

Neural Network

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```
In [58]:
          import numpy as np
          import imageio
          import sys
          import os
          import matplotlib.pyplot as plt
          import pickle
          import random
          import gcsfs
          !pip install qdown
          import gdown
          from __future__ import print_function
          from random import randrange
          from math import sqrt
        Requirement already satisfied: gdown in /usr/local/lib/python3.10/dist-p
        ackages (4.7.3)
```

Requirement already satisfied: filelock in /usr/local/lib/python3.10/dis

t-packages (from gdown) (3.13.3) Requirement already satisfied: requests[socks] in /usr/local/lib/python

3.10/dist-packages (from gdown) (2.31.0) Requirement already satisfied: six in /usr/local/lib/python3.10/dist-pac kages (from gdown) (1.16.0)

Requirement already satisfied: tqdm in /usr/local/lib/python3.10/dist-pa ckages (from gdown) (4.66.2)

Requirement already satisfied: beautifulsoup4 in /usr/local/lib/python3. 10/dist-packages (from gdown) (4.12.3)

Requirement already satisfied: soupsieve>1.2 in /usr/local/lib/python3.1 0/dist-packages (from beautifulsoup4->gdown) (2.5)

Requirement already satisfied: charset-normalizer<4,>=2 in /usr/local/li b/python3.10/dist-packages (from requests[socks]->gdown) (3.3.2)

Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.10 /dist-packages (from requests[socks]->gdown) (3.6)

Requirement already satisfied: urllib3<3,>=1.21.1 in /usr/local/lib/pyth on3.10/dist-packages (from requests[socks]->gdown) (2.0.7)

Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/pyth on3.10/dist-packages (from requests[socks]->gdown) (2024.2.2)

Requirement already satisfied: PySocks!=1.5.7,>=1.5.6 in /usr/local/lib/ python3.10/dist-packages (from requests[socks]->gdown) (1.7.1)

```
In [45]:
          sys.path.append(os.path.abspath('/content/cs5262-p2/Week9/code'))
          from network import Network
```

```
from gradient check import eval numerical gradient
          from data utils import load CIFAR10
          from vis utils import visualize grid
In [25]:
          %matplotlib inline
          plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plot
          plt.rcParams['image.interpolation'] = 'nearest'
          plt.rcParams['image.cmap'] = 'gray'
          # for auto-reloading external modules
          # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-
          %load ext autoreload
          %autoreload 2
          def rel error(x, y):
              """ returns relative error """
              return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(x))
        The autoreload extension is already loaded. To reload it, use:
```

Task 1: Design Your Neural Network

%reload ext autoreload

We use the class Network in the file network.py to represent instances of our network. The network parameters are stored in the instance variable self.params where keys are string parameter names and values are numpy arrays. Below, we initialize toy data and a toy model that we will use to develop your implementation.

```
In [15]:
          # Create a small net and some toy data to check your implementations.
          # Note that we set the random seed for repeatable experiments.
          input size = 4
          hidden size = 10
          num classes = 3
          num inputs = 5
          def init toy model():
              np.random.seed(0)
              return Network(input size, hidden size, num classes, std=1e-1)
          def init_toy_data():
              np.random.seed(1)
              X = 10 * np.random.randn(num inputs, input size)
              y = np.array([0, 1, 2, 2, 1])
              return X, y
          net = init_toy_model()
          X, y = init toy data()
```

Forward pass: compute scores

Open the file network.py and look at the method Network.loss. This function is to take the data and weights and computes the class scores, the loss, and the gradients on the parameters.

First, implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

