# Day 3, Practical 2, Hely's solution

### Helene Charlotte Wiese Rytgaard

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#### Task 1: Implementing the targeting algorithm.

1.

```
sim.fun <- function(n, intervene=list()) {</pre>
    # baseline covariates
    X0.1 < - runif(n, -2, 2)
    X0.2 <- rnorm(n)</pre>
    X0.3 < - rbinom(n, 1, 0.2)
    # baseline treatment (randomized)
    if ("A0" %in% names(intervene)) {
    AO <- intervene$AO
    } else {
    A0 < - rbinom(n, 1, 0.5)
    }
    # follow-up covariates
    X1.1 \leftarrow rbinom(n, 1, plogis(-0.7 + 0.3*X0.3 + 0.8*A0))
    X1.2 \leftarrow rbinom(n, 1, plogis(0.25 - 0.55*X0.3))
    # follow-up treatment
    if ("A1" %in% names(intervene)) {
    A1 <- intervene$A1(X1.1)
    A1 <- rbinom(n, 1, prob=plogis(0.9 - 5*(1-A0) - 4.7*X1.1 - 4.8*X1.2))
    # outcome
    Y <- rbinom(n, 1, prob=plogis(-0.9 - 0.2*A0 + 1.2*X1.1 - 0.1*A1 - 0.8*A1*(X1
    .1==0)))
    if (length(names(intervene))>0) {
    return(mean(Y))
    } else {
    return(data.table(X0.1=X0.1, X0.2=X0.2, X0.3=X0.3,
              AO=AO,
              X1.1=X1.1, X1.2=X1.2,
              A1=A1,
              Y=Y))
```

```
set.seed(15)
   (sim.data <- sim.fun(n=2000))
             X0.1
                         X0.2 X0.3 A0 X1.1 X1.2 A1 Y
   1: 0.40845618 -0.19620228
                                 0 1
                                          1
                                               0 0 1
  2: -1.21982429 0.59503302
                                  1 1
                                          0
                                               0 1 0
                                  0 1
                                          0
                                               0 0 0
  3: 1.86583493 -1.60888231
  4: 0.60362212 0.04123507
                                  0 1
                                               0 1 0
                                 0 0
  5: -0.53171243 -1.25139144
                                          0
                                             1 0 0
1996: -0.72294993 -0.43541869
                                          0
                                             0 0 1
                                 0 1
1997: -0.13592934 -0.80204340 0 0
                                          0
                                             0 0 0
                                 0 0
                                             1 0 0
1998: -1.67193359 -1.57095686
                                          0
1999: 0.68115948 -0.72905589
                               0 1
                                         0
                                             0 1 0
2000: 0.04187752 0.10649384
                                  0 0 0 0 0 1
  2.
   weight.truncation <- FALSE
   fit.pi0 <- glm(A0 ~ X0.1+X0.2+X0.3, family=binomial, data=sim.data)
   fit.pi1 <- glm(A1 \sim X0.1+X0.2+X0.3+A0+X1.1+X1.2, family=binomial, data=sim.data)
   sim.data[, cum.pi0:=predict(fit.pi0, type="response")]
   sim.data[, cum.pi1:=predict(fit.pi0, type="response")*predict(fit.pi1, type="response")
       )]
   if (weight.truncation) {
       sim.data[cum.pi0<0.01, cum.pi0:=0.01]
       sim.data[cum.pi1<0.01, cum.pi1:=0.01]
   sim.data[, H1:=(A0==1)/cum.pi0]
   sim.data[, H2:=(A0==1)*(A1==1)/cum.pi1]
  3.
   fit.Q2 <- glm(Y \sim A1 + X1.1 + X1.2 + A0 + X0.1 + X0.2 + X0.3,
            family=binomial, data=sim.data)
   sim.data[, pred.Q2:=predict(fit.Q2, newdata=copy(sim.data)[, A1:=1], type="response")]
  4.
   fit.tmle2 <- glm(Y \sim offset(qlogis(pred.Q2)), weights=H2,
           family=binomial, data=sim.data)
   sim.data[, pred.Q2.star:=predict(fit.tmle2, type="response")]
   ##-- check that we solve:
   sim.data[, mean(H2*(Y-pred.Q2.star))]
```

-2.22802486597902e-12

5.

