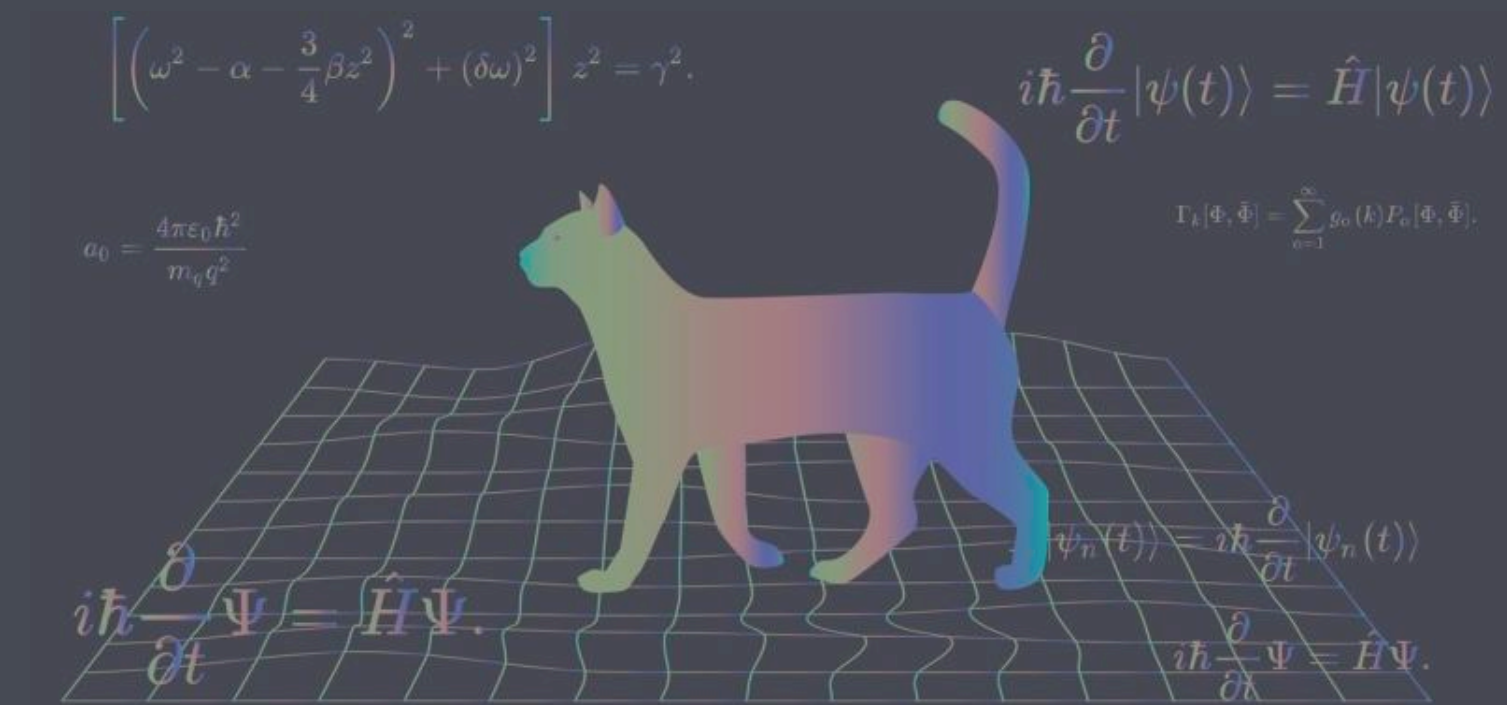


Cryptocurrency Forecasting with Quantum Machine Learning

CatsInHilbertSpace

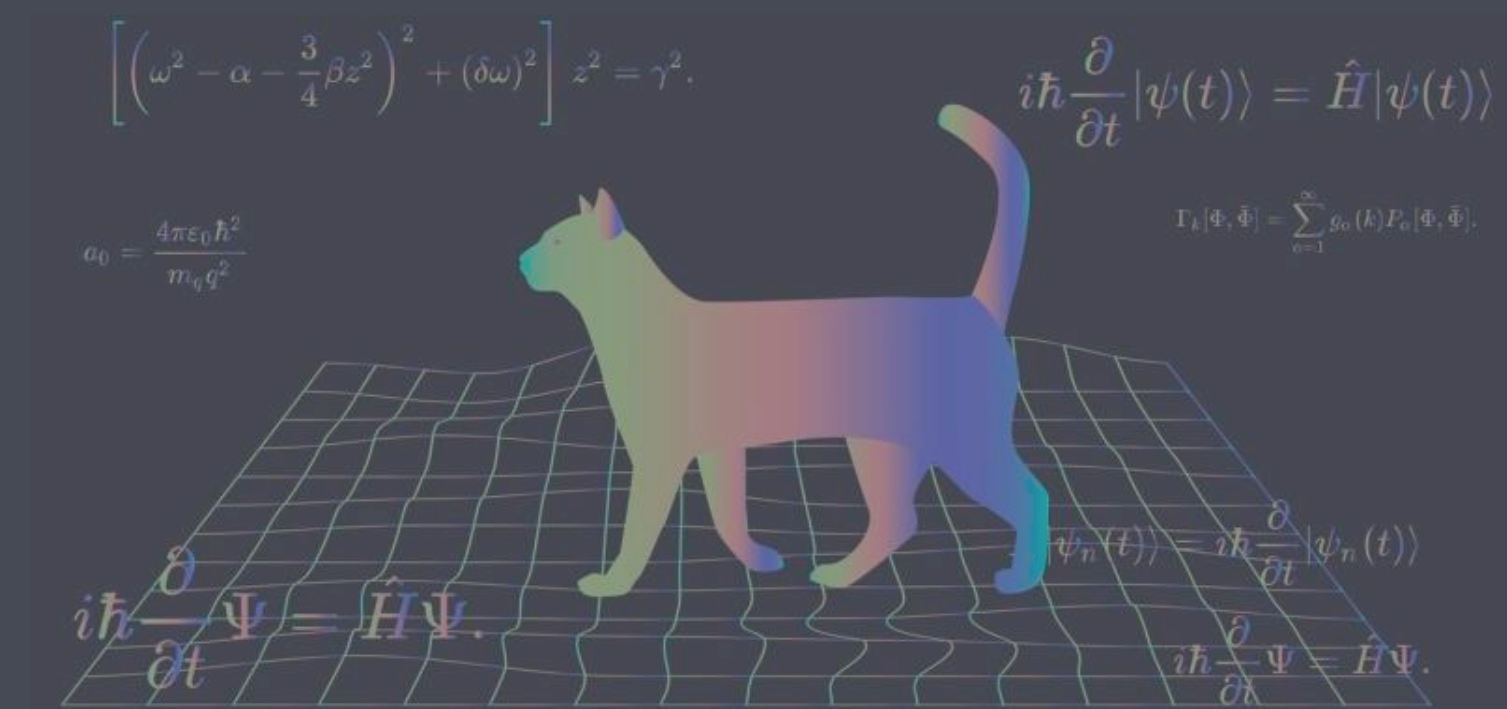
Project Overview

- The purpose of this work is to compare quantum and classical machine learning methods for time series forecasting of cryptocurrency
- In particular, this project analyzes the value of Ethereum, between 2015 and 2021. The project focuses on making near-term predictions of the open price given data from previous days
- The techniques include a classical CNN, Hybrid CNN with quantum layer, and custom quantum variational algorithm for sequences



Motivation

- Cryptocurrencies are notoriously volatile and challenging to predict
- However, there is a great financial incentive in predicting their value
- Ethereum is one of the most popular cryptocurrencies with a value that has grown drastically from \$7 in February 2016 to around \$2600 in February 2022
- This motivated forecasting the Ethereum Open price of Ethereum given data such as Open, Close, and Volume of the previous (e.g. 5) days
- The goal was to compare quantum and classical forecasting models of Ethereum

