

Problem Set 5, Part I

Problem 1: Sorting practice

1-1) {2, 3, 12, 13, 34, 24, 50, 27}

1-2) {3, 13, 24, 27, 34, 2, 50, 12}

1-3) {3, 2, 13, 12, 24, 27, 34, 50}

1-4) {12, 3, 2, 13, 34, 27, 50, 24}

1-5) {2, 3, 12, 13, 34, 27, 50, 24}

1-6) {3, 13, 24, 27, 2, 34, 50, 12}

Problem 2: Practice with big-O

2-1)

function	big-O expression
$a(n) = 5n + 1$	$a(n) = O(n)$
$b(n) = 2n + 3n^2 + n\log(n)$	$b(n) = O(n^2)$
$c(n) = 5n\log(n) + 10n^3 + n^2$	$c(n) = O(n^3)$
$d(n) = 3\log(n) + 7n$	$d(n) = O(n)$
$e(n) = 8 + 9n + 4n\log(n)$	$e(n) = O(n\log n)$

2-2) $O(n)$: the inner loop is executed $O(1)$ as it is not a function of n . However, the outer loop is executed $3n-2$ times which is equivalent to $O(n)$ times. Therefore the `count()` method would be called $O(n)$ times.

2-3) $O(n^3)$: The outer loop executes at $O(n)$ as it goes from 0 to n . The inner loop alone also executes at $O(n)$ as it goes from 0 to $2n$ and Big O excludes constants. The second inner loop alone also executes at $O(n)$. Therefore `count()` will execute $O(n^3)$ times.

Problem 3: Comparing two algorithms

worst-case time efficiency of algorithm A: $O(n \log n)$

Explanation: In the worst case scenario merge sort performs at $O(n \log n)$ efficiency. This is because merge sort divides the array in half over and over therefore giving $2n$ moves per level and there are approximately $\log n$ levels. In big O, this gives $O(n \log n)$. Additionally, worst case scenario the loop in algorithm A traverses through all the way through for a total of `arr.length` times which adds another $O(n)$. This therefore gives an overall worst-case time efficiency of $O(n \log n)$

worst-case time efficiency of algorithm B: $O(n^2)$

Explanation: The worst case scenario in Algorithm B is that there are no duplicates in the array. This would mean both loops would traverse all the way through. The outer loop executes n times and the inner loop would also execute n times with n being arr.length. This therefore gives a total time complexity of n^2 and the big O notation for this is $O(n^2)$;

Problem 4: Practice with references

4-1)

Expression	Address	Value
x	0x128	0x840
x.ch	0x840	'h'
y.prev	0x326	0x400
y.next.prev	0x666	0x320
y.prev.next	0x402	0x320
y.prev.next.next	0x322	null

4-2)

```
y.prev.next=x;  
x.prev=y.prev;  
y.prev=x;  
x.next=y;
```

4-3)

```
public static void addNexts(StringNode last){  
    StringNode trav=last;  
    while(trav.prev!=null){  
        trav.prev.next=trav;  
        trav=trav.prev;  
    }  
}
```