6.

```
[1] -1.271552e-17
```

7.

```
(est.own.tmle <- sim.data[, mean(pred.Q1.star)])</pre>
```

#### [1] 0.2759537

8. Compute the standard error by evaluating the efficient influence function, i.e.,

#### [1] 0.1107792

#### Task 2: Using ltmle software.

1.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 ~ X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 ~ X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
```

```
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
Estimator: tmle
Call:
ltmle(data = sim.data, Anodes = paste0("A", 0:1), Lnodes = c(paste0("X0.",
    1:3), paste0("X1.", 1:2)), Ynodes = "Y", abar = c(1, 1),
    variance.method = "ic")
   Parameter Estimate: 0.15695
    Estimated Std Err: 0.051843
               p-value: 0.0024662
    95% Conf Interval: (0.055343, 0.25856)
  2. Go back and change argument weight.truncation to TRUE.
  3.
   summary(fit.ltmle, estimator="iptw")$treatment$estimate
     iptw
0.1460717
  4.
   library(ltmle)
   set.seed(15)
   sim.data <- sim.fun(n=2000)</pre>
   fit.g <- ltmle(sim.data,</pre>
              Anodes=paste0("A",0:1),
              Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
              Ynodes="Y",
              gcomp=TRUE,
              abar=c(1,1), variance.method="ic")
   summary(fit.g)
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
```

```
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
Estimator: gcomp
Warning: inference for gcomp is not accurate! It is based on TMLE influence curves.
Call:
ltmle(data = sim.data, Anodes = paste0("A", 0:1), Lnodes = c(paste0("X0.",
    1:3), paste0("X1.", 1:2)), Ynodes = "Y", abar = c(1, 1),
    gcomp = TRUE, variance.method = "ic")
   Parameter Estimate: 0.22819
    Estimated Std Err: 0.055393
              p-value: 0.000037983
    95% Conf Interval: (0.11962, 0.33676)
```

#### True values of parameters:

ITT: -0.00931700000000002

static: -0.063294 dynamic: -0.050709

#### Task 3: Estimating the static effect.

```
summary(fit.ltmle.static)$effect.measures$ATE
   message("----")
   message("ipw output:")
   message("---")
   summary(fit.ltmle.static, estimator="iptw")$effect.measures$ATE
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
tmle output:
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] -0.215463
$std.dev
[1] 0.05409723
$pvalue
[1] 0.00006808408
$CI
           2.5%
                     97.5%
[1,] -0.3214916 -0.1094343
$log.std.err
[1] FALSE
ipw output:
$long.name
[1] "Additive Treatment Effect"
```

message("---")

\$estimate

```
[1] -0.2263073
$std.dev
[1] 0.04865195
$pvalue
[1] 0.000003294405
$CI
            2.5%
                      97.5%
[1,] -0.3216633 -0.1309512
$log.std.err
[1] FALSE
Task 4: Estimating the static effect with g-formula estimation.
   set.seed(15)
   sim.data <- sim.fun(n=2000)</pre>
   fit.g.static <- ltmle(sim.data,</pre>
                 Anodes=paste0("A",0:1),
                 Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                 Ynodes="Y",
                 abar=list(treatment=c(1,1), control=c(0,0)),
                 gcomp=TRUE,
                 variance.method="ic")
   message("----")
   message("g-formula output:")
   message("---")
   summary(fit.g.static)$effect.measures$ATE
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
```

```
[1] "Additive Treatment Effect"
$estimate
[1] -0.1435938
$std.dev
[1] 0.05750552
$pvalue
[1] 0.01252333
$CI
          2.5%
                     97.5%
[1,] -0.2563026 -0.03088509
$log.std.err
[1] FALSE
Task 5.
   message("----")
   message("tmle output:")
   message("---")
   summary(fit.ltmle.static)$effect.measures$ATE[c("estimate")]
   message("----")
   message("ipw output:")
   message("---")
   summary(fit.ltmle.static, estimator="iptw")$effect.measures$ATE[c("estimate")]
   message("----")
   message("g-formula output:")
   message("---")
   summary(fit.g.static)$effect.measures$ATE[c("estimate")]
-----
tmle output:
$estimate
[1] -0.215463
_____
ipw output:
---
$estimate
[1] -0.2263073
_____
g-formula output:
---
$estimate
[1] -0.1435938
```

Task 6: Estimating the ITT effect.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
Estimate of time to completion: < 1 minute
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] 0.03664088
$std.dev
[1] 0.02179757
$pvalue
[1] 0.09277035
$CI
             2.5%
                        97.5%
[1,] -0.006081571 0.07936332
$log.std.err
[1] FALSE
```