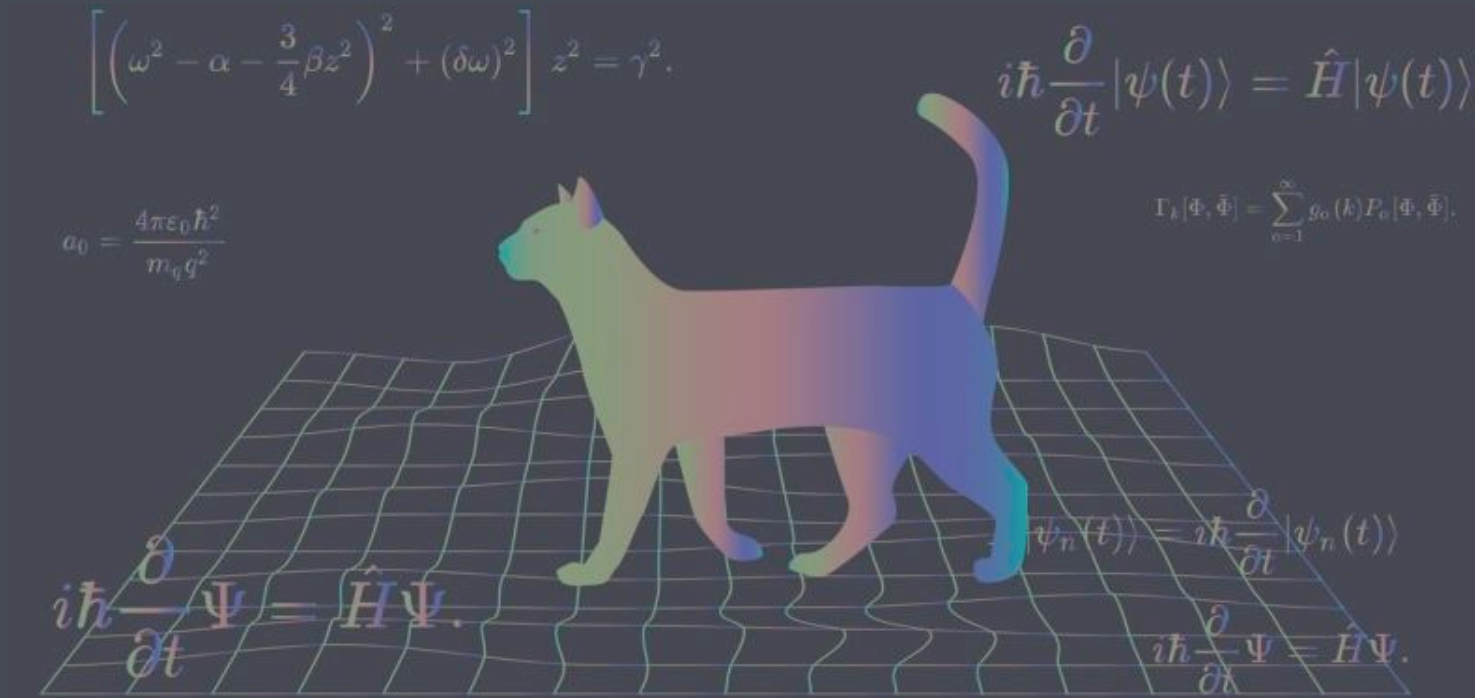


Data

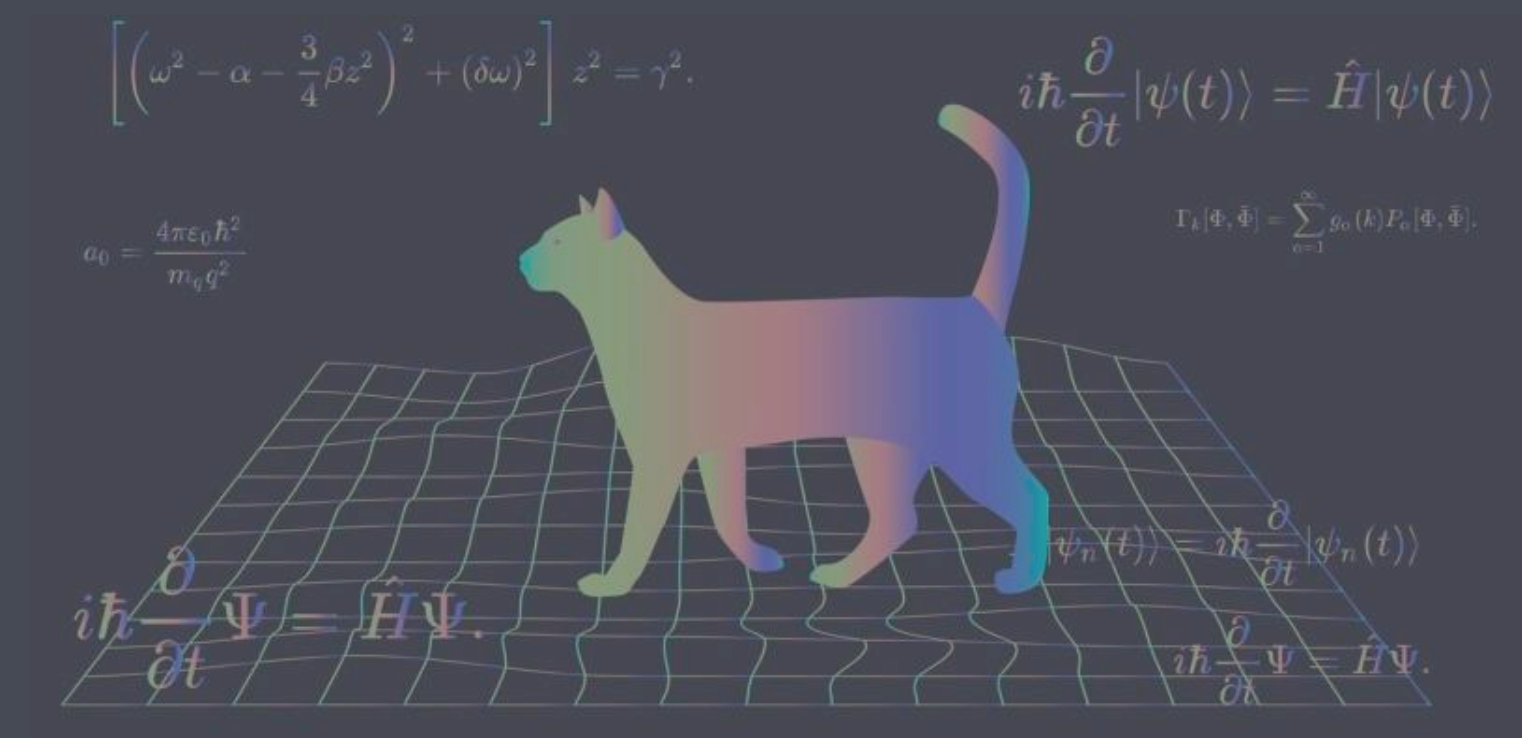
- Ethereum Data - Arpit Verma: <https://www.kaggle.com/varpit94/ethereum-data>
- This data consists of the Open, High, Low, Close, Adj Close, and Volume for each day between August 2015 to December 2021

| <div><div><div><div></div><div>Date</div></div><div></div></div></div> | <div><div><div><div></div><div># Open</div></div><div></div></div></div> | <div><div><div><div></div><div># High</div></div><div></div></div></div> | <div><div><div><div></div><div># Low</div></div><div></div></div></div> | <div><div><div><div></div><div># Close</div></div><div></div></div></div> | <div><div><div><div></div><div># Adj Close</div></div><div></div></div></div> | <div><div><div><div></div><div># Volume</div></div><div></div></div></div> |
|---|--|--|---|---|--|--|
| Date | Price from the first transaction of a trading day | Maximum price in a trading day | Minimum price in a trading day | Price from the last transaction of a trading day | Closing price adjusted to reflect the value after accounting for any corporate actions | Number of units traded in a day |
| 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| | | | | | |

