

# Massive MIMO

Bringing the Magic of Asymptotics to Wireless Networks

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Seminar at Interdisciplinary Centre for Security, Reliability and Trust

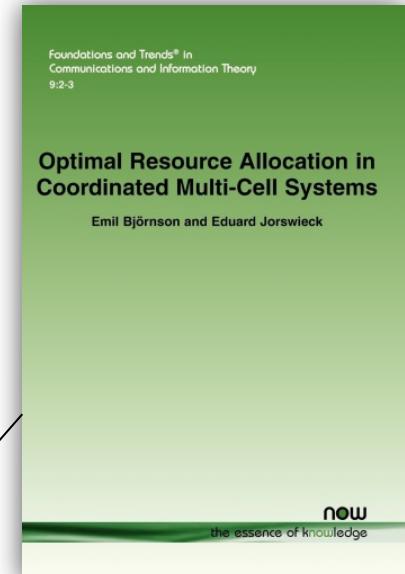
*University of Luxembourg*

*July 11, 2014*

[www.liu.se/oula](http://www.liu.se/oula)

# Biography

- 1983: Born in Malmö, Sweden
- 2007: Master of Science in Engineering Mathematics, Lund, Sweden
- 2011: PhD in Telecommunications, KTH, Stockholm, Sweden  
(Advisors: *Björn Ottersten, Mats Bengtsson*)
- 2012-2014: International Postdoc Grant Host: *Mérouane Debbah*, Supélec, Paris Home university: KTH, Sweden
- 2014: Assistant Professor (swe: Bitr. lektor)  
Division of Communication Systems,  
Electrical Engineering, Linköping University, Sweden



## ***Optimal Resource Allocation in Coordinated Multi-Cell Systems***

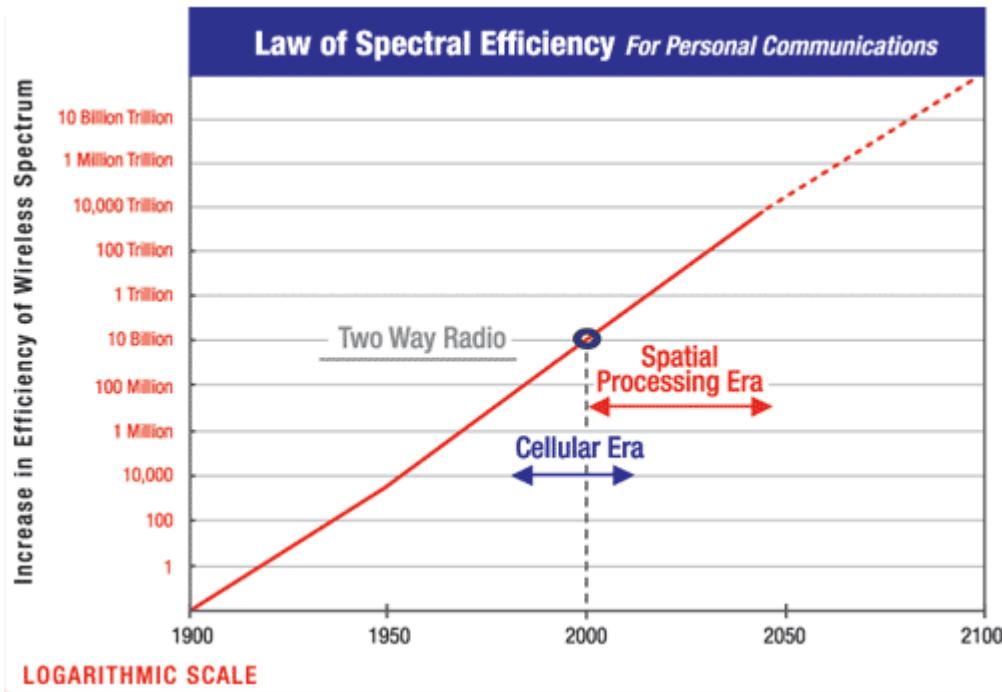
*Book by Emil Björnson, Eduard Jorswieck  
FnT in Communications and Information Theory*

Introduction

# **WHAT CAN THE PAST TELL US ABOUT THE FUTURE?**

# Incredible Success of Wireless Communications

- Last 45 years: 1 Million Increase in Wireless Traffic



Source: Personal Communications in 2025, Martin Cooper

## ***Martin Cooper's law***

*The number of simultaneous voice/data connections has doubled every 2.5 years (+32% per year) since the beginning of wireless*

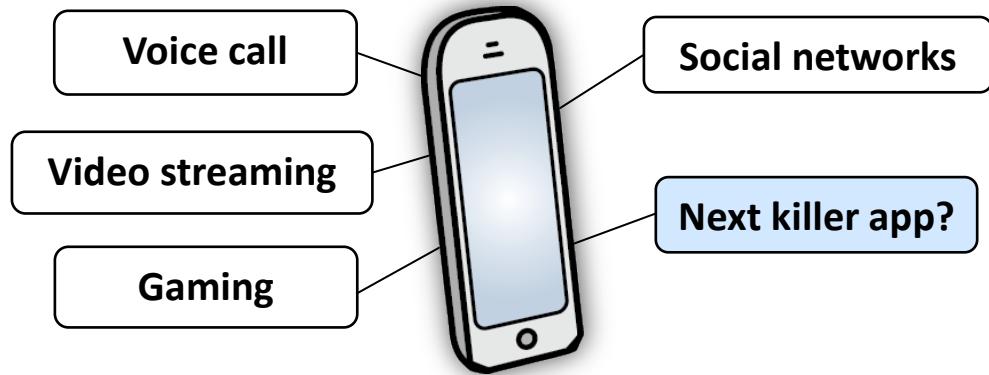


**Martin Cooper**  
Inventor of handheld cellular phones

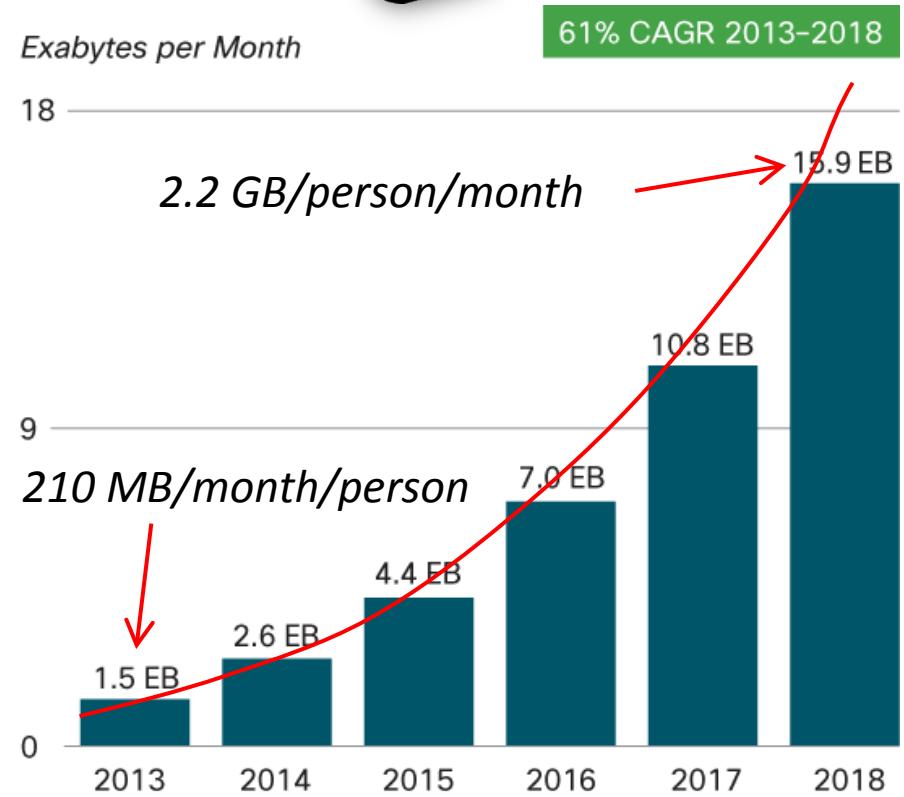
Source: Wikipedia

# Predictions for the Future

- Wireless Connectivity
  - A natural part of our lives



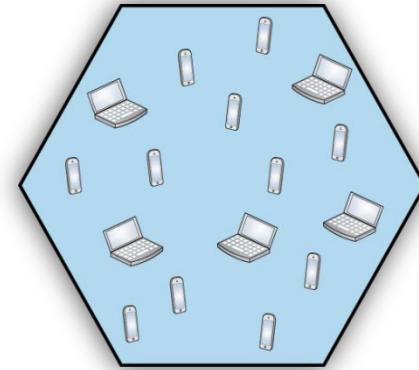
- Rapid Network Traffic Growth
  - 61% annual data traffic growth
  - Faster than in the past!
  - Exponential increase
  - Extrapolation: 20x until 2020  
200x until 2025  
2000x until 2030



# Evolving Networks for Higher Traffic

- Increase Network Throughput [bit/s]

- Consider a given area



- Formula for Network Throughput:

$$\frac{\text{Throughput}}{\text{bit/s in area}} = \frac{\text{Available spectrum}}{\text{in Hz}} \cdot \frac{\text{Cell density}}{\text{Cell/Area}} \cdot \frac{\text{Spectral efficiency}}{\text{bit/s/Hz/Cell}}$$

- Ways to achieve 1000x improvement:

	More spectrum	Higher cell density	Higher spectral efficiency
Nokia (2011)	10x	10x	10x
SK Telecom (2012)	3x	56x	6x

New regulations,  
cognitive radio,  
higher frequencies

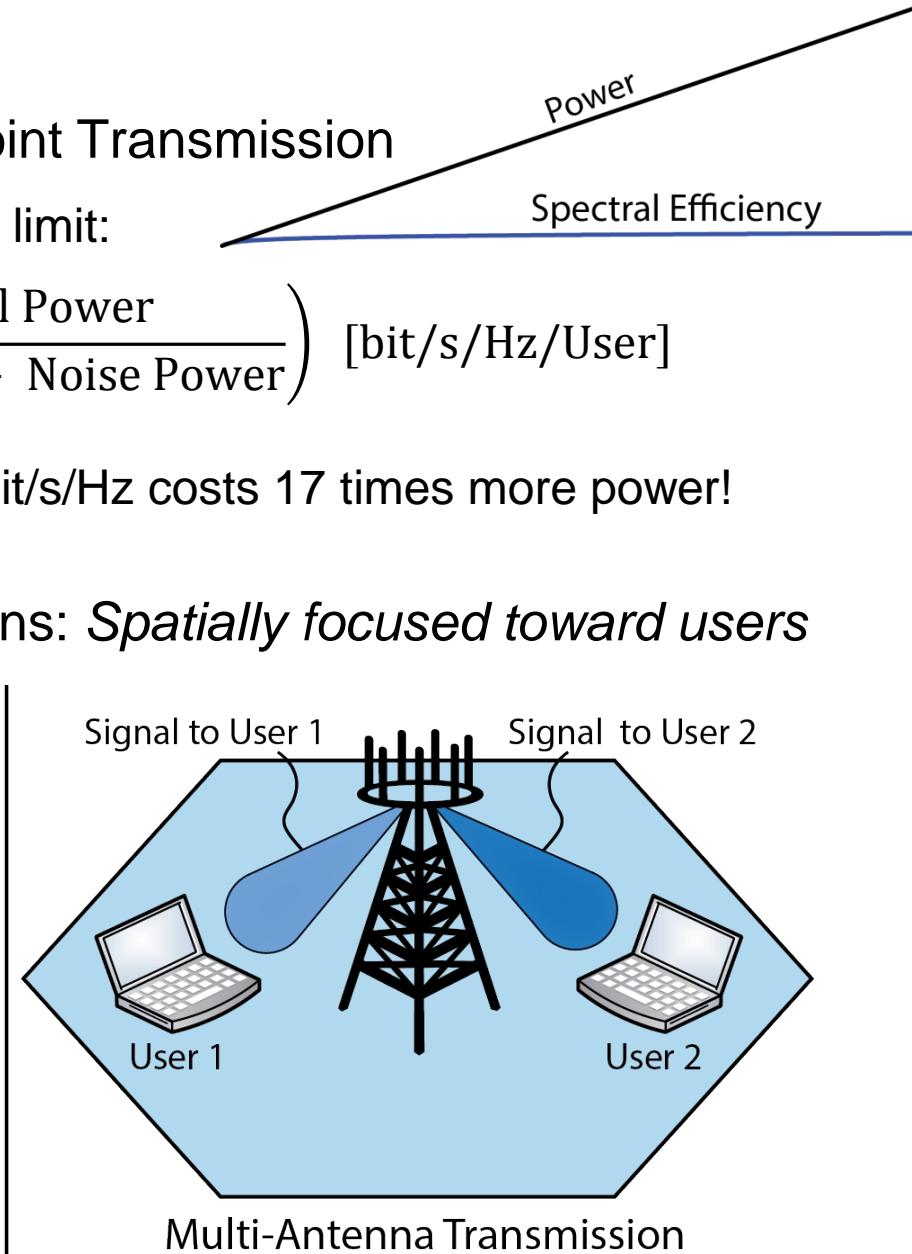
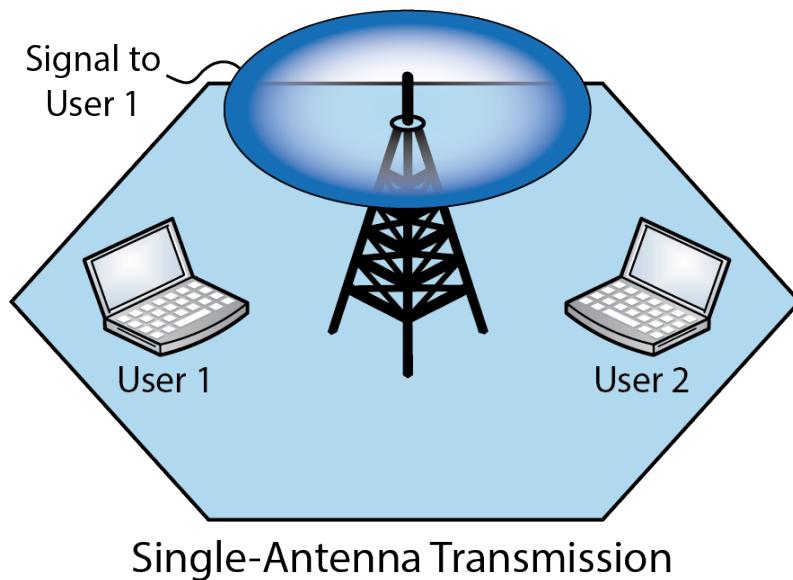
Smaller cells,  
heterogeneous  
deployments

**Massive MIMO**  
*(Topic of this seminar)*  
?x

Introduction to  
**MASSIVE MIMO**

# Higher Spectral Efficiency

- Spectral Efficiency of Point-to-Point Transmission
  - Governed by Shannon's capacity limit:
$$\log_2 \left( 1 + \frac{\text{Received Signal Power}}{\text{Interference Power} + \text{Noise Power}} \right) \text{ [bit/s/Hz/User]}$$
  - Cannot do much: 4 bit/s/Hz → 8 bit/s/Hz costs 17 times more power!
- Many Simultaneous Transmissions: *Spatially focused toward users*



# Multi-User MIMO (Multiple-input Multiple-output)

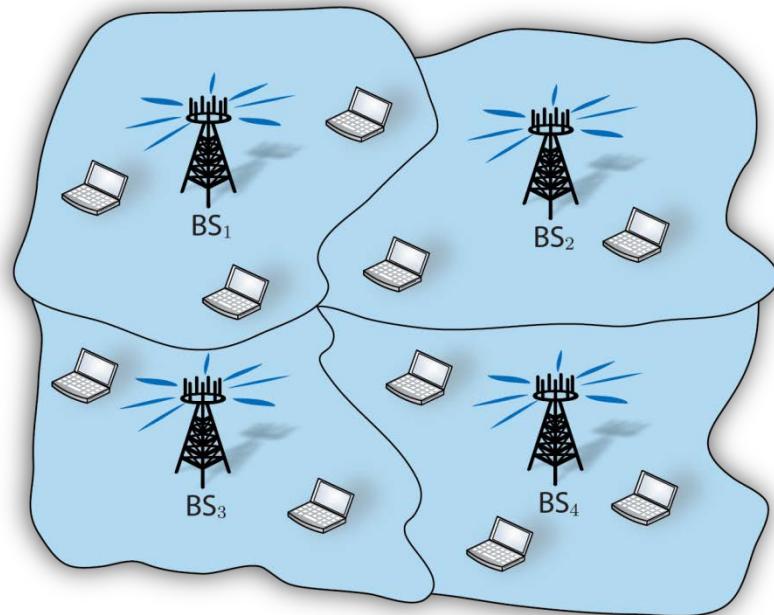
- Multi-Cell Multi-User MIMO
  - Base stations (BSs) with  $N$  antennas
  - Parallel uplink/downlink for  $K$  users
  - Channel coherence interval:  $T$  symbols
- Theory: Hardware is Limiting
  - Spectral efficiency roughly prop. to

$$\min\left(N, K, \frac{T}{2}\right)$$

- 2x improvement = 2x antennas and users (since  $T \in [100,10000]$ )

- Practice: Interference is Limiting

- Multi-user MIMO in LTE-A: Up to 8 antennas
- Interference since:
  - Hard to learn users' channels
  - Hard to coordinate BSs