#### Task 7: Estimating the dynamic effect.

```
Qform not specified, using defaults:
formula for X1.1:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0
formula for Y:
Q.kplus1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2 + A1
gform not specified, using defaults:
formula for AO:
A0 \sim X0.1 + X0.2 + X0.3
formula for A1:
A1 \sim X0.1 + X0.2 + X0.3 + A0 + X1.1 + X1.2
Estimate of time to completion: < 1 minute
Warning message:
In CheckForVarianceWarning(inputs, g.ratio) :
  Variance estimate is based on influence curve only, which may be significantly anticonservative b
$long.name
[1] "Additive Treatment Effect"
$estimate
[1] 0.04175735
$std.dev
[1] 0.04672911
$pvalue
[1] 0.3715335
$CI
            2.5%
                     97.5%
[1,] -0.04983003 0.1333447
$log.std.err
[1] FALSE
Task 8.
   message("----")
   message("tmle for static effect:")
   message("---")
   summary(fit.ltmle.static)$effect.measures$ATE[c("estimate", "std.dev")]
   message("----")
   message("tmle for dynamic effect:")
   message("---")
   summary(fit.ltmle.dynamic)$effect.measures$ATE[c("estimate", "std.dev")]
```

\_\_\_\_\_

message("---")

message("----")
message("tmle for itt effect:")

summary(fit.ltmle.itt)\$effect.measures\$ATE[c("estimate", "std.dev")]

```
tmle for static effect:
$estimate
[1] -0.215463
$std.dev
[1] 0.05409723
tmle for dynamic effect:
$estimate
[1] 0.04175735
$std.dev
[1] 0.04672911
______
tmle for itt effect:
$estimate
[1] 0.03664088
$std.dev
[1] 0.02179757
```

Task 9: Simulation study targeting the static effect.

```
library(ltmle)
ate.ltmle.static <- list()</pre>
ate.ipw.static <- list()</pre>
ate.g.static <- list()</pre>
ate.g2.static <- list()</pre>
for (m in 1:500) {
   set.seed(15+m)
   sim.data <- sim.fun(n=2000)</pre>
   ##- 1.
   fit.ltmle <- ltmle(sim.data,</pre>
              Anodes=paste0("A",0:1),
              Lnodes=c(paste0("X0.", 1:3),
               paste0("X1.", 1:2)),
              Ynodes="Y",
              abar=list(treatment=c(1,1), control=c(0,0)))
   ate.ipw.static[[m]] <- summary(fit.ltmle, estimator="iptw")$effect.measures$ATE$
    estimate
   fit.g <- ltmle(sim.data, Anodes=paste0("A",0:1), Lnodes=c(paste0("X0.", 1:3),</pre>
   paste0("X1.", 1:2)), Ynodes="Y",
          abar=list(treatment=c(1,1), control=c(0,0)), gcomp=TRUE)
   ate.g.static[[m]] <- summary(fit.g)$effect.measures$ATE$estimate</pre>
   ##- 3.
```

Task 10. See Figure 1.