| Date | Open | High | Low | Close | Adj Close | Volume |
|------------|------|------|------|-------|-----------|---------|
| 2015-08-07 | 2.83 | 3.54 | 2.52 | 2.77 | 2.77 | 164329 |
| 2015-08-08 | 2.79 | 2.8 | 0.71 | 0.75 | 0.75 | 674188 |
| 2015-08-09 | 0.71 | 0.88 | 0.63 | 0.7 | 0.7 | 532170 |
| 2015-08-10 | 0.71 | 0.73 | 0.64 | 0.71 | 0.71 | 405283 |
| 2015-08-11 | 0.71 | 1.13 | 0.66 | 1.07 | 1.07 | 1463100 |
| 2015-08-12 | 1.06 | 1.29 | 0.88 | 1.22 | 1.22 | 2150620 |
| 2015-08-13 | 1.22 | 1.97 | 1.17 | 1.83 | 1.83 | 4068680 |
| 2015-08-14 | 1.81 | 2.26 | 1.75 | 1.83 | 1.83 | 4637030 |
| 2015-08-15 | 1.8 | 1.88 | 1.57 | 1.69 | 1.69 | 2554360 |
| 2015-08-16 | 1.68 | 1.7 | 1.09 | 1.57 | 1.57 | 3550790 |
| 2015-08-17 | 1.58 | 1.58 | 1.19 | 1.2 | 1.2 | 1942830 |
| 2015-08-18 | 1.22 | 1.33 | 1.09 | 1.09 | 1.09 | 1485680 |
| 2015-08-19 | 1.17 | 1.32 | 1.17 | 1.26 | 1.26 | 1486240 |
| 2015-08-20 | 1.25 | 1.53 | 1.25 | 1.46 | 1.46 | 2843760 |
| 2015-08-21 | 1.48 | 1.56 | 1.35 | 1.4 | 1.4 | 2020970 |
| 2015-08-22 | 1.4 | 1.48 | 1.35 | 1.38 | 1.38 | 948310 |



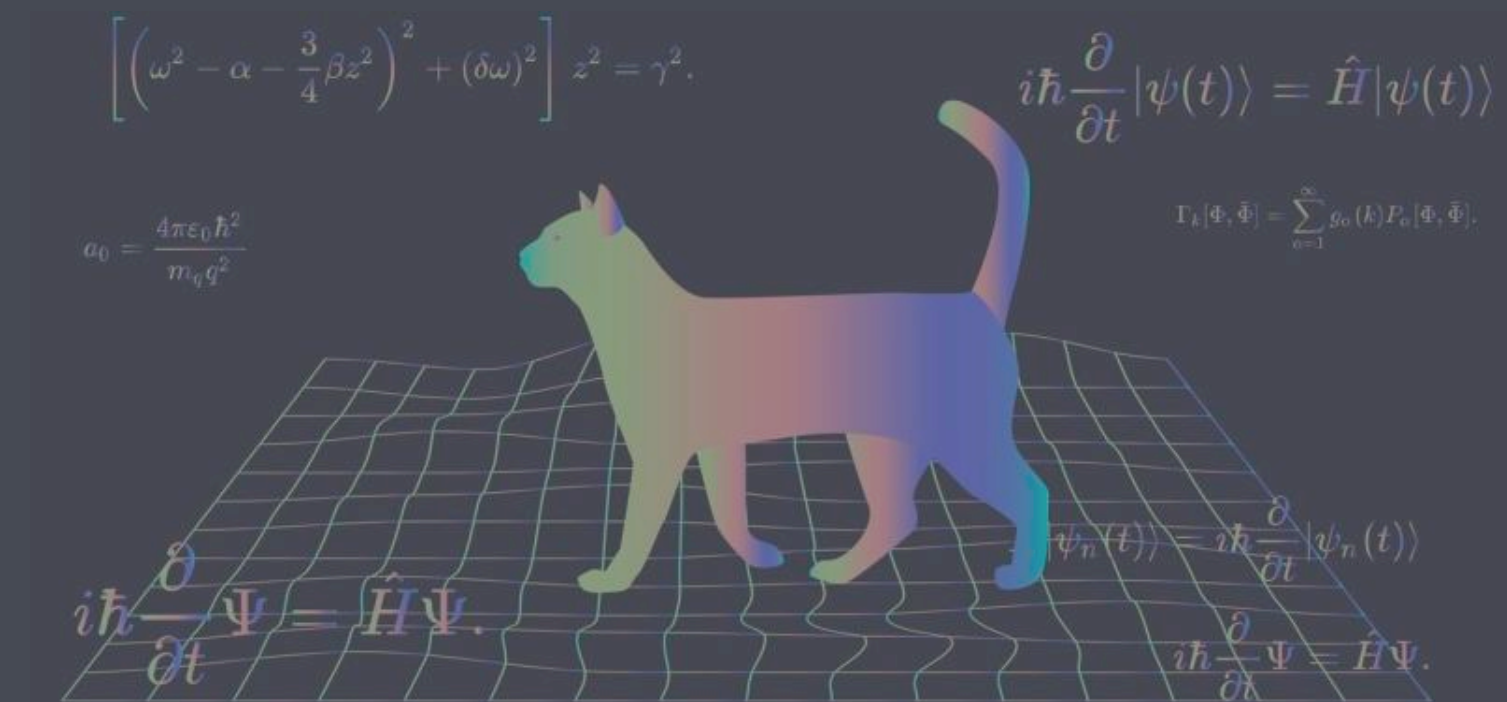
Algorithms



- **CNN:** Convolutional Neural Network
 - Primarily used in processing image data, but also proven useful and efficient in sequential data using 1D convolutional layers
 - Used two 1D convolutional layers followed by max pooling layers, and ending with two dense layers
- **Hybrid CNN:** Convolutional Neural Network with one-two quantum layers
 - Same structure as CNN but replaced one dense layer with one-two quantum layers
 - Quantum layer includes angle embedding of features and different circuit structures, such as PennyLane's defined strongly entangled layers
- **Variational Algorithm:** Custom variational algorithm
 - Circuit iterates over sequence, embedding each previous date's data with an angle embedding of the features into the six qubits and using similar circuit structures as in Hybrid CNN

