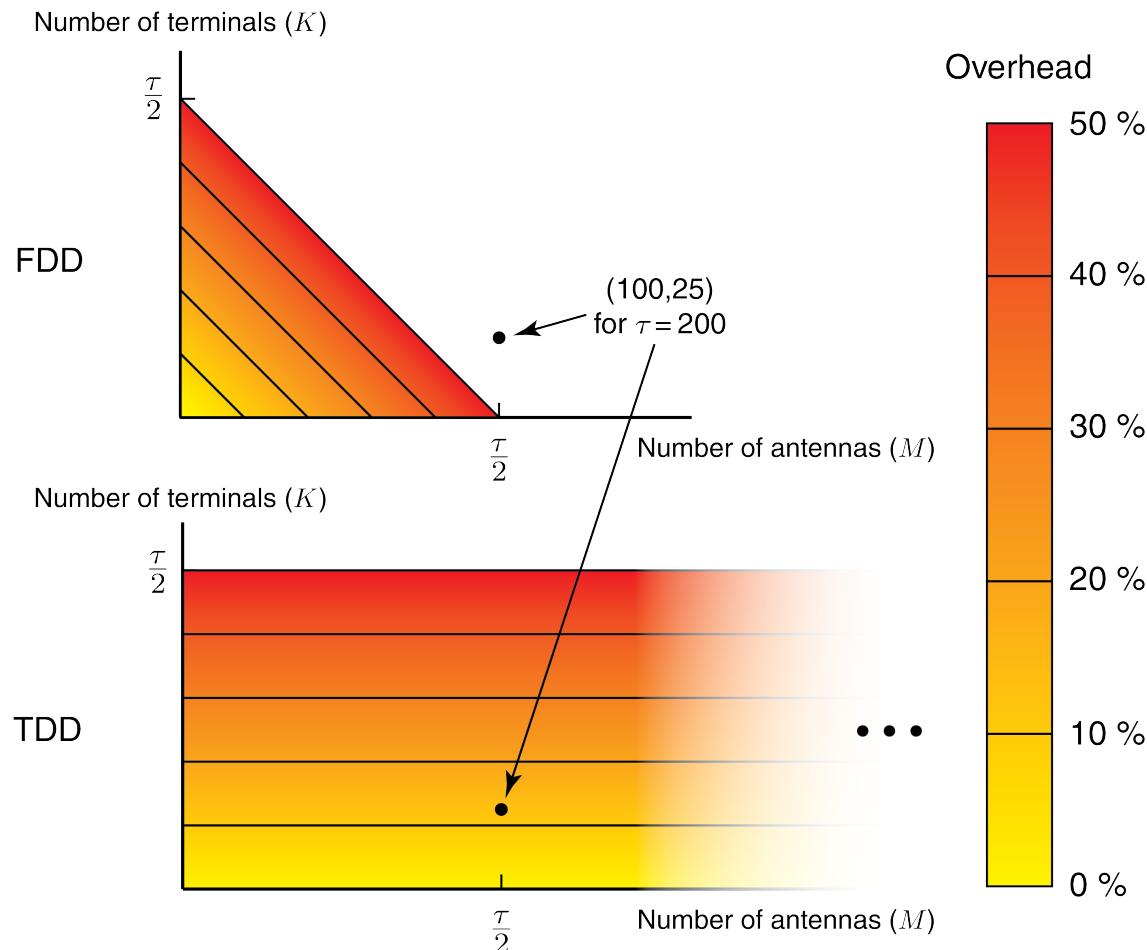
*Channel coherence limits both antennas and users in FDD, but only users in TDD*

*FDD possible with low mobility*

## Open question

*Can we reduce estimation and feedback load?*

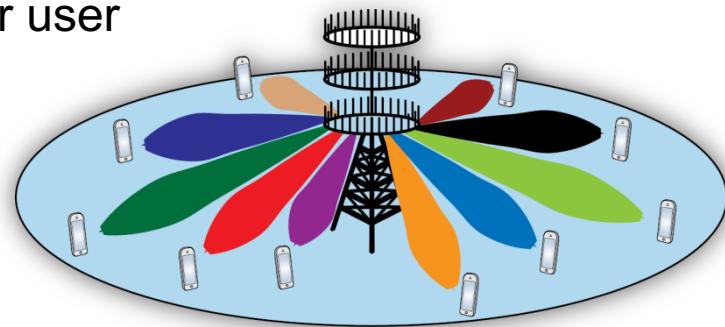
*Yes, under channel sparsity:  
Exists in line-of-sight, but probably not in general!*



# **SUMMARY**

# Summary

- Massive MIMO: The way to increase spectral efficiency in 5G networks
  - >20x gain over IMT-Advanced are foreseen
  - BSs with many small antennas and transceiver chains
  - Higher spectral efficiency per cell, not per user
  - Many potential deployment strategies
- Facts to Remember
  - Massive MIMO  $\neq$  Massive size: TV sized panels at cellular frequencies
  - Favorable propagation in most propagation environments
  - Resource allocation and processing are simplified, not complicated
- Further Reading
  - Emil Björnson, Erik G. Larsson, Thomas L. Marzetta, “*Massive MIMO: 10 Myths and One Grand Question*,” Submitted to IEEE Commun. Magazine.



# QUESTIONS?

**Dr. Emil Björnson**



**Slides and papers available online:**  
<http://www.commsys.isy.liu.se/en/staff/emibj29>

***Would you like to learn more?***

*Come to Stockholm on June 29! I give a tutorial on this topic at IEEE SPAWC 2015!*