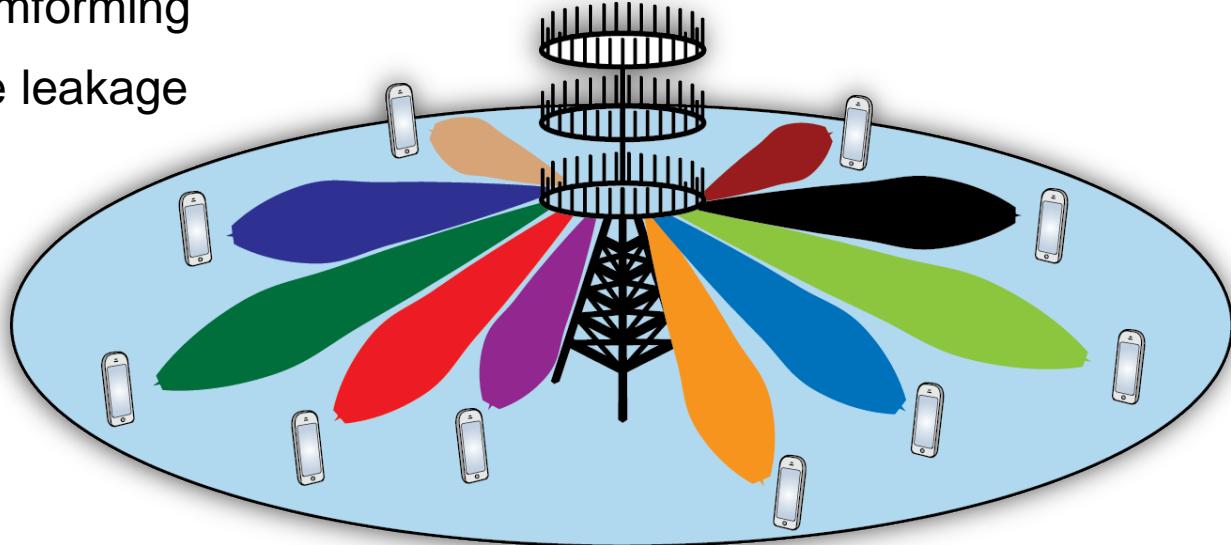
**End of MIMO road?**  
No reason to add  
more antennas/users?

# Taking Multi-User MIMO to a New Level

- Network Architecture: Massive MIMO
  - Use large arrays at BSs; e.g.,  $N \approx 200$  antennas,  $K \approx 40$  users
  - Key: Excessive number of antennas,  $N \gg K$
  - Very narrow beamforming
  - Little interference leakage

*Spectral efficiency prop.  
to number of users!*

$$\min\left(N, K, \frac{T}{2}\right) \approx K$$



- 2013 IEEE Marconi Prize Paper Award

Thomas Marzetta, “*Noncooperative Cellular Wireless with Unlimited Numbers of Base Station Antennas*,” IEEE Trans. Wireless Communications, 2010.

- Analytic assumption:  $N \rightarrow \infty$

# What is the Key Difference?

- Number of Antennas?
  - 3G/UMTS: 3 sectors x 20 element-arrays = 60 antennas
  - 4G/LTE-A: 4-MIMO x 60 = 240 antennas
- We Already have Many Antennas!

*Typical vertical array:*

*10 antennas x 2 polarizations*

*Only 1-2 antenna ports*



## Massive MIMO Characteristics

*Active antennas: Many antenna ports*

*Coherent flexible beamforming*

*Multi-user MIMO with many users*

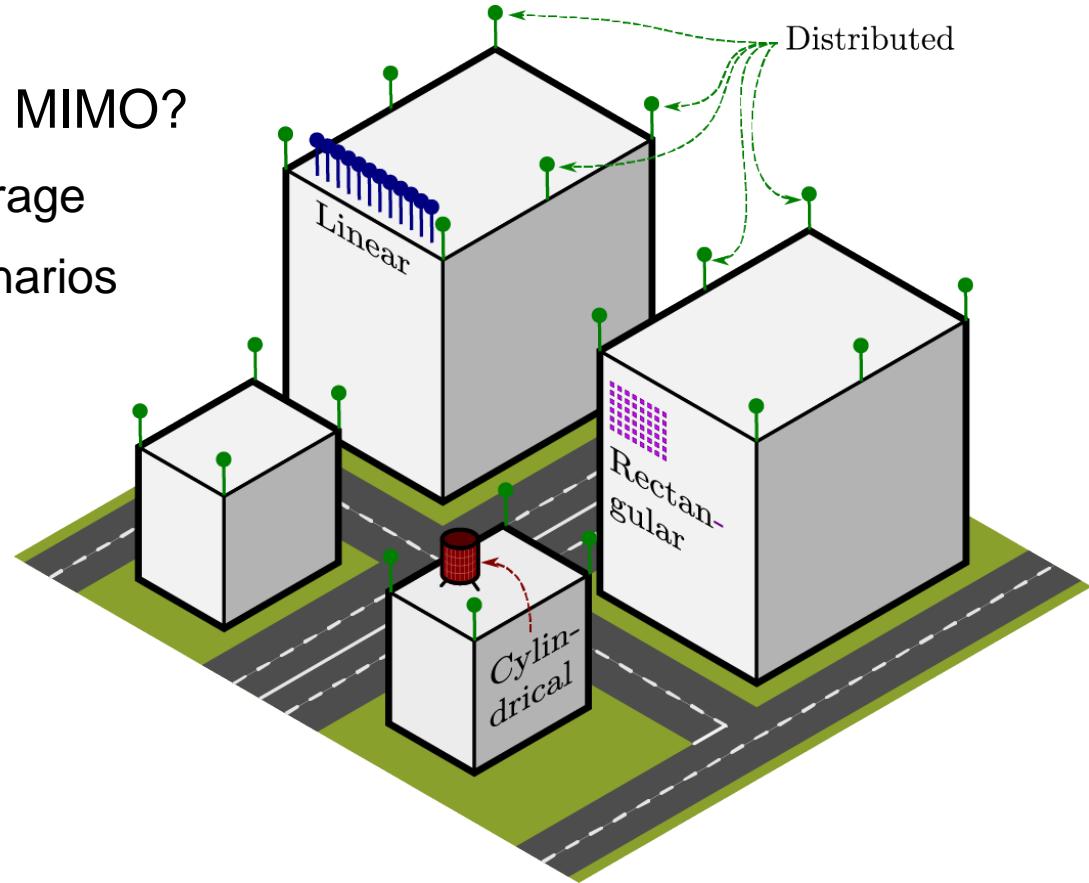


*3 sectors, 4 vertical arrays per sector*

*Image source: gigaom.com*

# Massive MIMO Deployment

- When to Deploy Massive MIMO?
  - Improve wide-area coverage
  - Special superdense scenarios
- Co-located Deployment
  - 1D, 2D, or 3D arrays
  - One or multiple sectors
- Distributed Deployment
  - Remote radio heads
  - Cloud RAN



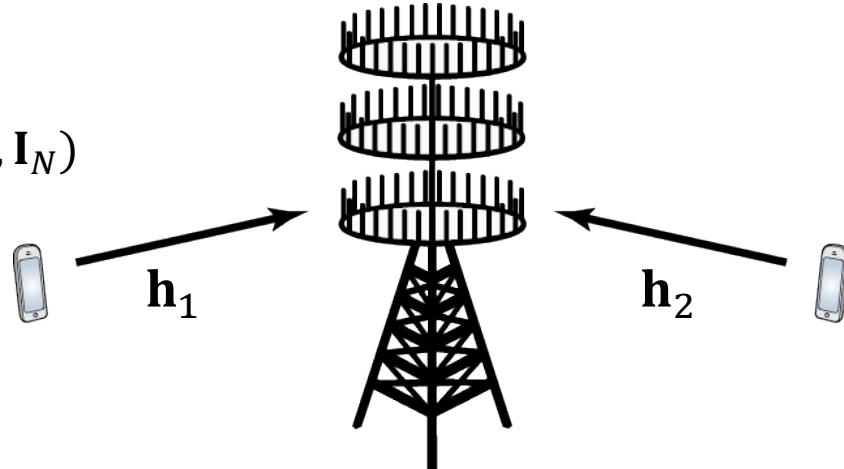
Basic Motivation

# ASYMPTOTIC PROPERTIES

# Asymptotic Channel Orthogonality

- Example: Uplink Transmission

- Two users channels:  $\mathbf{h}_1, \mathbf{h}_2 \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_N)$
- Signals:  $s_1, s_2 \sim \mathcal{CN}(0, P)$
- Noise:  $\mathbf{n} \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_N)$
- Received:  $\mathbf{y} = \mathbf{h}_1 s_1 + \mathbf{h}_2 s_2 + \mathbf{n}$



- Linear Processing for User 1:  $\tilde{y}_1 = \mathbf{w}_1^H \mathbf{y} = \mathbf{w}_1^H \mathbf{h}_1 s_1 + \mathbf{w}_1^H \mathbf{h}_2 s_2 + \mathbf{w}_1^H \mathbf{n}$

- Matched filter:  $\mathbf{w}_1 = \frac{1}{N} \mathbf{h}_1$

- Signal remains:

$$\mathbf{w}_1^H \mathbf{h}_1 = \frac{1}{N} \|\mathbf{h}_1\|^2 \xrightarrow{N \rightarrow \infty} \mathbb{E}[|h_{11}|^2] = 1$$

- Interference vanishes:

$$\mathbf{w}_1^H \mathbf{h}_2 = \frac{1}{N} \mathbf{h}_1^H \mathbf{h}_2 \xrightarrow{N \rightarrow \infty} \mathbb{E}[h_{11}^H h_{21}] = 0$$