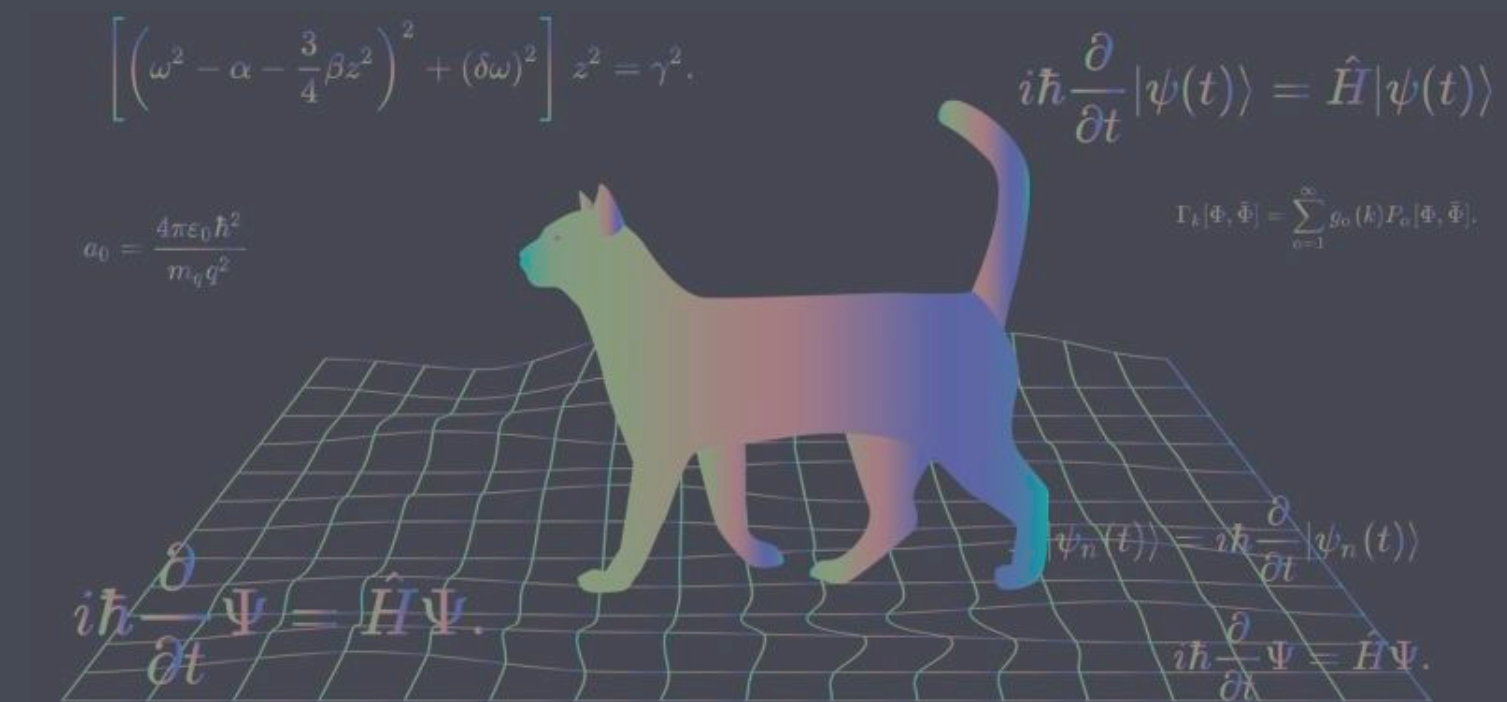
Software & Services

- **PennyLane**: for the Hybrid CNN and Variational Algorithm
- **Braket**: for running on simulators
- **Torch**: for CNN and Hybrid CNN
- **Scikit-Learn**: for preprocessing data
- **Matplotlib**: for plotting data
- **Pandas** and **Numpy**: for representing data

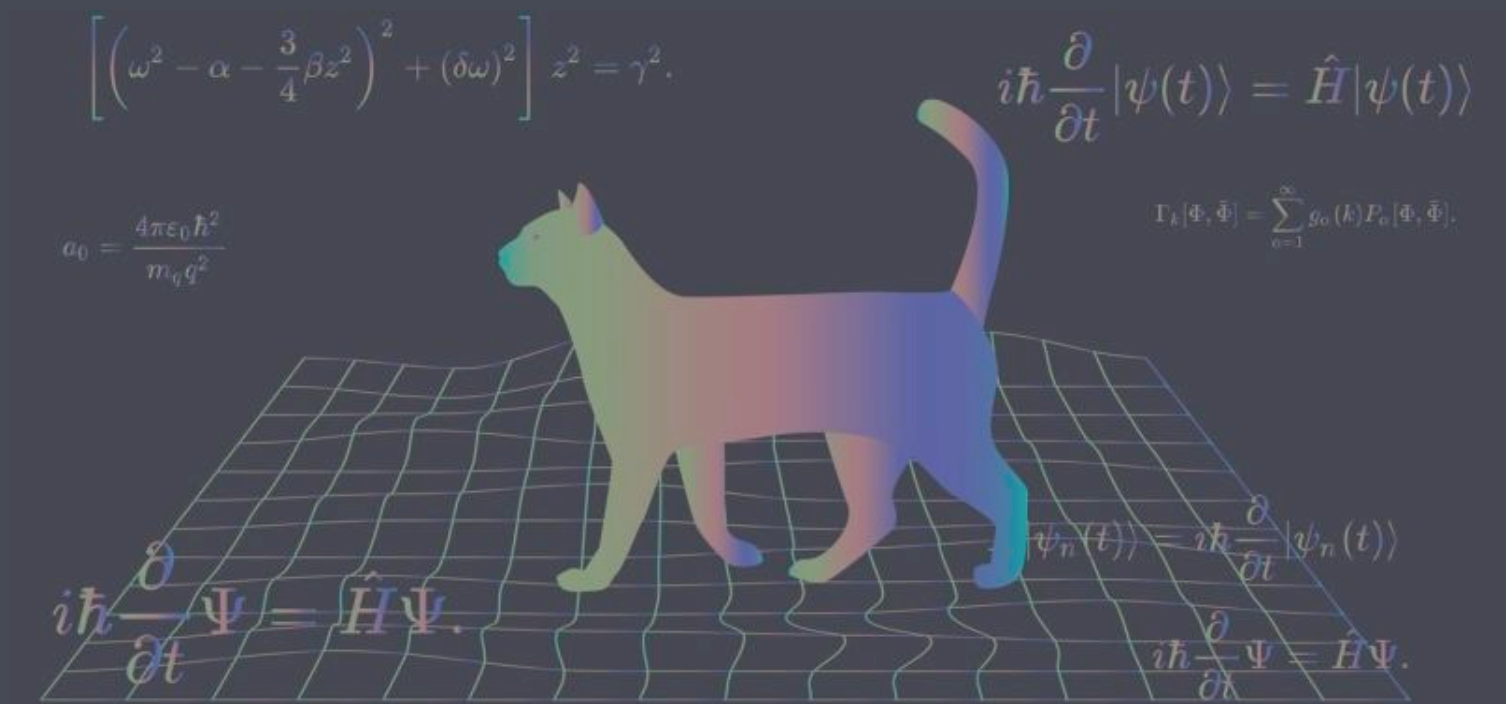


Procedure

- **Read:** read data in as pandas dataframe
- **Preprocess:** basic preprocessing, including standardizing the features, scaling y between 0 and 1, and reshaping data.
- **Train:** optimize square loss comparing training batch processed predictions and true values
- **Test:** compare square loss of predictions and true values
- **Write:** write results to csv file, including information about parameters
- **Plot:** plot results in several formats, comparing different model predictions



Plot 1: Local Simulator CNN (+ Quantum)



■ Overall

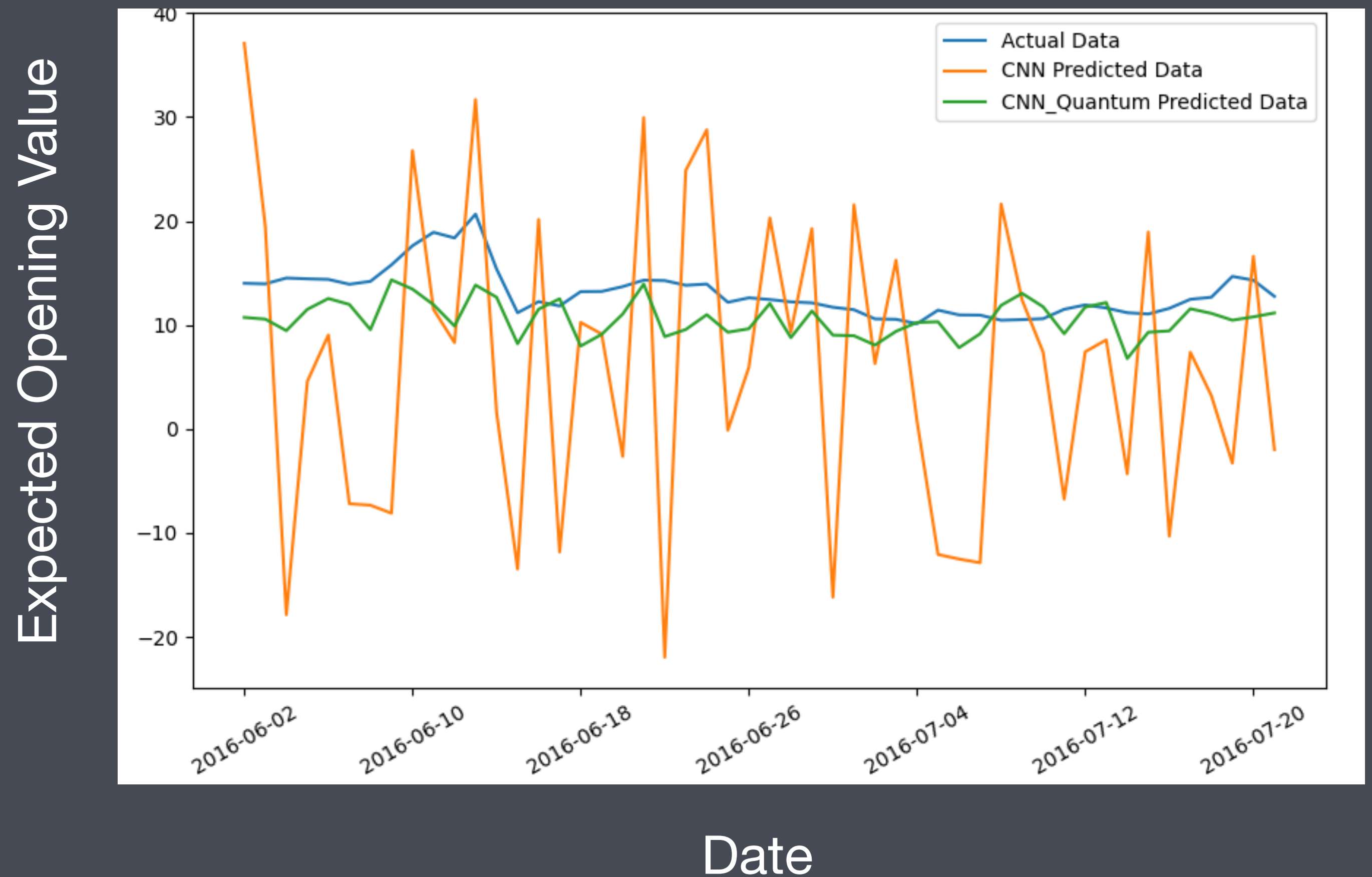
- Size: Train: 100 samples, Test: 50
- Iterations: 1000, Batch Size: 10
- CNN Layers Out Channels: 128, 64
- Lookback: 5