```
In [16]:
          scores = net.loss(X)
          print('Your scores:')
          print(scores)
          print()
          print('correct scores:')
          correct scores = np.asarray([
            [-0.81233741, -1.27654624, -0.70335995],
            [-0.17129677, -1.18803311, -0.47310444],
            [-0.51590475, -1.01354314, -0.8504215],
            [-0.15419291, -0.48629638, -0.52901952],
            [-0.00618733, -0.12435261, -0.15226949]])
          print(correct scores)
          print()
          # The difference should be very small. We get < 1e-7
          print('Difference between your scores and correct scores:')
          print(np.sum(np.abs(scores - correct scores)))
        Your scores:
        [[-0.81233741 -1.27654624 -0.70335995]
         [-0.17129677 -1.18803311 -0.47310444]
         [-0.51590475 -1.01354314 -0.8504215 ]
         [-0.15419291 -0.48629638 -0.52901952]
         [-0.00618733 -0.12435261 -0.15226949]]
        correct scores:
        [[-0.81233741 -1.27654624 -0.70335995]
         [-0.17129677 -1.18803311 -0.47310444]
         [-0.51590475 -1.01354314 -0.8504215 ]
         [-0.15419291 -0.48629638 -0.52901952]
         [-0.00618733 -0.12435261 -0.15226949]]
        Difference between your scores and correct scores:
        3.6802720745909845e-08
```

Forward pass: compute loss

In the same function, implement the second part that computes the data and regularizaion loss.

```
In [21]:
          !ls
        cs5262-p2 sample data
         loss, \_ = net.loss(X, y, reg=0.05)
```

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```
# should be very small, we get < 1e-12
print('Difference between your loss and correct loss:')
print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Difference between your loss and correct loss: 0.02851791272476567

Backward pass

In this step, it will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

```
In [32]: # Use numeric gradient checking to check your implementation of the bac
# If your implementation is correct, the difference between the numeric
# analytic gradients should be less than 1e-8 for each of W1, W2, b1, a

loss, grads = net.loss(X, y, reg=0.05)

# these should all be less than 1e-8 or so
for param_name in grads:
    f = lambda W: net.loss(X, y, reg=0.05)[0]
    param_grad_num = eval_numerical_gradient(f, net.params[param_name],
    print('%s max relative error: %e' % (param_name, rel_error(param_gr

W2 max relative error: 1.0000000e+00
b2 max relative error: 4.447625e-11
W1 max relative error: 1.0000000e+00
b1 max relative error: 2.738421e-09
```

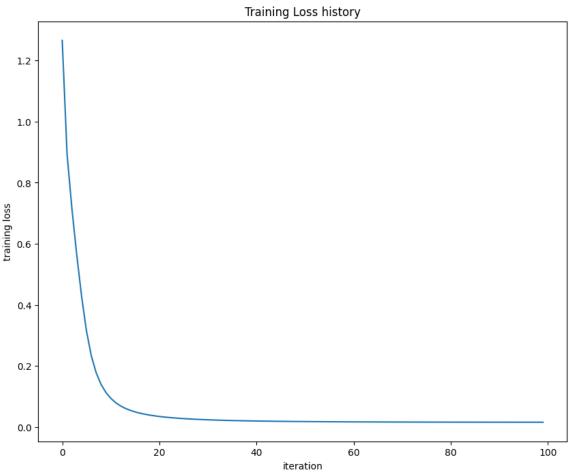
Task 2: Network Training

To train the network we will use stochastic gradient descent (SGD). Complete the missing sections in Network.train to implement the training procedure. Then, You will also have to implement Network.predict, as the training process periodically performs prediction to keep track of accuracy over time while the network trains.

Once you have implemented the method, run the code below to train a network on toy data. You should achieve a training loss less than 0.2.

```
pit.piot(stats['loss_nistory'])
plt.xlabel('iteration')
plt.ylabel('training loss')
plt.title('Training Loss history')
plt.show()
```

Final training loss: 0.015629557257289952



Load CIFAR-10

Now that you have implemented a two-layer network that passes gradient checks and works on toy data, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier on a real dataset.

N_VOC - N_CLOTH[HOSK]