- Noise vanishes:

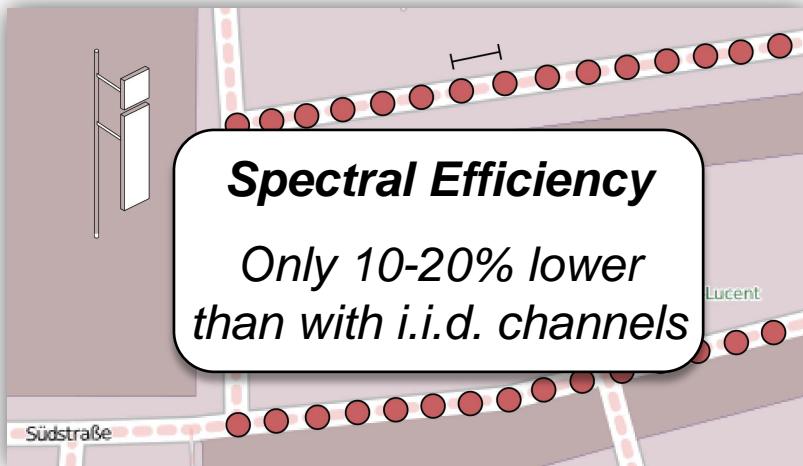
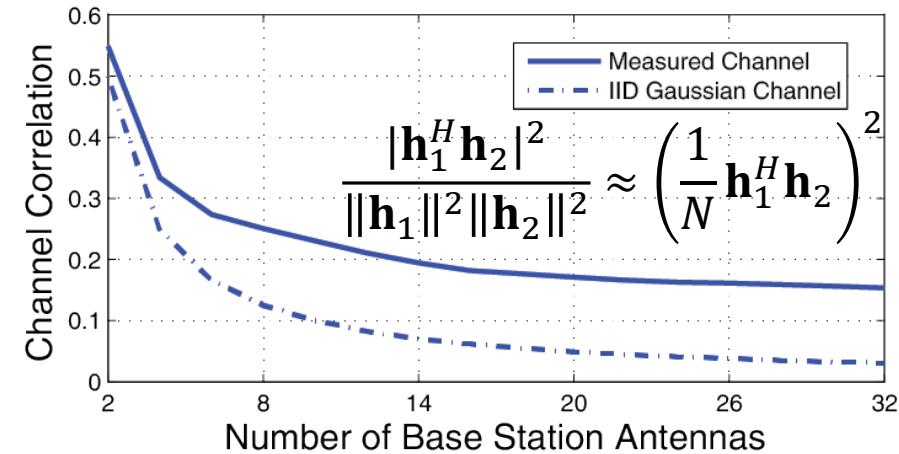
$$\mathbf{w}_1^H \mathbf{n} = \frac{1}{N} \mathbf{h}_1^H \mathbf{n} \xrightarrow{N \rightarrow \infty} \mathbb{E}[h_{11}^H n_1] = 0$$

Asymptotically noise/interference-free communication:  $\tilde{y}_1 \xrightarrow{N \rightarrow \infty} s_1$

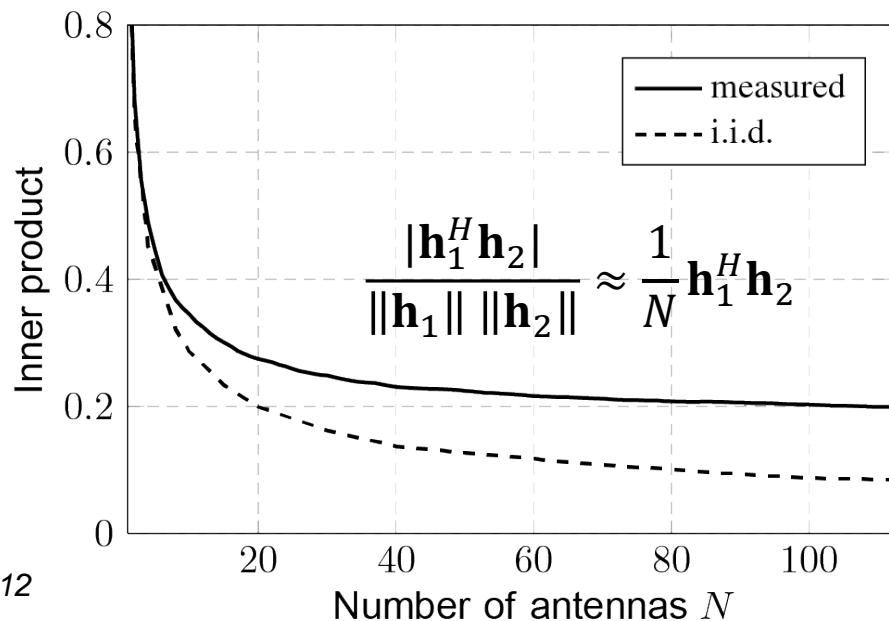
# Does This Hold for Practical Channels?

- Initial Measurements: Show similar results

Source: X. Gao, O. Edfors, F. Rusek, and F. Tufvesson, "Linear Pre-Coding Performance in Measured Very-Large MIMO Channels," VTC 2011.



Source: J. Hoydis, C. Hoek, T. Wild, and S. ten Brink, "Channel Measurements for Large Antenna Arrays," ISWCS 2012  
15



# Difference: Analysis and Measurements

- Analysis with i.i.d. Rayleigh Fading

- No line-of-sight propagation
- Many scattering objectives
- No dominant directivity

A photograph showing a dense urban skyline with numerous skyscrapers and buildings. The sky is clear with some light clouds. The buildings vary in height and architectural style, creating a complex scattering environment.

*Less true as  $N \rightarrow \infty$   
(Higher array resolution)*

- Alternative Channel Properties

- Scattering “less” rich: Other random distributions
- Spatial correlation: Directivity and user-correlation
- Line-of-sight components
- Spherical wavefronts

*Affect if  
 $\frac{1}{N} \mathbf{h}_1^H \mathbf{h}_2 \rightarrow \mathbf{0}$   
and convergence  
speed*

# Finite $N$ : Anticipated Spectral Efficiency

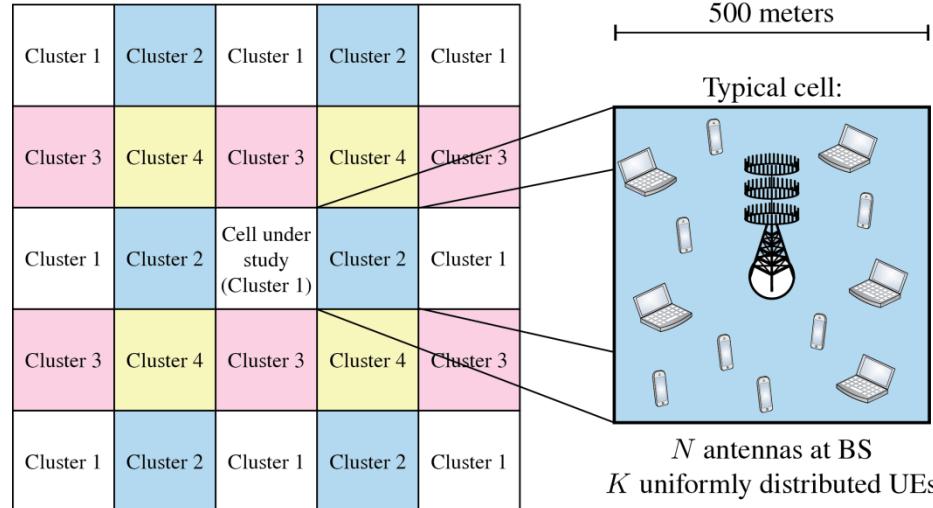
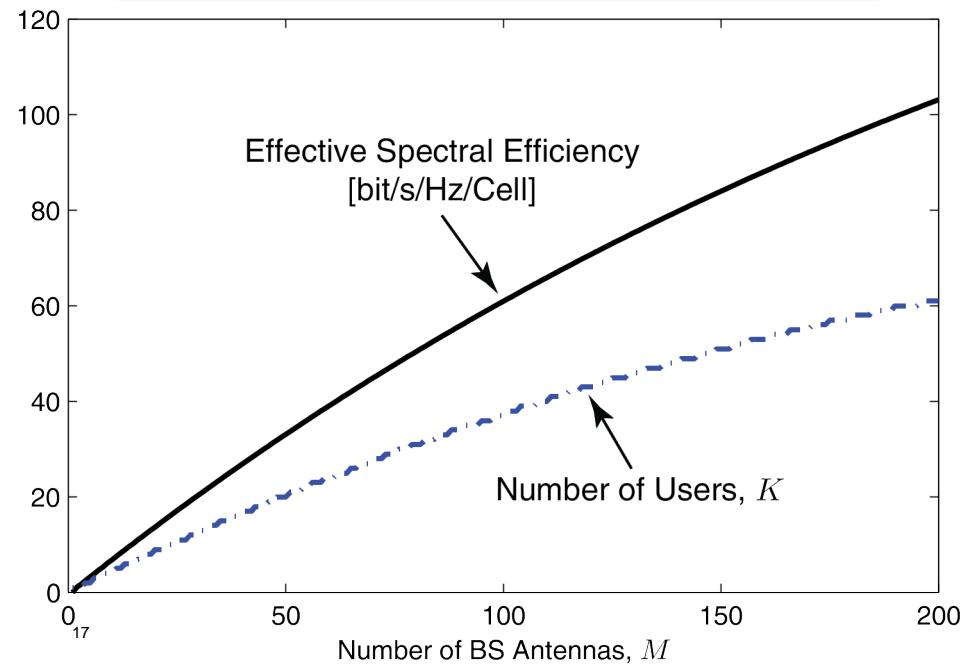
- What Might Massive MIMO Deliver?

## Simulation

LTE-like system parameters

Coherence interval:  $T = 1000$

Channels: i.i.d. Rayleigh fading



## Observations

Baseline: 3 bit/s/Hz/cell (IMT-Advanced)

Massive MIMO,  $N = 100$ : x20 gain

Massive MIMO,  $N = 200$ : x34 gain

Per scheduled user:  $\approx 2$  bit/s/Hz

Higher multiplexing gains are possible!

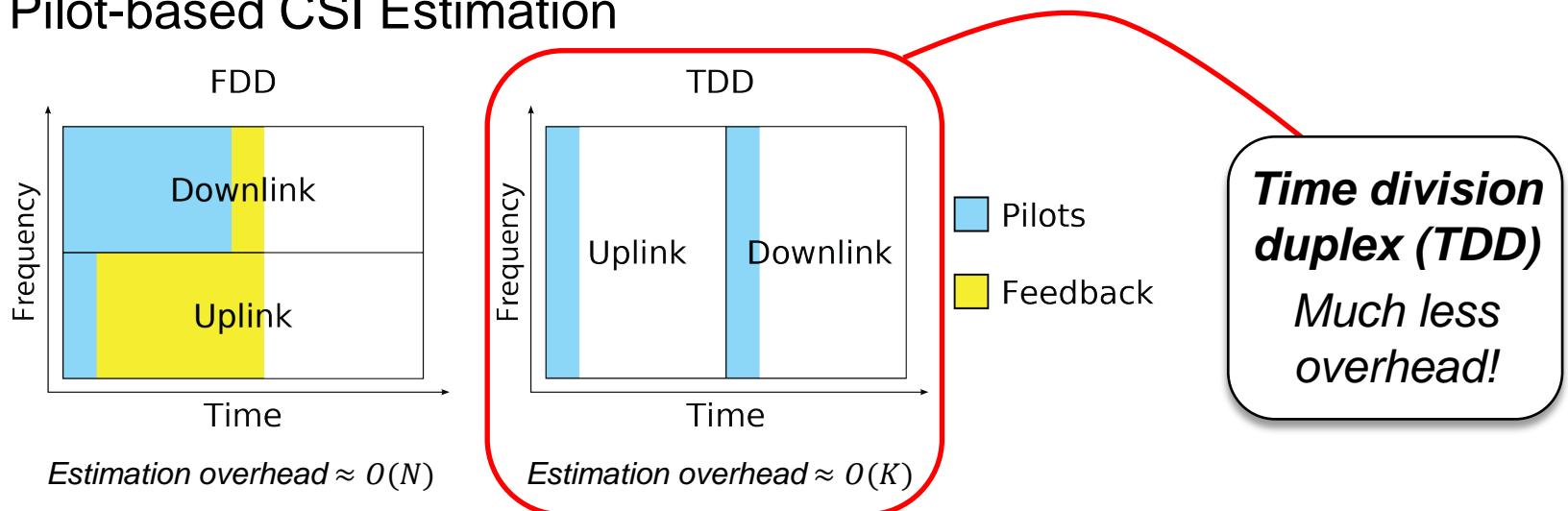
Recent and Fundamental Research Results

# **“THE MAGIC OF ASYMPTOTICS”**



# Interference Management

- Interference Vanishes as  $N \rightarrow \infty$  Using Linear Processing
  - Finite  $N$ : Reject remaining interference with zero-forcing processing
  - Requires channel state information (CSI) at BSs
- Pilot-based CSI Estimation



**Key Property:** Robustness to Interference

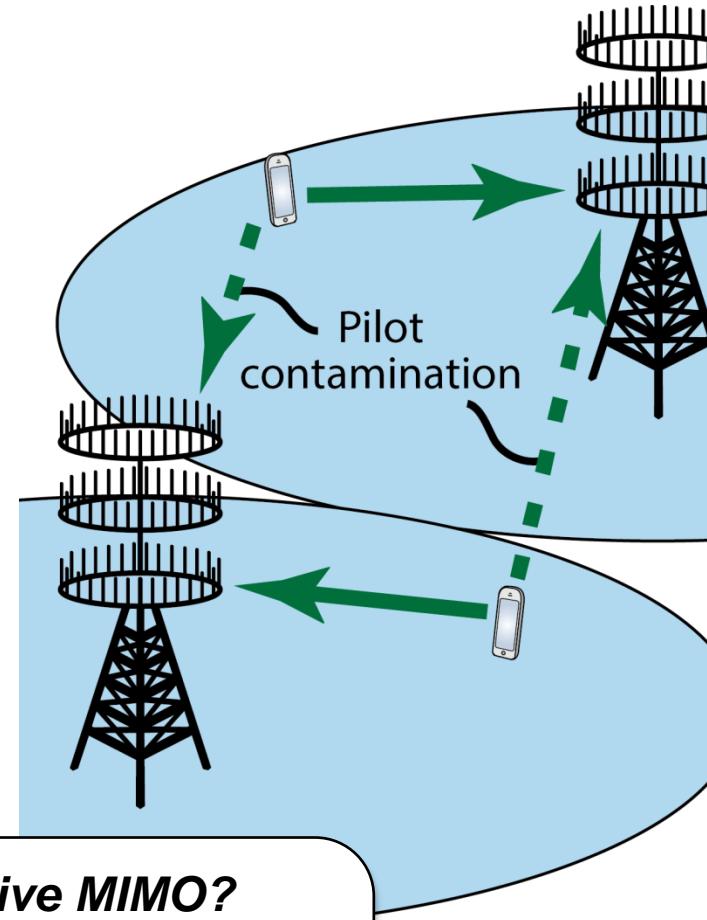
Imperfect CSI: Cannot reject all interference

Interference acts as noise: Vanishes as  $N \rightarrow \infty$



# Interference Management

- Limiting Factor: Coherence Interval  $T$ 
  - Not more than  $T$  orthogonal pilots
  - Full frequency reuse for data transmission
  - Multi-cell: Must reuse pilots across cells
- Pilot Contamination
  - BS cannot tell difference between users
  - Channel estimates are correlated
  - This interference doesn't vanish as  $N \rightarrow \infty$



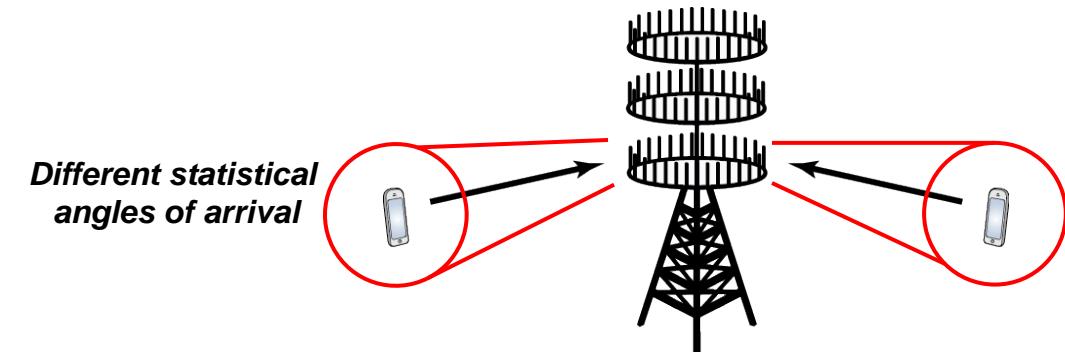
***Will Pilot Contamination Kill Massive MIMO?***

*No, but treat it with much respect!*

Make: Target SINR  $\ll \frac{\text{Pathloss}^2 \text{ from transmitter}}{\sum \text{Pathloss}^2 \text{from interferers}}$

# Interference Management

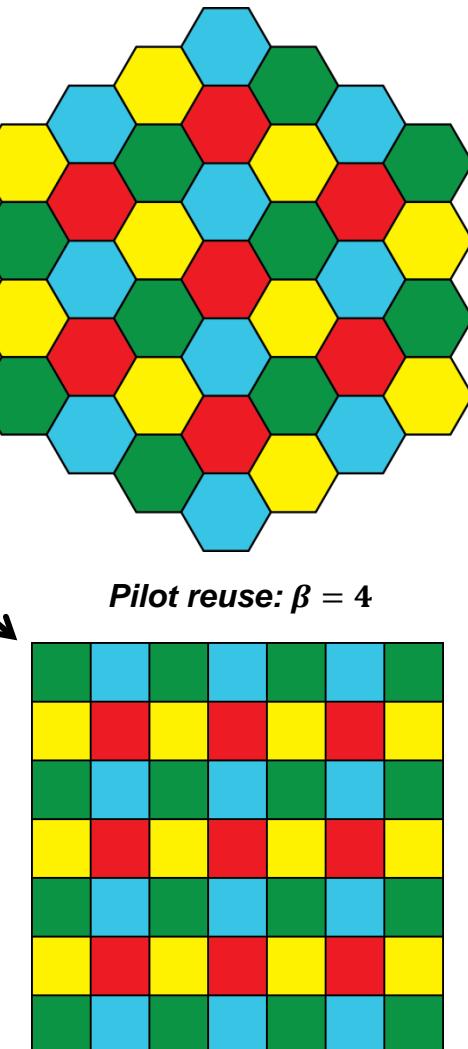
- Solution: Smart Pilot Allocation
  - Fractional pilot reuse
  - Simple: Distance-based patterns
  - Advanced: Exploit spatial correlation



**Key Property: High Area Spectral Efficiency**

$$\text{Multiplicative gain} \approx \min\left(N, K, \frac{T}{2\beta}\right) \leq \frac{T}{2\beta} \text{ per cell?}$$

Higher rates per user → Higher pilot reuse factor

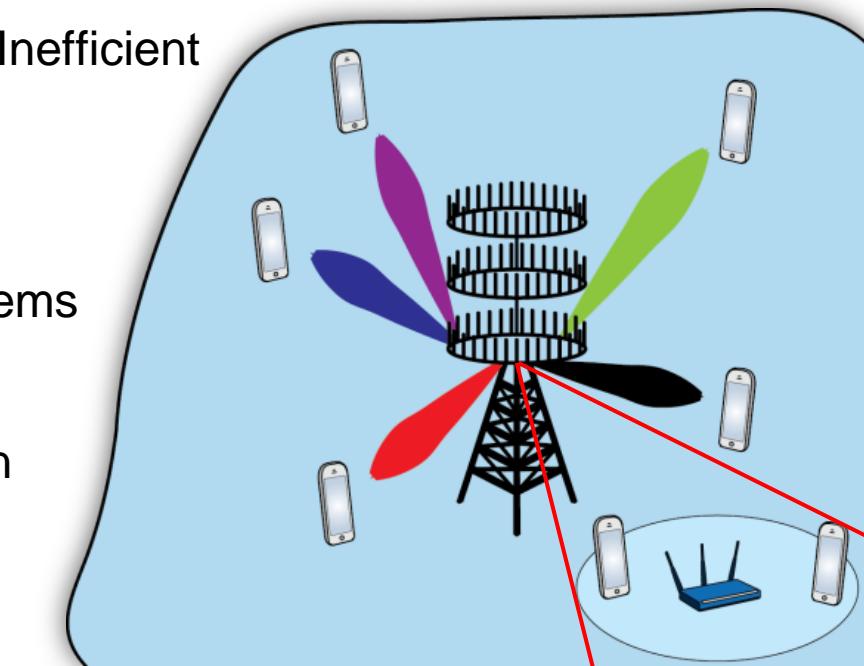


Reference: H. Huh, G. Caire, H. C. Papadopoulos, and S. A. Ramprashad, "Achieving "Massive MIMO" Spectral Efficiency with a Not-so-Large Number of Antennas," *IEEE Trans. Wireless Communications*, 2012.

H. Yin, D. Gesbert, M. Filippou, and Y. Liu, "A coordinated approach to channel estimation in large-scale multiple-antenna systems," *IEEE J. Sel. Areas Commun.*, 2013.

# Distributed Coordination with Other Systems

- Heterogeneous Deployments
  - Massive MIMO: Coverage and mobility management
  - Small cells: Small path loss → High local area throughput
- Inter-Tier Interference
  - Major limiting factor!
  - Spatial transmitter coordination ← Unreliable
  - Orthogonal in time/frequency ← Inefficient
- Cognitive Radio Approach
  - Listen: Data signals from other systems
  - Estimate: Spatial covariance matrix
  - Transmit: Orthogonal to matrix span



# Distributed Coordination with Other Systems

- TDD Coordination Protocol
  - Estimate received interference subspace
  - Transmit orthogonal to the  $M$  dominating interferers

**Fully Distributed**

*Use only local information*

*No feedback or exchange*

*Scalable!*

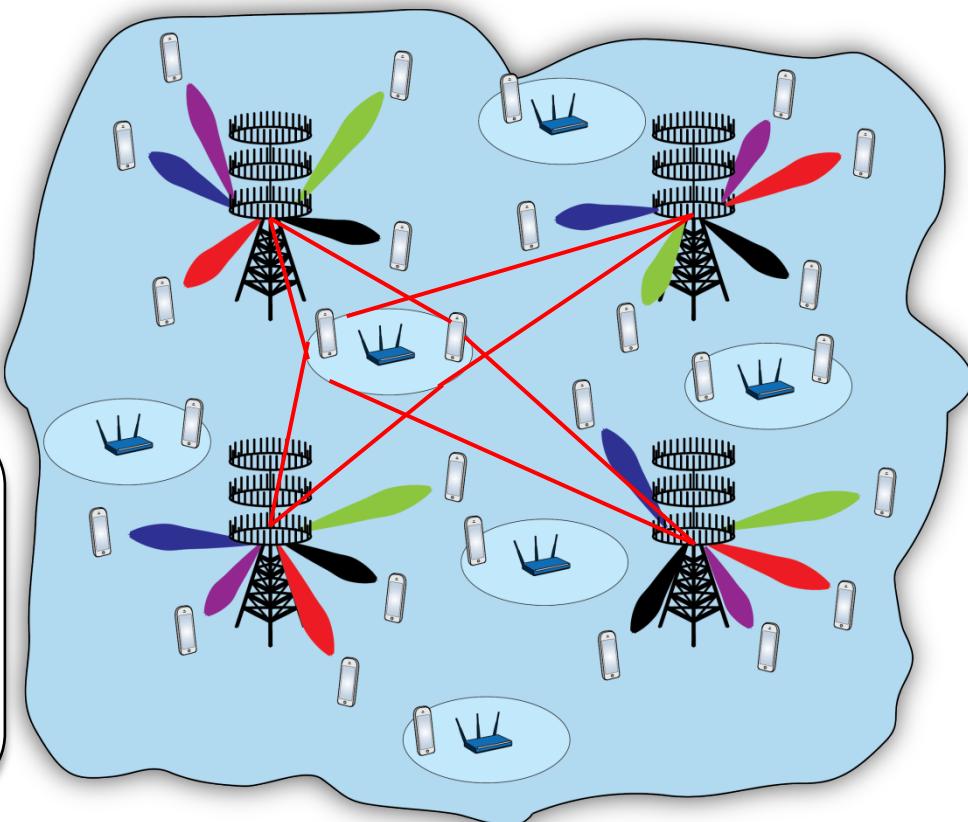


**Key Property: Distributed Coordination**

*N large: Subspace dimension  $M \ll N$*

*Small signal loss, much less interference*

*Combine with user selection?*



Reference: J. Hoydis, K. Hosseini, S. ten Brink, and M. Debbah, *Making Smart Use of Excess Antennas: Massive MIMO, Small Cells, and TDD*, Bell Labs Technical Journal, 2013

# Optimizing Networks for Energy Efficiency (EE)

- Designing Cells for EE
  - Given symmetric cell topology
  - Guarantee a rate  $R$  per user
  - How to achieve optimal EE?

- Energy Efficiency in bit/Joule

$$EE = \frac{\text{Average Sum Rate [bit/s]}}{\text{Power Consumption [Joule/s]}} = \frac{KR}{\text{Transmit Power} + \text{Circuit Power}}$$

- Maximize by selecting  $N$ ,  $K$ , and  $R$ !
- Detailed circuit power model is required:

$$C_{0,0} + C_{0,1}N + C_{1,0}K + C_{1,1}NK + C_{2,0}K^2 + C_{3,0}K^3 + C_{2,1}NK^2 + C_rKR$$

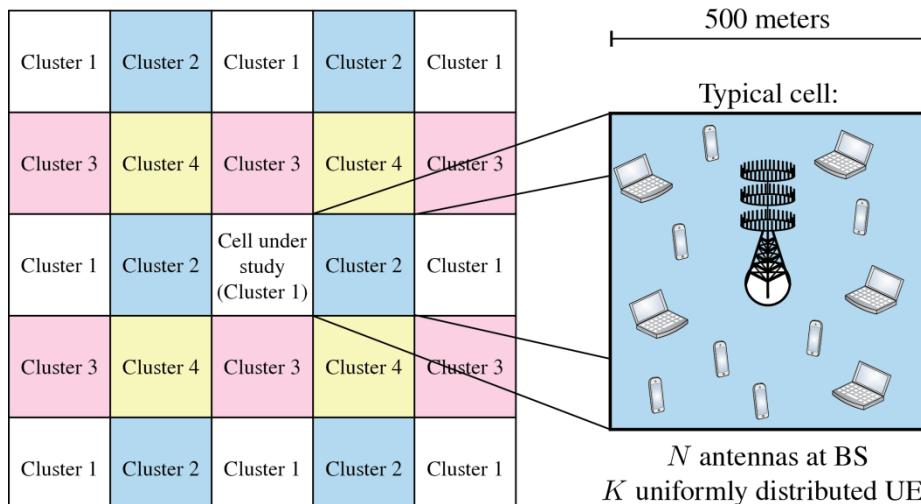
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*Fixed power*  
*(control signals,  
transceiver chain  
infrastructure, etc.)*

*Circuit power per*  
*user*

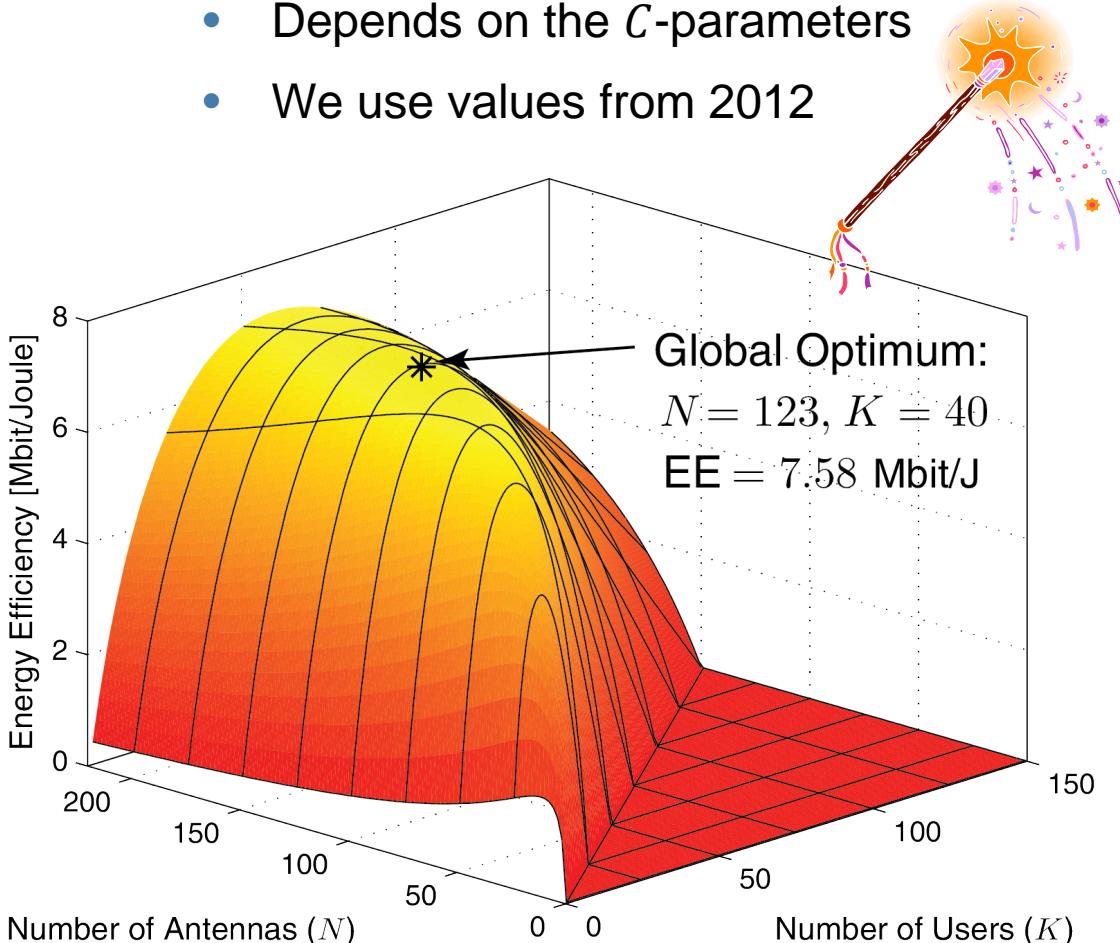
*Cost of channel estimation  
and precoding computation*

*Coding/decoding  
data streams*



# Optimizing Networks for Energy Efficiency (EE)

- What is the EE-Optimal Solution?
  - Depends on the  $C$ -parameters
  - We use values from 2012



**Key Property: EE-optimality**  
*Massive MIMO is the solution*

**Golden Combination**  
*Large array gain*  
*Many simultaneous users*  
*Fractional pilot reuse*

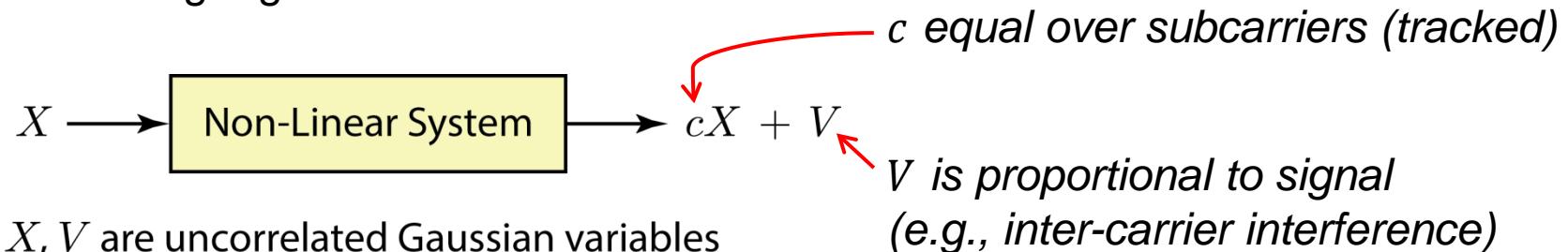
**Transmit Power**  
*Total: Similar to today*  
*Per antenna: Much smaller*  
*Use handset technology?*

# Impact of Hardware Impairments

- Real Hardware is Non-Ideal
  - Hardware impairments: Phase noise, I/Q-imbalance, non-linearities, etc.
  - Impact reduced by calibration/compensation (not fully removed!)
- Simple Hardware Model:



- Assume: Gaussian Input Signal
  - Example: OFDM signal
  - Bussgang's Theorem:



# Impact of Hardware Impairments

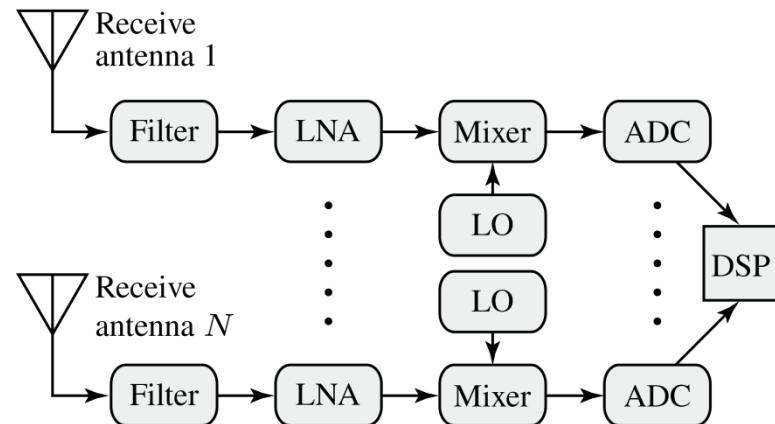
- Impact of Hardware Impairments
  - Additive distortion noise at BS and user
  - Recall: Regular noise/interference vanish as  $N \rightarrow \infty$