■ CNN

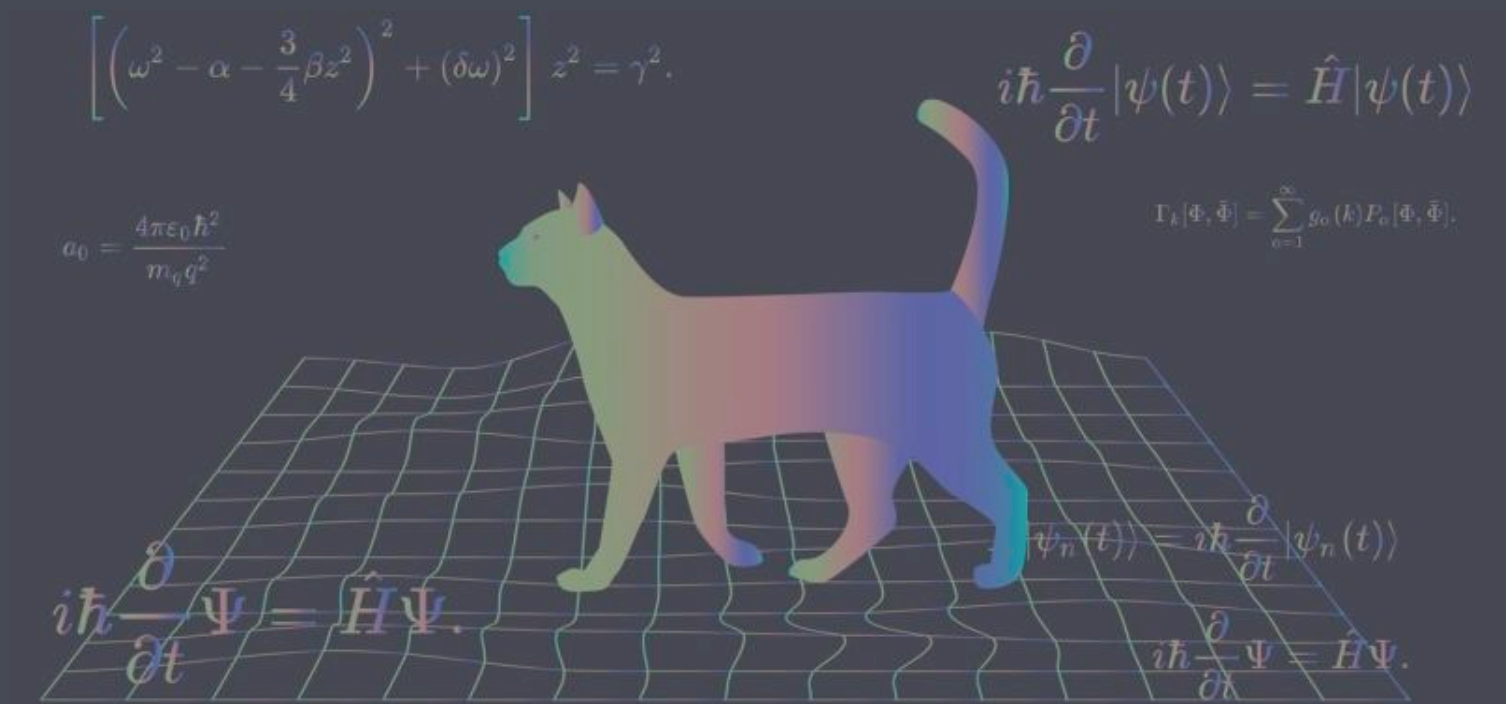
- Times: Train: 1.94s, Test: .002
- Loss: Train: 9.45e-7, Test: 1.05e-5

■ CNN+Quantum

- Times: Train: 776.82s, Test: 2.44
- Loss: Train: 1.03e-7, Test: 4.67e-7



Plot 2: Local Simulator CNN (+ Quantum)



■ Overall

- Size: Train: 100 samples, Test: 50
- Iterations: 1000, Batch Size: 5
- CNN Layers Out Channels: 128, 64
- Lookback: 4