```
y_val = y_train[mask]
      mask = list(range(num_training))
      X train = X train[mask]
      y train = y train[mask]
      mask = list(range(num test))
      X \text{ test} = X \text{ test[mask]}
      y_test = y_test[mask]
      # Normalize the data: subtract the mean image
      mean image = np.mean(X train, axis=0)
      X train -= mean image
      X val -= mean image
      X test -= mean image
      # Reshape data to rows
      X train = X train.reshape(num training, -1)
      X val = X val.reshape(num validation, -1)
      X test = X test.reshape(num test, -1)
      return X_train, y_train, X_val, y_val, X_test, y_test
 # Cleaning up variables to prevent loading data multiple times (which \pi
 try:
     del X train, y train
     del X test, y test
     print('Clear previously loaded data.')
  except:
     pass
 # Invoke the above function to get our data.
 X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
 print('Train data shape: ', X train.shape)
 print('Train labels shape: ', y train.shape)
 print('Validation data shape: ', X_val.shape)
 print('Validation labels shape: ', y_val.shape)
  print('Test data shape: ', X_test.shape)
 print('Test labels shape: ', y test.shape)
Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

Train a network

To train our network we will use SGD. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
In [64]: input_size = 32 * 32 * 3
hidden_size = 50
```

```
iteration 0 / 1000: loss 2.302910
iteration 100 / 1000: loss 2.303191
iteration 200 / 1000: loss 2.305855
iteration 300 / 1000: loss 2.356384
iteration 400 / 1000: loss 2.427878
iteration 500 / 1000: loss 2.457598
iteration 600 / 1000: loss 2.456318
iteration 700 / 1000: loss 2.386205
iteration 800 / 1000: loss 2.315118
iteration 900 / 1000: loss 2.301357
Validation accuracy: 0.281
```

Debug the training

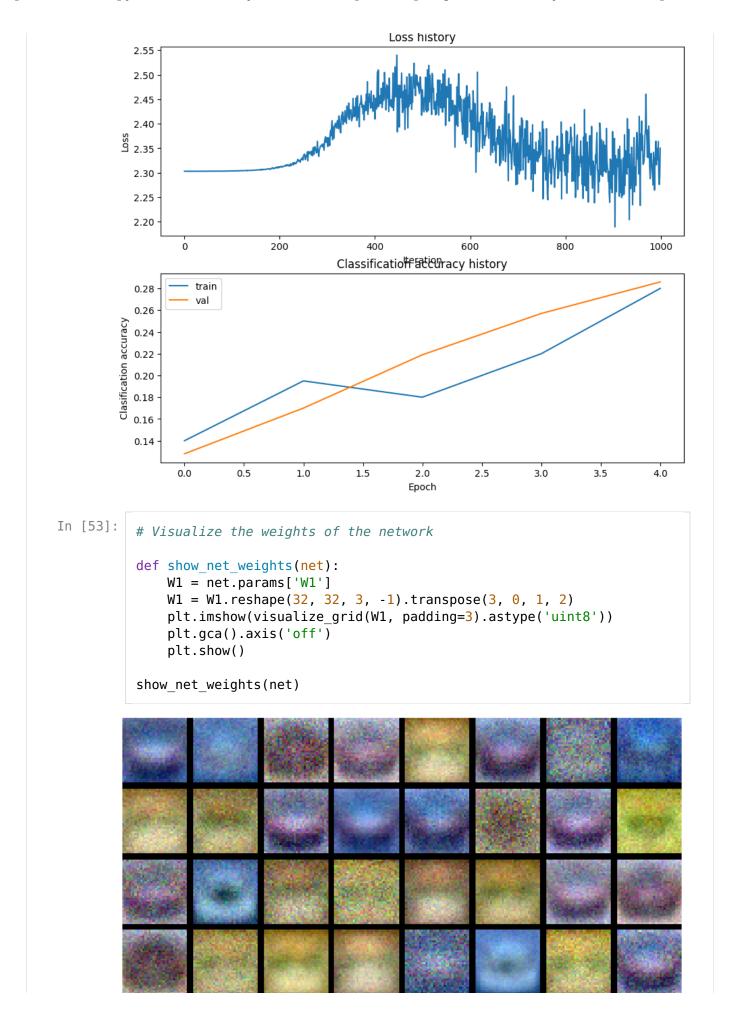
With the default parameters we provided above, you should get a validation accuracy of about 0.29 on the validation set. This isn't very good.

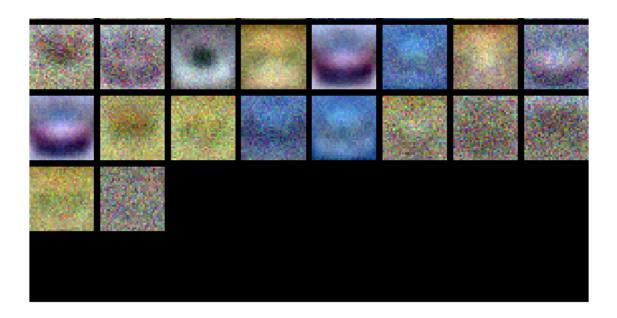
One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

