

## Sorting (record, key)

Target: Sorting any type of data

We need to be able to compare objects

The sorting method should be the same for all types

Total order:

- antisymmetric:  $v \leq w, w \leq v \rightarrow v = w$
- transitive:  $v \leq w, w \leq x \rightarrow v \leq x$
- total:  $v \leq w$  or  $w \leq v$  or both

Non-transitive

Stone-scissors-paper

Callback = a reference to executable code

- The client passes an array of object to `sort()`
- `sort()` calls `compareTo()` on the objects that should be sorted

implements comparable, `compareTo()` returns pos/neg/zero int.

negative if "less" than compared object

positive if "larger" than compared object

zero if "equal" to compared object

`Double.compareTo()` is non-transitive ( $-0.0 \neq 0.0$ ; NaN)

Selection sort: Find "smallest", put first, repeat  $(N^2)$   
(swap)

Insertion sort: Swap if "left" element is "larger" than "right" element  
Worst case  $N^2$  Best case  $N$ , Better if almost sorted

Partially sorted if #inversions  $\leq cN$ ,  $c$  is a constant  
(almost)

Binary insertion sort, binary search to find "insertion point"  
in sorted part of array.

Shell sort

$h$ -sorting ( $h$ -sorted array is  $h$  interleaved sorted subsequences)  $h \rightarrow 1$

Worst case  $N^2$  ( $N \log^2 N$  for best gap sequence) Best case  $N \log N$

No complete mathematical analysis has been found.

Not efficient for big arrays because of caching

(Radix sort)

## Shuffling

Randomize sorting order

Shuffle sort Generate one <sup>random</sup> number for each element

Pseudo Random Number Generators

seed - same seed  $\rightarrow$  same sequence

large prime seed is often best.

quality of number generators vary.

(Microsoft - shuffle browsers) (IE to right 50% of time)

Knuth shuffle swap  $a[i]$  with random  $a[r]$

Not completely random

"The generation of random numbers is too important to be left to chance!"  
- Robert R. Coveyou

Hardware solutions are generally better.