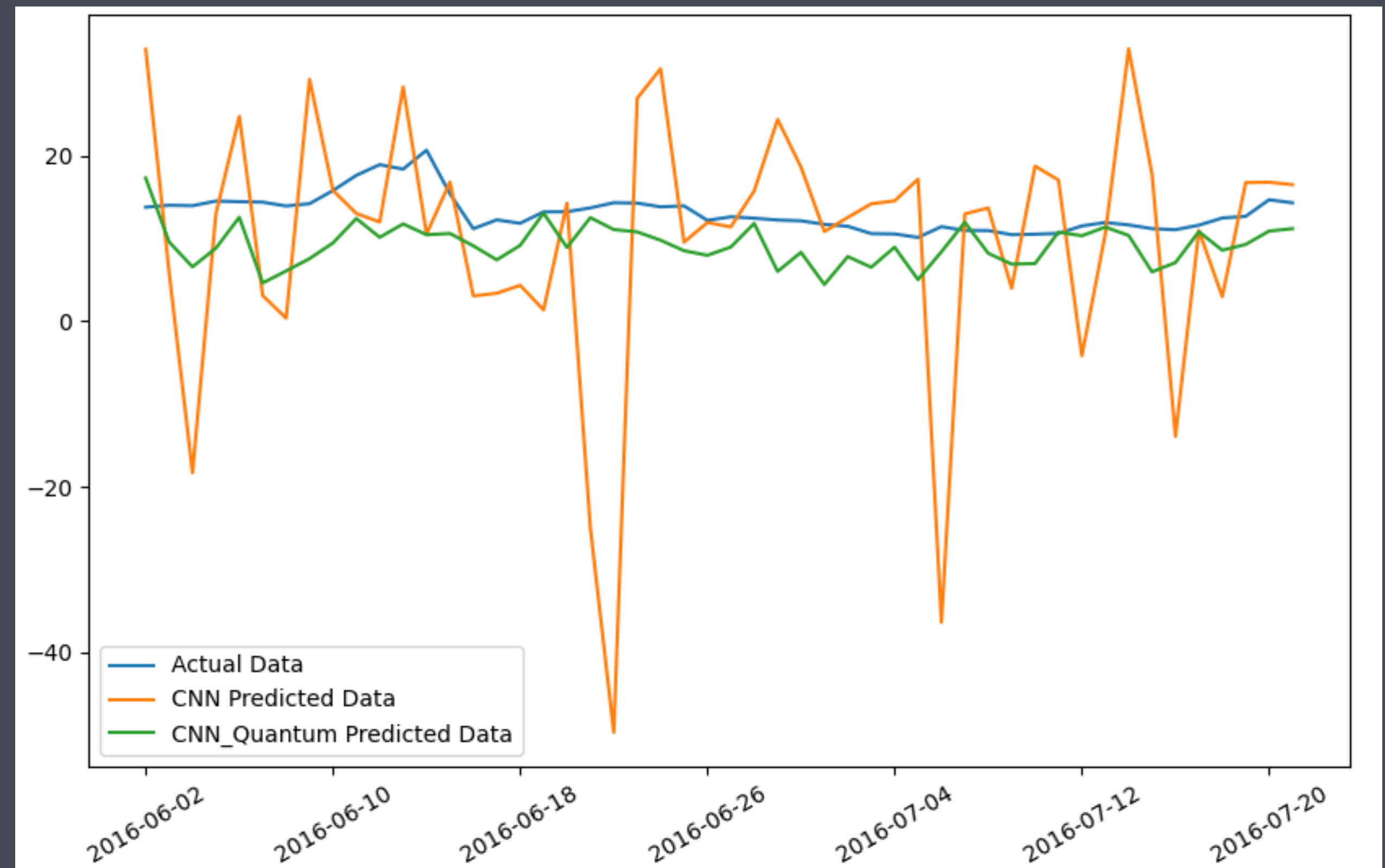
■ CNN

- Times: Train: 4.69s, Test: .002
- Loss: Train: 9.97e-07, Test: 1.123e-05

■ CNN+Quantum

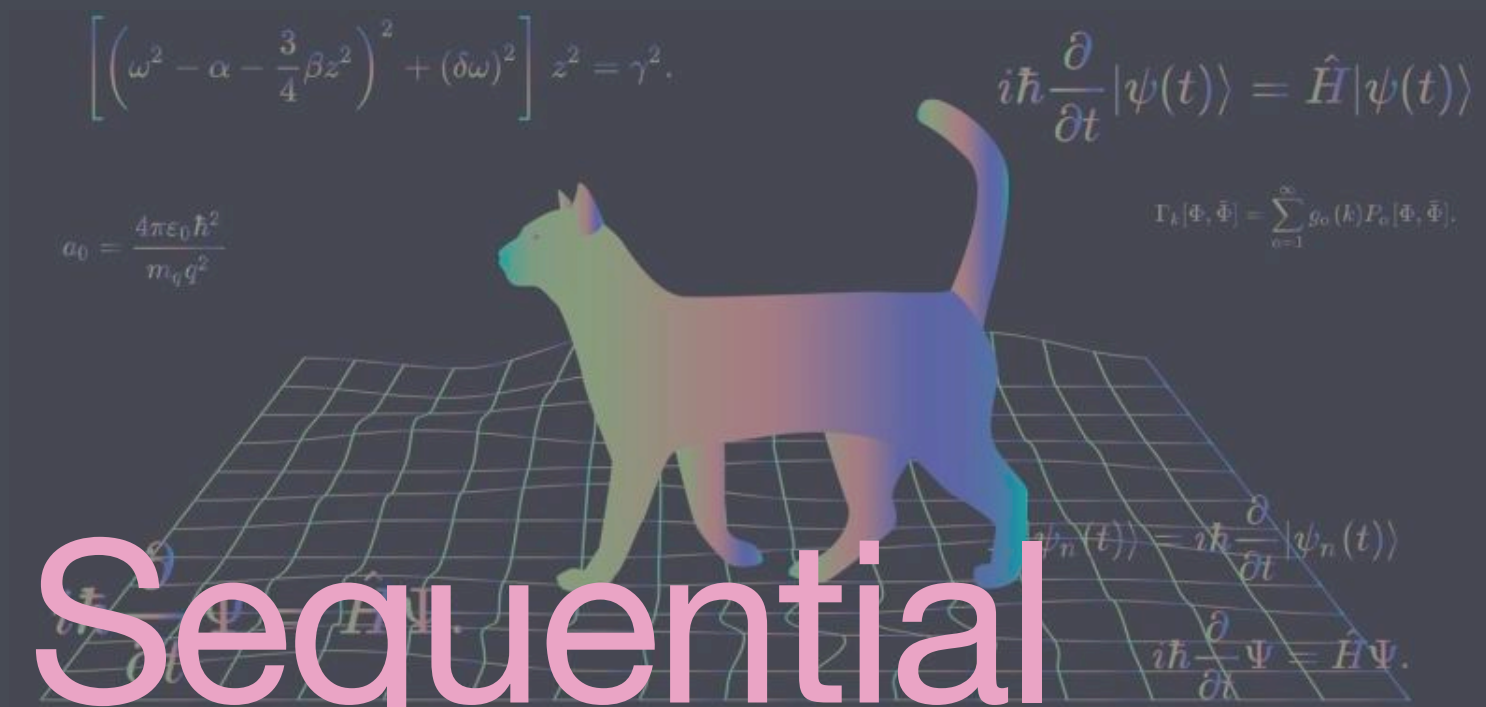
- Times: Train: 154.53, Test: 0.86
- Loss: Train: 1.30e-07, Test: 9.49e-07

Expected Opening Value



Date

Plot 3: Local Simulator CNN (+ Quantum) & Custom Variational Sequential



■ Overall

- Size: Train: 100 samples, Test: 50
- Iterations: 1000 (100 for Variational), Batch Size: 10
- CNN Layers Out Channels: 64, 32
- Lookback: 5