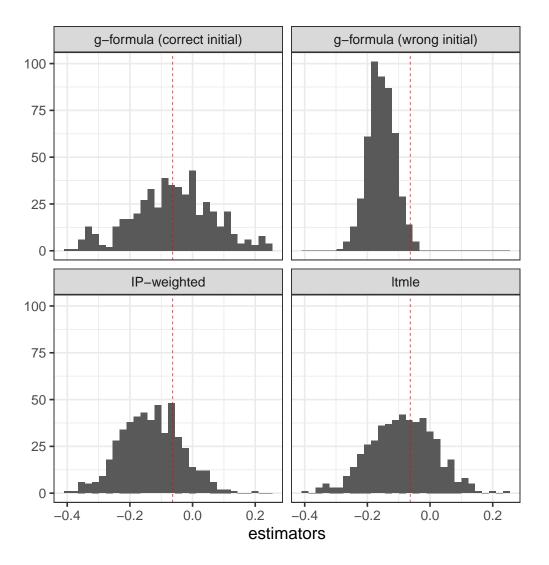


Figure 1

Task 11: Continuing the simulation study with TMLE targeting the dynamic effect and the ITT effect.

```
library(ltmle)
ate.ltmle.static <- list()</pre>
ate.se.ltmle.static <- list()</pre>
ate.ltmle.itt <- list()</pre>
ate.se.ltmle.itt <- list()
ate.ltmle.dynamic <- list()</pre>
ate.se.ltmle.dynamic <- list()</pre>
for (m in 1:500) {
    set.seed(15+m)
    sim.data <- sim.fun(n=2000)
    ##- 1.
    fit.ltmle <- ltmle(sim.data,</pre>
               Anodes=paste0("A",0:1),
               Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
               Ynodes="Y",
                abar=list(treatment=c(1,1), control=c(0,0)),
                Qform=c(X1.1="Q.kplus1\sim X0.1+X0.2+X0.3+A0",
                    Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
               variance.method="ic")
    ate.ltmle.static[[m]] <- summary(fit.ltmle)$effect.measures$ATE$estimate
    ate.se.ltmle.static[[m]] <- summary(fit.ltmle)$effect.measures$ATE$std.dev</pre>
    fit.ltmle.itt <- ltmle(sim.data,</pre>
               Anodes=paste0("A",0),
               Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2), "A1"),
                {\tt Qform=c\,(X1.1="Q.kplus1}{\sim}{\tt X0.1+X0.2+X0.3+A0"}\,,
                    Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
                abar=list(treatment=c(1), control=c(0)),
                variance.method="ic")
    ate.ltmle.itt[[m]] <- summary(fit.ltmle.itt)$effect.measures$ATE$estimate
    ate.se.ltmle.itt[[m]] <- summary(fit.ltmle.itt)$effect.measures$ATE$std.dev
    fit.ltmle.dynamic <- ltmle(sim.data,</pre>
                    Anodes=paste0("A",0:1),
                    Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                    Ynodes="Y".
                    Qform=c(X1.1="Q.kplus1~X0.1+X0.2+X0.3+A0",
                        Y="Q.kplus1\sim X0.1+X0.2+X0.3+A0+X1.1+X1.2+A1*X1.1"),
                    rule=list(treatment=function(row) c(1, ifelse(row["X1.1"]==1, 0, 1)
    ),
                      control=function(row) c(0,0)),
                    variance.method="ic")
    ate.ltmle.dynamic[[m]] <- summary(fit.ltmle.dynamic)$effect.measures$ATE$estimate
    ate.se.ltmle.dynamic[[m]] <- summary(fit.ltmle.dynamic)$effect.measures$ATE$std.
    dev
}
```

Task 12. See Figure 2.

coverage: tmle for static effect:
--[1] 0.568
----coverage: tmle for itt effect:
--[1] 0.938
----coverage: tmle for dynamic effect:

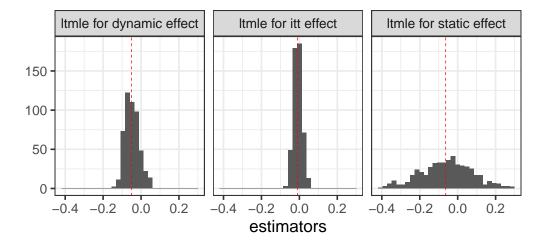


Figure 2

Task 13: Using super learning.

1.

[1] 0.928

```
fit.ltmle.sl <- ltmle(sim.data, Anodes=paste0("A",0:1),</pre>
                 Lnodes=c(paste0("X0.", 1:3), paste0("X1.", 1:2)),
                 Ynodes="Y",
                 SL.library=list(Q=c("SL.glm", "SL.mean", "SL.glm.interaction",
                         "SL.glmnet", "SL.gam"),
                         g=c("SL.glm", "SL.mean", "SL.glmnet",
                         "SL.gam")),
                 rule=list(treatment=function(row) c(1, ifelse(row["X1.1"]==1, 0, 1)),
                   control=function(row) c(0,0)), variance.method="ic")
  2.
   fit.ltmle.sl$fit$Q[[1]]
   fit.ltmle.sl\fit\g
$X1.1
                               Risk
                                           Coef
SL.glm_All
                         0.02662852 0.00000000
SL.mean_All
                         0.02792894 0.04233679
SL.glm.interaction_All 0.02660383 0.50686160
SL.glmnet_All
                                 NA 0.0000000
SL.gam_All
                         0.02660866 0.45080161
$Y
                                          Coef
                              Risk
                         0.2166817 0.00000000
                         0.2385468 0.00000000
                         0.2158281 0.90147281
                         0.2167009 0.00000000
```

SL.glm\_All SL.mean\_All SL.glm.interaction\_All 0.2186063 0.09852719 SL.glmnet\_All SL.gam\_All [[1]]

[[1]]\$AO

Risk Coef SL.glm\_All 0.2501241 SL.mean\_All 0.2497703 1 SL.glmnet\_All 0.2497703 0 SL.gam\_All 0.2502473 0

[[1]]\$A1

Risk Coef SL.glm\_All 0.02687716 0.0000000 SL.mean\_All 0.06689833 0.0000000 SL.glmnet\_All 0.02684041 0.6521786 SL.gam\_All 0.02688544 0.3478214

[[2]] [[2]]\$AO

Risk Coef

SL.glm_All	0.2501241	0
SL.mean_All	0.2497703	1
SL.glmnet_All	0.2497703	0
SL.gam_All	0.2502473	0

## [[2]]\$A1

	Risk	Coef
SL.glm_All	0.02687716	0.0000000
SL.mean_All	0.06689833	0.0000000
SL.glmnet_All	0.02684041	0.6521786
SL.gam_All	0.02688544	0.3478214