Objective: Learn to do clustering and noise reduction in data using PCA

```
In [2]: import matplotlib.pyplot as plt
import numpy as np
from numpy.linalg import svd
from sklearn.datasets import load_digits

digits = load_digits()
digits.data.shape

Out[2]: (1797, 64)

PCA using SVD

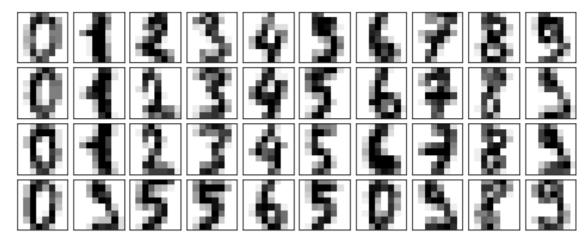
In [3]: def pca(X):
    U, S, PT = svd(X, full_matrices=False)
    Sigma = np.diag(S)
```

```
y = digits.target
print("Shape of X", X.shape)
print("Shape of y", y.shape)
Shape of X (1797, 64)
```

```
In [6]: #Visualize the original data
plot_digits(X)
```

Shape of y (1797,)

ax.imshow(

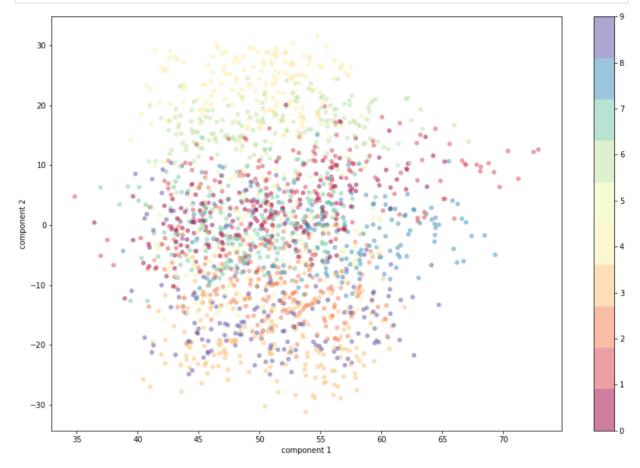


Task 1: Dimensionality reduction: Conduct PCA on the the matrix \$X\$ to find out the dimension required to capture 80% of the variance

```
In [7]:
          import seaborn as sns
          T, S, P = pca(X)
          #plt.plot(sorted(S, reverse=True));
In [8]:
          #SS, _
                 = np.linalg.eig(S)
          explained_variance = (SS ** 2) / 4
          explained_variance_ratio = (explained_variance / explained_variance.sum())
          plt.plot(np.cumsum(explained variance ratio))
          plt.grid()
          plt.xlabel('number of components')
          plt.ylabel('cumulative explained variance');
           1.00
         cumulative explained variance
           0.95
           0.90
           0.85
           0.80
           0.75
           0.70
                           1000
                                                            4000
                                                 3000
                                      2000
                                number of components
```

Task 2: Clustering: Project the original data matrix X on the first two PCs and draw the scalar plot

```
cmap=plt.cm.get_cmap('Spectral', 10))
plt.xlabel('component 1')
plt.ylabel('component 2')
plt.colorbar();
```



Task 3: Denoising: Remove noise from the noisy data

```
In [10]: # Adding noise to the original data
X = digits.data
y = digits.target
np.random.seed(42)
noisy = np.random.normal(X, 4)
plot_digits(noisy)
```

Tips:

• Decompose the noisy data using PCA

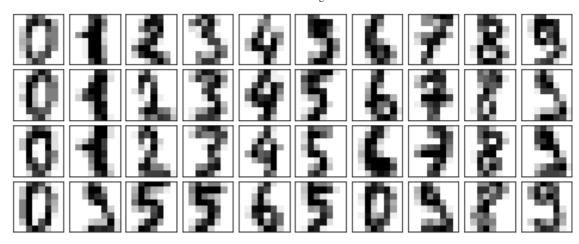
 Reconstruct the data using just a few dominant components. For eg. check the variance plot

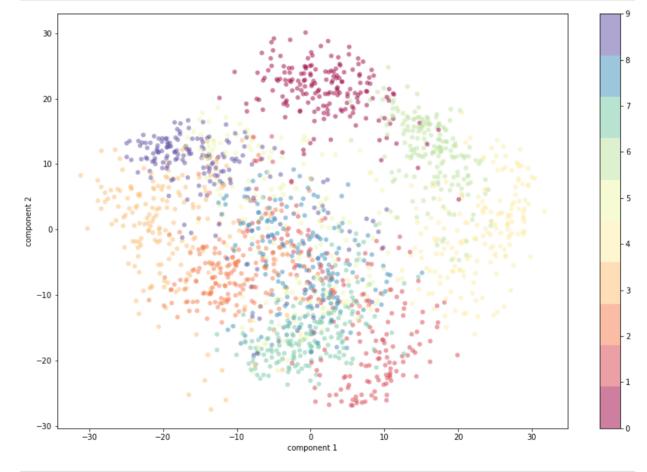
Since the nature of the noise is more or less similar across all the digits, they are not the fearues with enough variance to discriminate between the digits.

```
In [11]:
    T, S, P = pca(noisy)
    n_comps = None
    X_denoised = np.dot(noisy, P)
    plot_digits(X_denoised @ P.T)
```