■ CNN

- Times: Train: 3.74s, Test: .002
- Loss: Train: 4.55e-6, Test: 0.00012

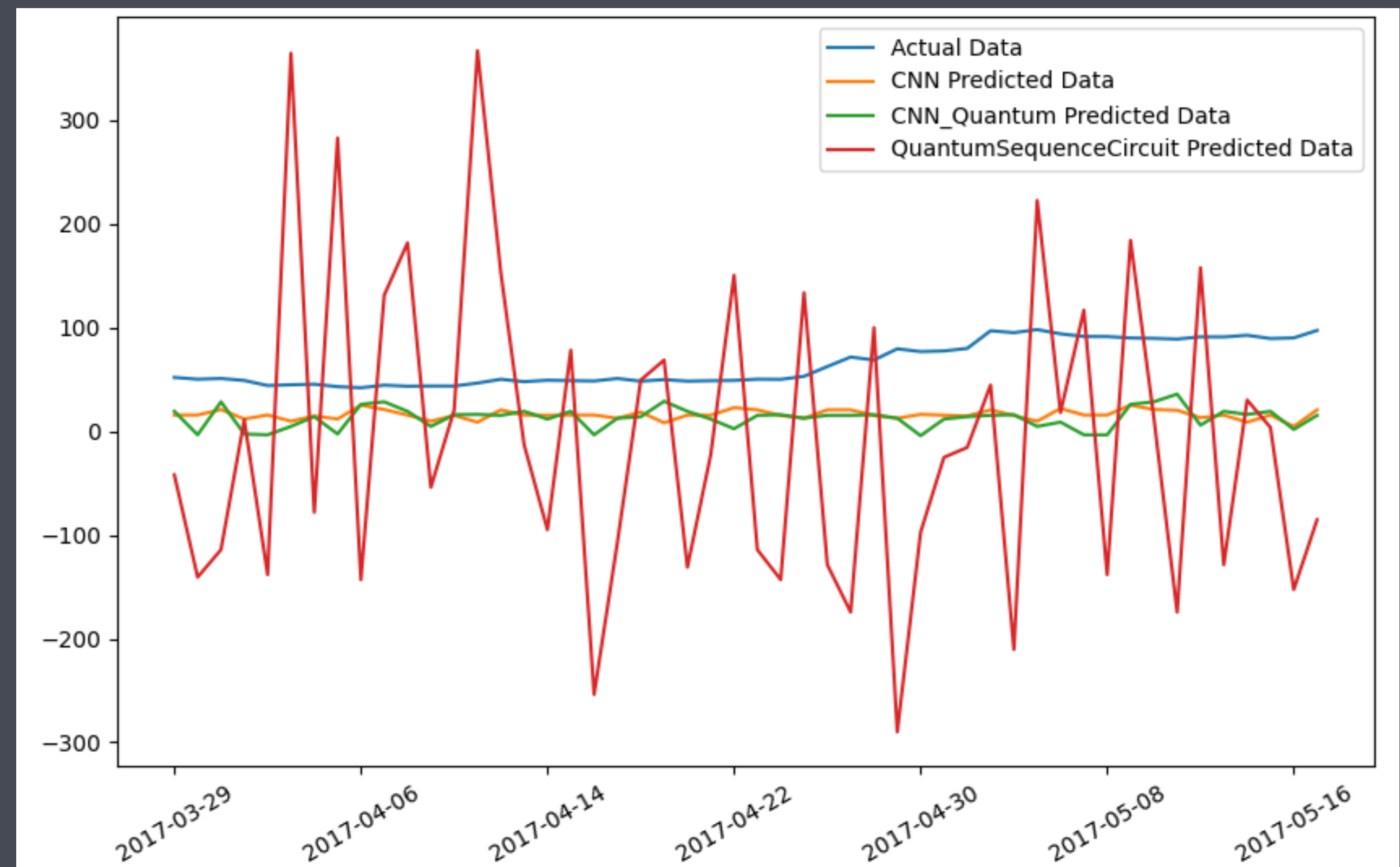
■ CNN+Quantum

- Times: Train: 152.61s, Test: .833
- Loss: Train: 1.85e-5, Test: 0.000138

■ Custom Variational Sequential

- Times: Train: 395.17s, Test: 0.35
- Loss: Train: 0.005, Test: 0.002

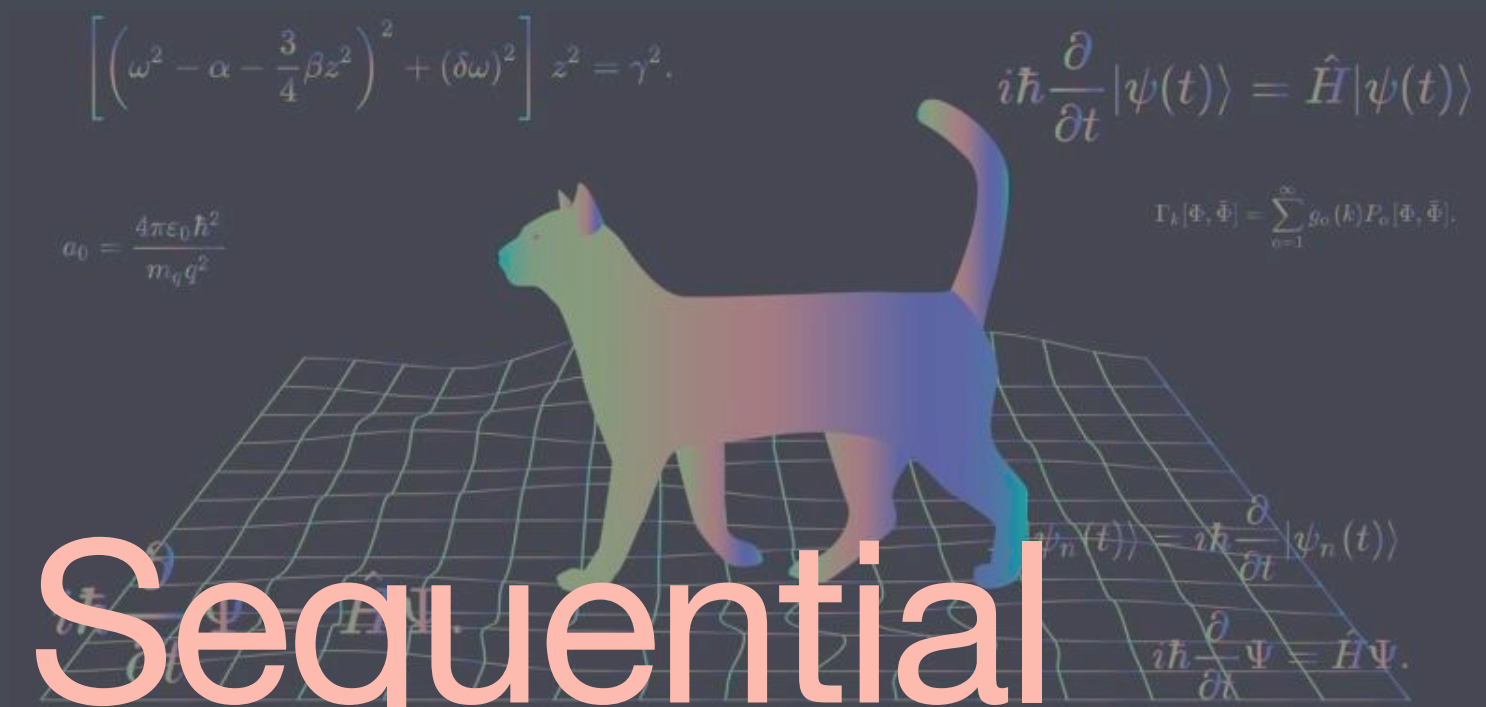
Expected Opening Value



*Note the later start date

Date

Plot 4: Local Simulator CNN (+ Quantum) & Custom Variational Sequential



■ Overall

- Size: Train: 50 samples, Test: 25
- Iterations: 1000 (100 for Variational), Batch Size: 5
- CNN Layers Out Channels: 64, 32
- Lookback: 4