**Key Property: Small Impact of Hardware Impairments**

*Distortion noise from BSs vanish in “space”*

*(Unaffected: Distortion noise from user devices)*



**Low Impairments vs. Low Cost and Power**

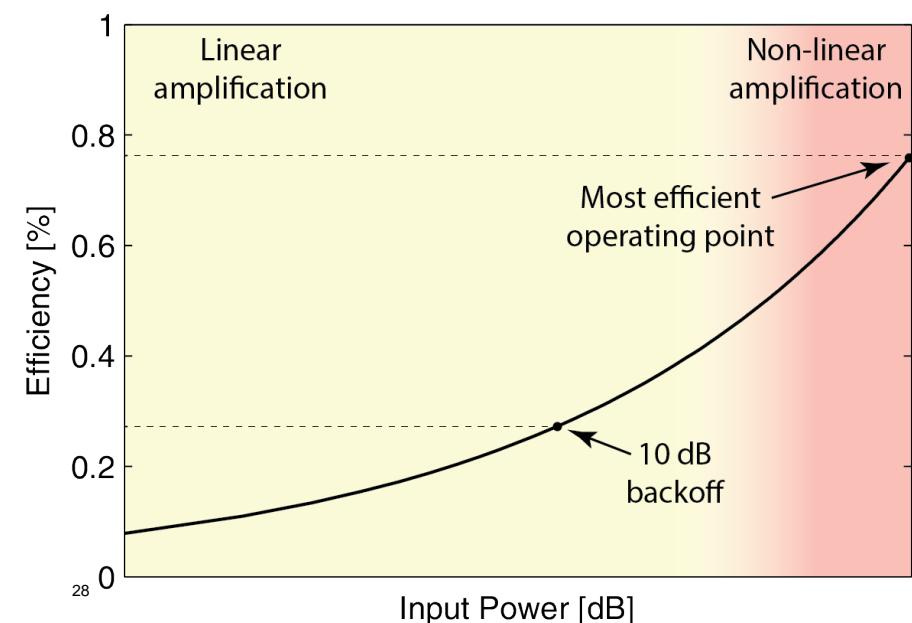
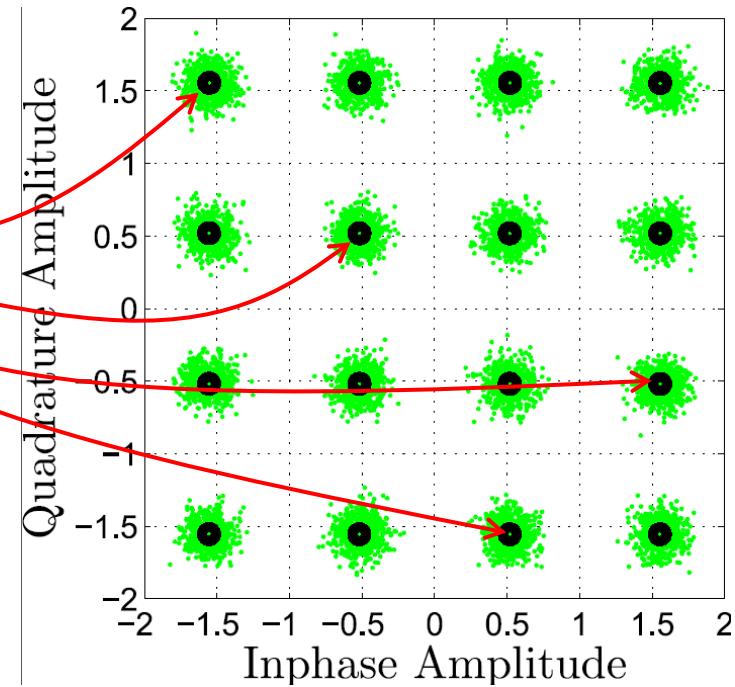
*Tolerate larger impairments → Cheap and energy-efficient hardware*

*N antenna ports:  
Cost and circuit power increase sublinearly in N!*

# Hardware-Friendly Signal Shaping

- Downlink Transmission
  - Received signal:  $y = \mathbf{h}^H \mathbf{w} + n$
- Signal Shaping: Given  $s = \mathbf{h}^H \mathbf{w}$ 
  - How to pick  $\mathbf{w}$ ? ( $N$  degrees of freedom)

The diagram illustrates the received signal equation  $y = \mathbf{h}^H \mathbf{w} + n$ . It shows three paths from the channel and noise source to the final received signal  $y$ , which is labeled as the Effective Signal  $s$ .



**Conventional: Matched filter  $\mathbf{w} \propto \frac{\mathbf{h}}{\|\mathbf{h}\|} s$**

*Pro: Minimize transmit power  $\|\mathbf{w}\|^2$*

*Con: Large power variations ( $\sim 10$  dB) over antennas and time*

# Hardware-Friendly Signal Shaping

- Alternative:  $|w_1|^2 = \dots = |w_N|^2$  for all  $s$ 
  - Pro: Constant envelope at antennas
  - Con: Requires more radiated power

## Metric: Total Consumed Power

Conventional:  $\text{Total} = \text{radiated} + \text{inefficiencies}$

Constant envelope:  $\text{Total} \approx \text{radiated}$

Large  $N$ : Constant envelop is competitive!

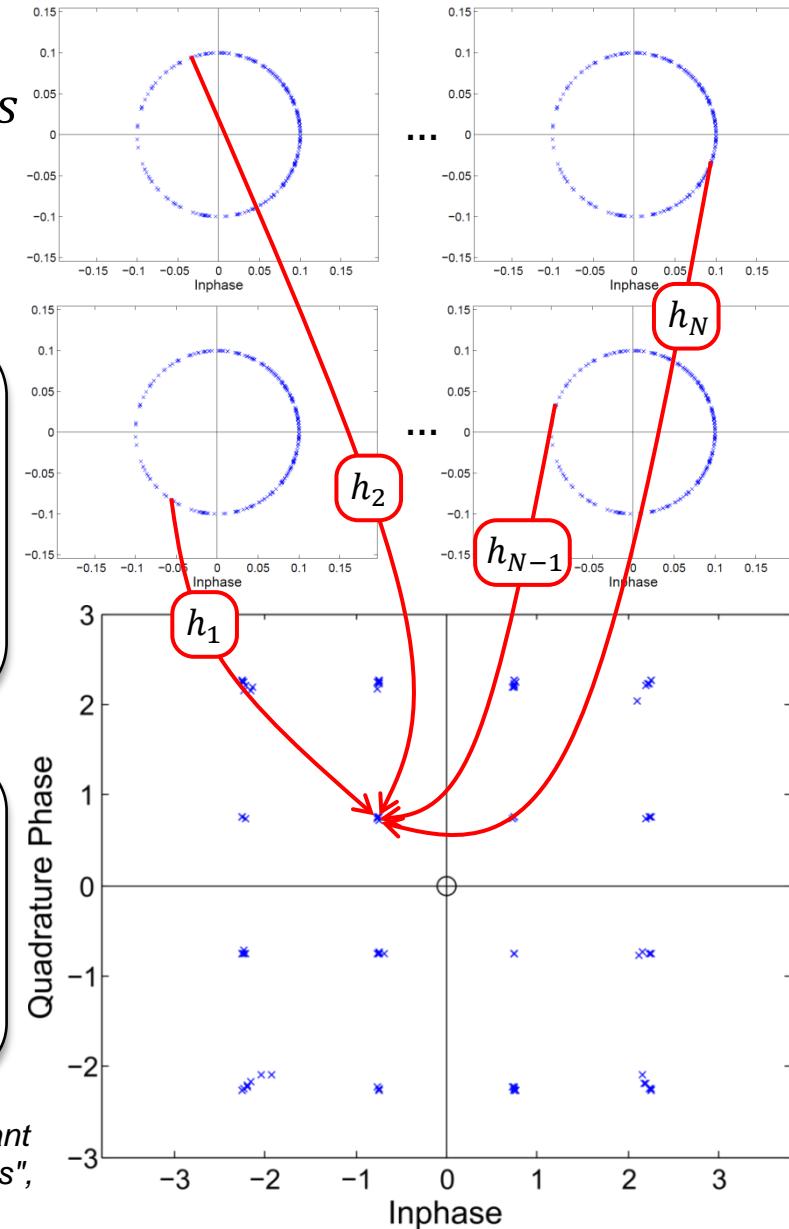
## Key Property: Simplified Amplifiers

Signals with low peak-to-average ratio

Easier to design amplifiers

Cheaper to implement

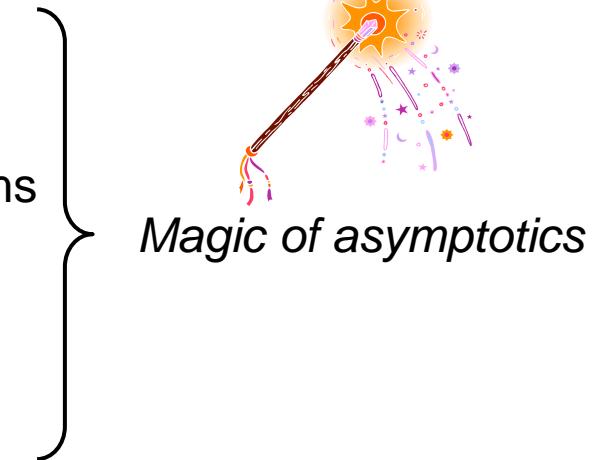
Reference: S.K. Mohammed, Erik G. Larsson, "Per-Antenna Constant Envelope Precoding for Large Multi-User MIMO Systems", IEEE Transactions on Communications, 2013.



# **SUMMARY**

# Summary

- Massive MIMO: A technique to increase spectral efficiency
  - Massive multi-user MIMO: Potentially 20x-40x gain over IMT-Advanced
  - Many different deployment strategies
- Excessive Number of Antennas
  - Quasi-orthogonal user channels
  - Robust interference rejection
  - Distributed coordination with other systems
  - High energy efficiency
  - Resilience to hardware impairments
  - Hardware-friendly signal shaping
- Important: *Channel coherence interval*
  - Limits multiplexing gain and per-user performance
  - Pilot contamination mitigated by smart pilot allocation



# Bringing the Magic to Reality

- FP7 MAMMOET project (Massive MIMO for Efficient Transmission)
  - Bridge gap between “theoretical and conceptual” massive MIMO
  - Develop: Flexible, effective and efficient solutions

**WP4** Validation and proof-of-concept

**WP2** Efficient FE solutions  
(IC solutions,  
Comp/Calibration)

**WP3** Baseband Solutions  
(Algorithms,  
Architectures & Design)

**WP1** System approach, scenarios and requirements





# Linköping University

## expanding reality

**THANK YOU FOR LISTENING!**

**QUESTIONS?**

**Dr. Emil Björnson**

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