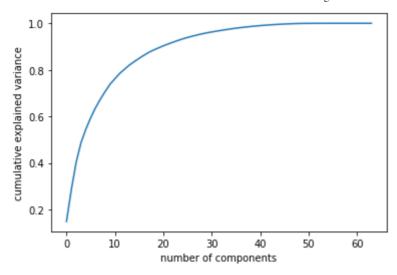
Task 4: Study the impact of normalization of the dataset before conducting PCA. Discuss if it is critical to normalize this particular data compared to the dataset in other notebooks

All the above excercise can be done using the SKLEAR library as follows



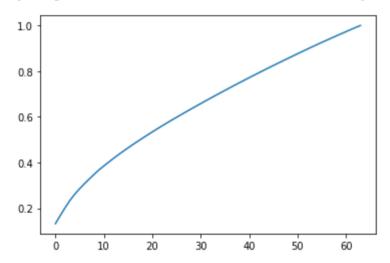


```
pca = PCA().fit(digits.data)
    plt.plot(np.cumsum(pca.explained_variance_ratio_))
    plt.xlabel('number of components')
    plt.ylabel('cumulative explained variance');
```

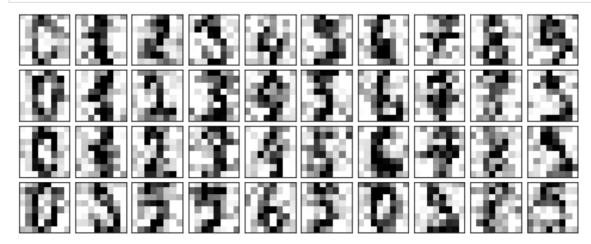


```
In [16]:
    S_diag = np.diag(S)#**2 / 4
    SS = S_diag / np.sum(S_diag)
    plt.plot(np.cumsum(SS))
```

Out[16]: [<matplotlib.lines.Line2D at 0x7fc119270ac0>]



```
In [17]:
    np.random.seed(42)
    noisy = np.random.normal(digits.data, 4)
    plot_digits(noisy)
```

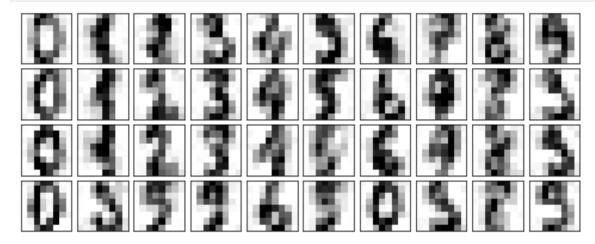


```
pca = PCA(0.50).fit(noisy) # 50% of the variance amounts to 12 principal comp
pca.n_components_
plt.plot(np.cumsum(pca.explained_variance_ratio_))
```

```
plt.xlabel('number of components')
plt.ylabel('cumulative explained variance');
```

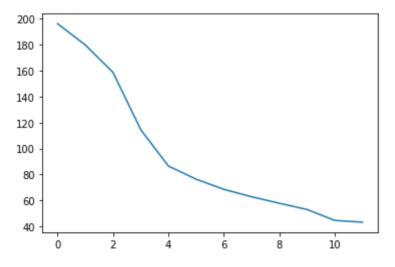
```
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```

```
In [19]: components = pca.transform(noisy)
    filtered = pca.inverse_transform(components)
    plot_digits(filtered)
```



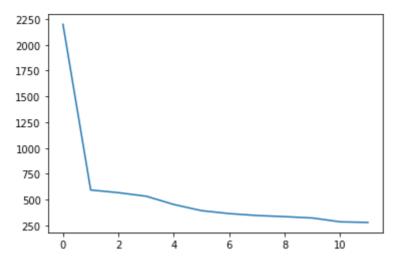
```
In [20]: plt.plot(pca.explained_variance_)
```

Out[20]: [<matplotlib.lines.Line2D at 0x7fc117b2bac0>]



```
In [21]: plt.plot(np.diag(S)[:12])
```

Out[21]: [<matplotlib.lines.Line2D at 0x7fc118a17be0>]



In []:
In []: