

oppg. 1)

$$E[X] = \sum_x x \cdot f(x)$$

$$= (0 \cdot 0.05) + (1 \cdot 0.10) + (2 \cdot 0.25)$$

$$+ (3 \cdot 0.40) + (4 \cdot 0.15) + (5 \cdot 0.05)$$

$$= \underline{2.65}$$

$$E[X] = \frac{\text{sum}(x)}{n}, \quad \text{gjennomsnitt verdiene av } x.$$

$$\approx 2.644 \quad (i \text{ min simulering})$$

$$P(X \leq 2) \approx 0.404$$

Dette er relativt nærme eksakt verdi,
dividet noe.

Oppg. 2a) X = kontinu komp.

$$F_X(x) = 1 - \exp\left\{-\frac{x^2}{a}\right\} \quad x \geq 0$$

$$= P(X \text{ har v\u00e6rdet innen } x \text{ \u00e5r}) = P(X \leq x)$$

$$f_X(x) = F_X(x) \frac{d}{dx} = \frac{\frac{2}{a} x \cdot e^{-\frac{x^2}{a}}}{\text{For \u00f8ring!}}$$

$$E[X] = \int_0^{\infty} x \cdot \frac{2}{a} x \cdot e^{-\frac{x^2}{a}} dx = \frac{2}{a} \int_0^a x^2 e^{-\frac{x^2}{2}}$$

$$= \frac{\sqrt{\pi} \sqrt{a}}{2}$$

$$2b) \quad U \sim \text{Unif}[0, 1]$$

$$g(U) = X$$

$$1. \quad X = F_X^{-1}(U)$$

$$U = 1 - \exp\left(-\frac{x^2}{d}\right)$$

$$\exp\left(-\frac{x^2}{d}\right) = 1 - U$$

$$-\frac{x^2}{d} = \ln(1 - U)$$

$$g(U) = X = \sqrt{-d \ln(1 - U)}$$

$$2c) \quad X = F_Y^{-1}(U)$$

$$2c) \quad x = F_Y^{-1}(U)$$

$$F_Y(x) = P(Y \leq x)$$

$$= P(X,$$

опы 3)

$$f_{XY}(x, y)$$

$$f_X(x) = \begin{cases} x=0, & \frac{1}{18} + \frac{1}{6} + \frac{1}{18} + \frac{1}{18} = \frac{1}{3} \\ x=1, & \dots = \frac{1}{3} \\ x=2, & \dots = \frac{1}{3} \end{cases}$$

$$f_{Y|X}(y|x) = f_{XY}(x, y) / f_X(x)$$

$$= 3 \cdot f_{XY}(x, y)$$

$$E[X] = 0 \cdot \frac{1}{3} + 1 \cdot \frac{1}{3} + 2 \cdot \frac{1}{3} = 1$$

$$f_Y(y) = \begin{cases} y=0, & \frac{3}{18} = \frac{1}{6} \\ y=1, & \frac{5}{18} \\ y=2, & \frac{5}{18} \\ y=3, & \frac{5}{18} \end{cases}$$

$$E[Y] = \frac{5}{18} + 2 \cdot \frac{5}{18} + 3 \cdot \frac{5}{18} = \frac{5}{3}$$

$P(Y) \neq P(Y|X)$, da es
unke unabhängig

oppg 4a)

$$P(A_i) = \frac{1}{6} + \frac{5}{6} \left(\frac{1}{6} + \frac{5}{6} \cdot \frac{1}{6} \right)$$

$$= 1 - P(\overline{A_i}) = \left(\frac{5}{6} \right)^3$$

$$= 1 - \frac{125}{216} = \frac{91}{216} \approx 0.421$$

$$E(Y_i) = \sum_x x \cdot f_{Y_i}(x) = 1 \cdot 0.421$$

$$\text{Var}[Y_i] = E\left[(Y_i - E[Y_i])^2\right]$$

$$= \boxed{E[Y_i^2] - E[Y_i]^2} = (1^2 \cdot 0.421) - 0.421^2$$

$$\approx 0.244$$

$$\begin{aligned}
 E[X] &= \sum_x 5x \cdot f_{Y_i}(x) = 5 \cdot E[Y_i] \\
 &\approx 2.11
 \end{aligned}$$

$$\text{Var}[X_i] = E[X_i^2] - E[X_i]^2$$

$$\begin{aligned}
 E[X_i^2] &= \sum_x x^2 \cdot P(X_i = x) \\
 &= 1^2 \cdot \left(3 \cdot \frac{1}{6} + \left(\frac{5}{6} \right)^2 \right) + 2^2 \cdot \left(\binom{3}{2} \cdot \left(\frac{1}{6} \right)^2 \cdot \frac{5}{6} \right) \\
 &\quad + 3^3 \cdot \left(\left(\frac{1}{6} \right)^3 \right) = \frac{26}{9} \approx 2.22
 \end{aligned}$$

$$5.88 - 2.11^2 \approx 1.44$$