```
In [51]: # Plot the loss function and train / validation accuracies
   plt.subplot(2, 1, 1)
   plt.plot(stats['loss_history'])
   plt.title('Loss history')
   plt.xlabel('Iteration')
   plt.ylabel('Loss')

   plt.plot(stats['train_acc_history'], label='train')
   plt.plot(stats['val_acc_history'], label='val')
   plt.title('Classification accuracy history')
   plt.xlabel('Epoch')
   plt.ylabel('Clasification accuracy')
   plt.legend()
   plt.show()
```





Task 3: Tune Your Network

What's wrong? Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

Tuning. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer size, learning rate, numer of training epochs, and regularization strength. You might also consider tuning the learning rate decay, but you should be able to get good performance using the default value.

Approximate results. You should be aim to achieve a classification accuracy of greater than 48% on the validation set. Our best network gets over 52% on the validation set.

Experiment: You goal in this exercise is to get as good of a result on CIFAR-10 as you can, with a fully-connected Neural Network. Feel free implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

I Use random search to explore different hyperparameter combinations, evaluating each configuration's performance on the validation set. It iterates a defined number of times, and updates the best configuration based on highest validation accuracy. run_network function creates, trains, and evaluates the neural network with random

hyperparametes. After all iterations, it selectss the best performing model and its corresponding hyperparameters.

```
In [55]:
         # TODO: Tune hyperparameters using the validation set. Store your best
         # model in best net.
         # To help debug your network, it may help to use visualizations similar
         # ones we used above; these visualizations will have significant qualit
         # differences from the ones we saw above for the poorly tuned network.
         # Tweaking hyperparameters by hand can be fun, but you might find it us
         # write code to sweep through possible combinations of hyperparameters
         # automatically like we did on the previous exercises.
         # Define hyperparameter ranges
         hidden sizes = [50, 100, 200]
         num iters = [1000, 2000]
         batch sizes = [100, 200]
         learning rates = [1e-4, 5e-4, 1e-3]
         learning rate decays = [0.95]
         regs = [0.1, 0.25, 0.5]
         best val acc = -1
         best hyperparams = None
         best net = None
In [56]:
         def run network(input size, hidden size, num classes, X train, y train,
                        num iter, batch size, learning rate, learning rate deca
             # Create and train the network
             net = Network(input size, hidden size, num classes)
             stats = net.train(X train, y train, X val, y val,
                             num iters=num iter, batch size=batch size,
                             learning rate=learning rate, learning rate decay=
                              reg=reg, verbose=False)
             # Evaluate on validation set
             val acc = (net.predict(X val) == y val).mean()
             # Evaluate on test set (optional)
             test acc = (net.predict(X test) == y test).mean() if X test is not
             return stats, val acc, net, test acc
In [60]:
         # Random search hyperparameters
         num\ configs = 20 # Number of random configurations to try
         for in range(num configs):
             hidden size = random.choice(hidden sizes)
             num iter = random.choice(num iters)
             batch size = random.choice(batch sizes)
             learning rate = random.choice(learning rates)
```

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```
learning rate decay = random.cnoice(learning rate decays)
      reg = random.choice(regs)
      stats, val acc, net, test acc = run network(
          input size, hidden_size, num_classes,
          X train, y train, X val, y val, X test, y test,
          num iter, batch size, learning rate,
          learning rate decay, reg)
     print("hs: {}, ni: {}, bs: {}, lr: {:.5f}, lrd: {}, reg: {:.5f}, va
          hidden size, num iter, batch size, learning rate, learning rate
     if val acc > best val acc:
          best val acc = val acc
          best hyperparams = {
              'hidden size': hidden size,
              'num iter': num iter,
              'batch size': batch size,
              'learning_rate': learning rate,
              'learning rate decay': learning rate decay,
              'reg': reg
          best net = net
 print("Best validation accuracy:", best val acc)
 print("Best hyperparameters:", best hyperparams)
hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.50000, val: 0.
47
hs: 50, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg: 0.10000, val: 0.
45
hs: 50, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg: 0.25000, val: 0.
hs: 100, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg: 0.10000, val:
hs: 200, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg: 0.50000, val:
0.31
hs: 200, ni: 1000, bs: 200, lr: 0.00050, lrd: 0.95, reg: 0.25000, val:
hs: 200, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg: 0.50000, val:
hs: 50, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg: 0.25000, val: 0.
43
hs: 100, ni: 2000, bs: 100, lr: 0.00100, lrd: 0.95, reg: 0.50000, val:
hs: 100, ni: 2000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.10000, val:
0.51
hs: 100, ni: 1000, bs: 200, lr: 0.00010, lrd: 0.95, reg: 0.25000, val:
0.28
hs: 50, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg: 0.25000, val: 0.
hs: 200, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg: 0.10000, val:
hs: 200, ni: 1000, bs: 200, lr: 0.00010, lrd: 0.95, reg: 0.50000, val:
hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.10000, val: 0.
47
hs: 50, ni: 2000, bs: 200, lr: 0.00050, lrd: 0.95, reg: 0.25000, val: 0.
```

```
hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.10000, val: 0.
hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.10000, val: 0.
47
hs: 100, ni: 2000, bs: 200, lr: 0.00100, lrd: 0.95, reg: 0.10000, val:
hs: 100, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg: 0.50000, val:
0.45
Best validation accuracy: 0.505
Best hyperparameters: {'hidden size': 100, 'num iter': 2000, 'batch size
': 200, 'learning_rate': 0.001, 'learning_rate_decay': 0.95, 'reg': 0.1}
Here is example output:
    hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.50000, val: 0.47
    hs: 50, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg:
    0.10000, val: 0.45
    hs: 50, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg:
    0.25000, val: 0.29
    hs: 100, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg:
    0.10000, val: 0.30
    hs: 200, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg:
    0.50000, val: 0.31
    hs: 200, ni: 1000, bs: 200, lr: 0.00050, lrd: 0.95, reg:
    0.25000, val: 0.46
    hs: 200, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg:
    0.50000, val: 0.44
    hs: 50, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg:
    0.25000, val: 0.43
    hs: 100, ni: 2000, bs: 100, lr: 0.00100, lrd: 0.95, reg:
    0.50000, val: 0.46
    hs: 100, ni: 2000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.10000, val: 0.51
    hs: 100, ni: 1000, bs: 200, lr: 0.00010, lrd: 0.95, reg:
    0.25000, val: 0.28
    hs: 50, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg:
    0.25000, val: 0.29
    hs: 200, ni: 1000, bs: 100, lr: 0.00010, lrd: 0.95, reg:
    0.10000, val: 0.31
    hs: 200, ni: 1000, bs: 200, lr: 0.00010, lrd: 0.95, reg:
    0.50000, val: 0.30
    hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.10000, val: 0.47
    hs: 50, ni: 2000, bs: 200, lr: 0.00050, lrd: 0.95, reg:
    0.25000, val: 0.49
    hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.10000, val: 0.47
    hs: 50, ni: 1000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.10000, val: 0.47
    hs: 100, ni: 2000, bs: 200, lr: 0.00100, lrd: 0.95, reg:
    0.10000, val: 0.49
    hs: 100, ni: 1000, bs: 100, lr: 0.00050, lrd: 0.95, reg:
```

```
0.50000, val: 0.45
           Best validation accuracy: 0.505
           Best hyperparameters: {'hidden size': 100, 'num iter':
           2000, 'batch size': 200, 'learning rate': 0.001,
           'learning rate decay': 0.95, 'reg': 0.1}
In [63]:
        END OF YOUR CODE
        <network.Network object at 0x7c22a394e5f0>
In [72]:
        best net = None # store the best model into this
        best val = -1
        best stats = []
        # TODO: Tune hyperparameters using the validation set. Store your best
        # model in best net.
        # To help debug your network, it may help to use visualizations similar
        # ones we used above; these visualizations will have significant qualit
        # differences from the ones we saw above for the poorly tuned network.
        # Tweaking hyperparameters by hand can be fun, but you might find it us
        # write code to sweep through possible combinations of hyperparameters
        # automatically like we did on the previous exercises.
        # Cleaning up variables to prevent loading data multiple times
           del X train, y train
           del X test, y test
           print('Clear previously loaded data.')
        except:
           pass
        X train, y train, X val, y val, X test, y test = get CIFAR10 data()
        print('Train data shape:', X train.shape)
        print('Train labels shape:', y_train.shape)
        print('Validation data shape:', X val.shape)
        print('Validation labels shape:', y val.shape)
        print('Test data shape:', X test.shape)
        print('Test labels shape:', y test.shape)
        input size = 32 * 32 * 3
        hidden size = 100
        num classes = 10
        best net = Network(input size, hidden size, num classes)
        # Train the best network
        best stats = best net.train(X train, y train, X val, y val,
                  num iters=2000, batch size=300,
                   learning rate=1e-3, learning rate decay=0.95,
                   reg=0.25, verbose=True)
        # Predict on the validation set
```

```
pest_val = (pest_net.predict(x_val) == y_val).mean()
          print('Validation accuracy: ', best val)
        Clear previously loaded data.
        Train data shape: (49000, 3072)
        Train labels shape: (49000,)
        Validation data shape: (1000, 3072)
        Validation labels shape: (1000,)
        Test data shape: (1000, 3072)
        Test labels shape: (1000,)
        iteration 0 / 2000: loss 2.303274
        iteration 100 / 2000: loss 2.398500
        iteration 200 / 2000: loss 2.119829
        iteration 300 / 2000: loss 2.295983
        iteration 400 / 2000: loss 2.112713
        iteration 500 / 2000: loss 2.017723
        iteration 600 / 2000: loss 2.214724
        iteration 700 / 2000: loss 2.104626
        iteration 800 / 2000: loss 2.147233
        iteration 900 / 2000: loss 2.130871
        iteration 1000 / 2000: loss 2.213727
        iteration 1100 / 2000: loss 2.053128
        iteration 1200 / 2000: loss 2.051237
        iteration 1300 / 2000: loss 2.176885
        iteration 1400 / 2000: loss 2.097822
        iteration 1500 / 2000: loss 2.120195
        iteration 1600 / 2000: loss 2.109702
        iteration 1700 / 2000: loss 1.866950
        iteration 1800 / 2000: loss 2.055764
        iteration 1900 / 2000: loss 1.935185
        Validation accuracy: 0.505
In [73]:
          # Plot the loss function and train / validation accuracies
          plt.subplot(2, 1, 1)
          plt.plot(best stats['loss history'])
          plt.title('Loss history')
          plt.xlabel('Iteration')
          plt.ylabel('Loss')
          plt.subplot(2, 1, 2)
          plt.plot(best stats['train acc history'], label='train')
          plt.plot(best stats['val acc history'], label='val')
          plt.title('Classification accuracy history')
          plt.xlabel('Epoch')
          plt.ylabel('Clasification accuracy')
          plt.legend()
          plt.show()
                                            Loss history
```