■ CNN

- Times: Train: 4.15s, Test: .002
- Loss: Train: 1.06e-6, Test: 0.00024

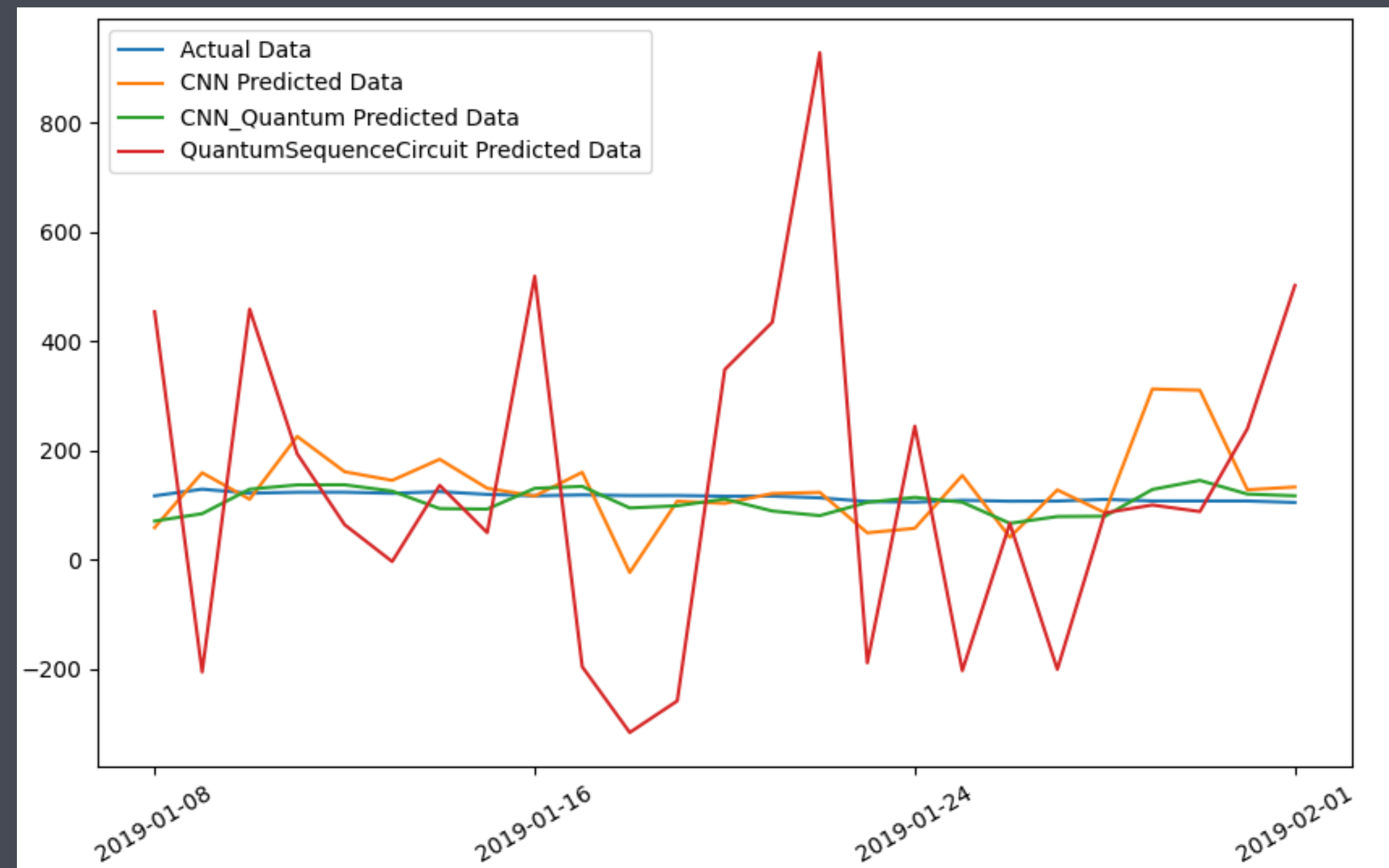
■ CNN+Quantum

- Times: Train: 157.44s, Test: .423
- Loss: Train: 1.28e-6, Test: 2.60e-5

■ Custom Variational Sequential

- Times: Train: 2714s*, Test: .0.438
- Loss: Train: 0.003, Test: 0.004

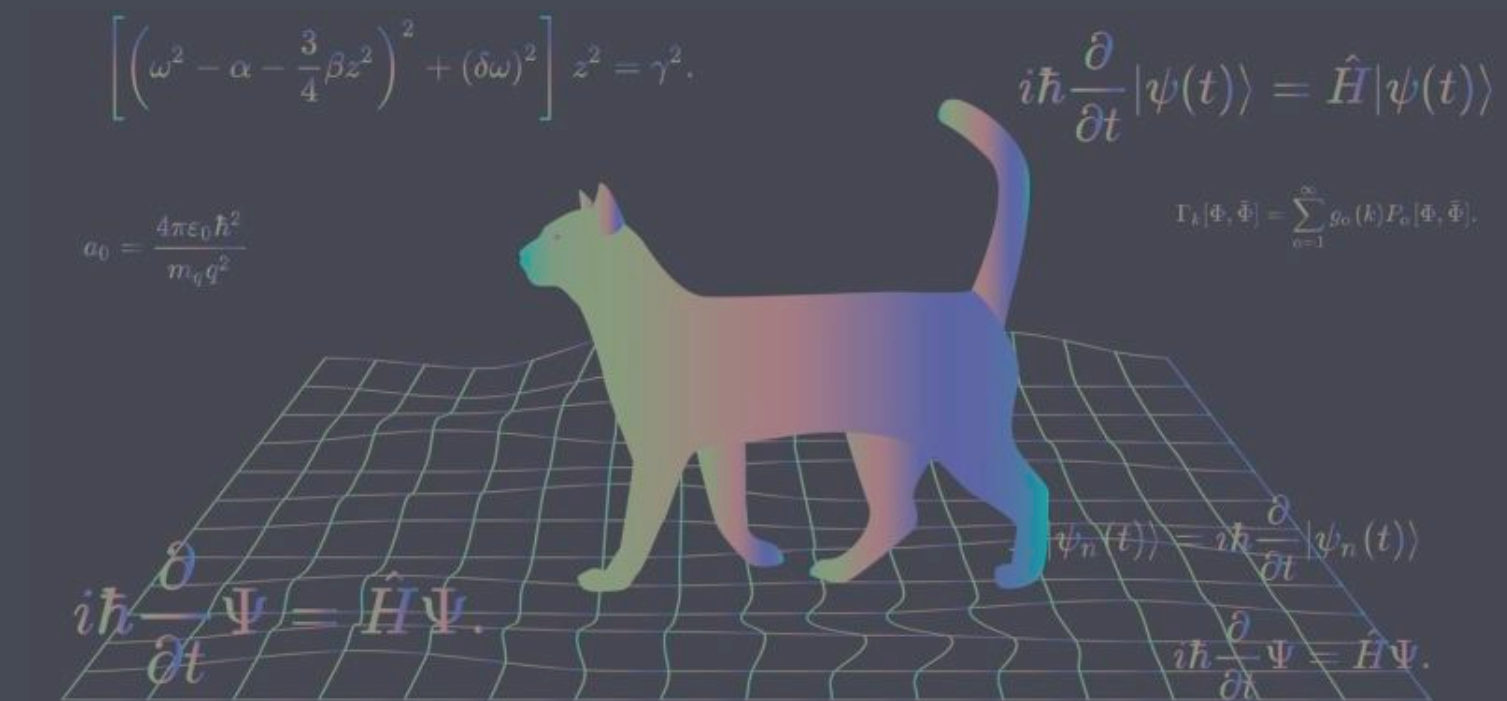
Expected Opening Value



*Compute was training other modes simultaneously

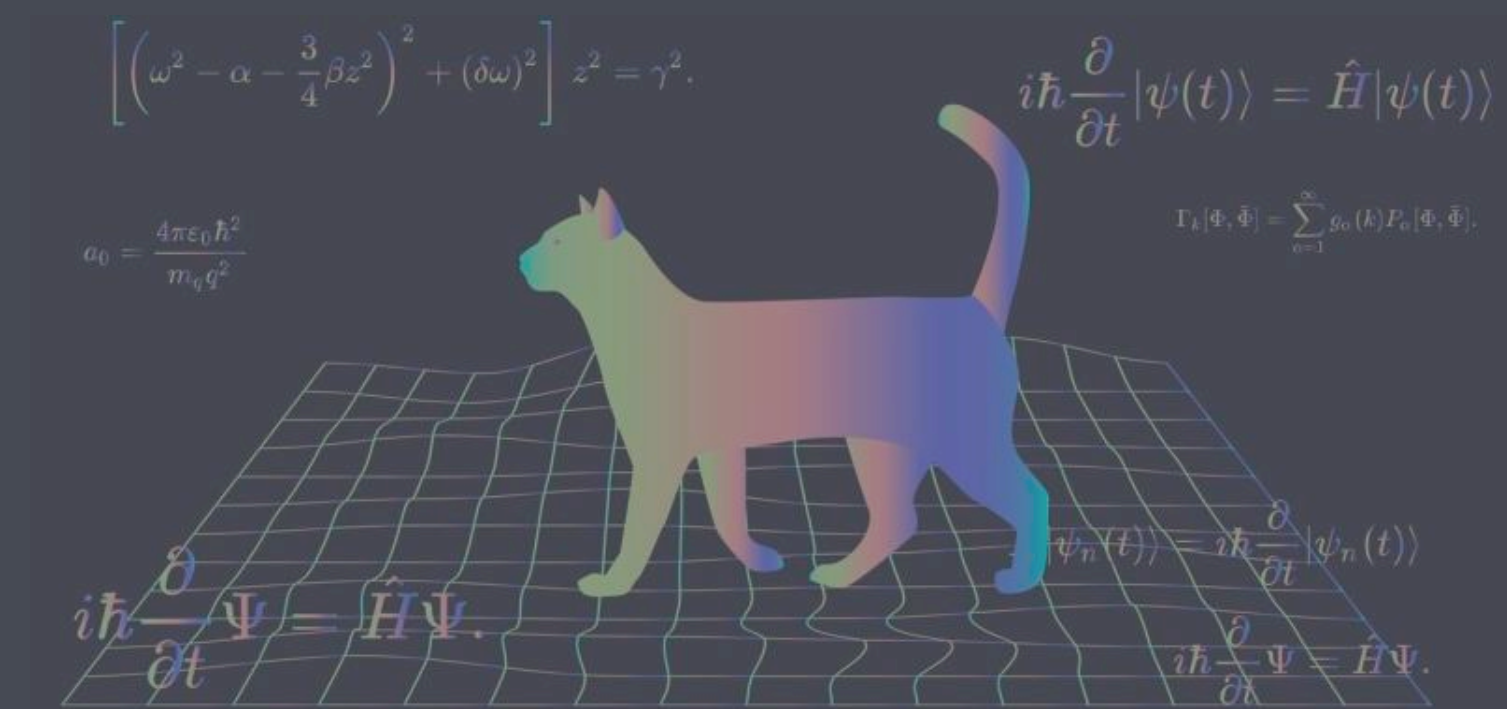
Date

Overall Trends



- Overall, non-quantified trends that were observed from the different parameter choices and train and test sizes. The following rankings were observed:
- **Best performance** (testing square loss)
 1. Hybrid CNN + Quantum
 2. CNN
 3. Custom Variational Sequential
- **Fastest** (test and train times)
 1. CNN
 2. Hybrid CNN + Quantum
 3. Custom Variational Sequential

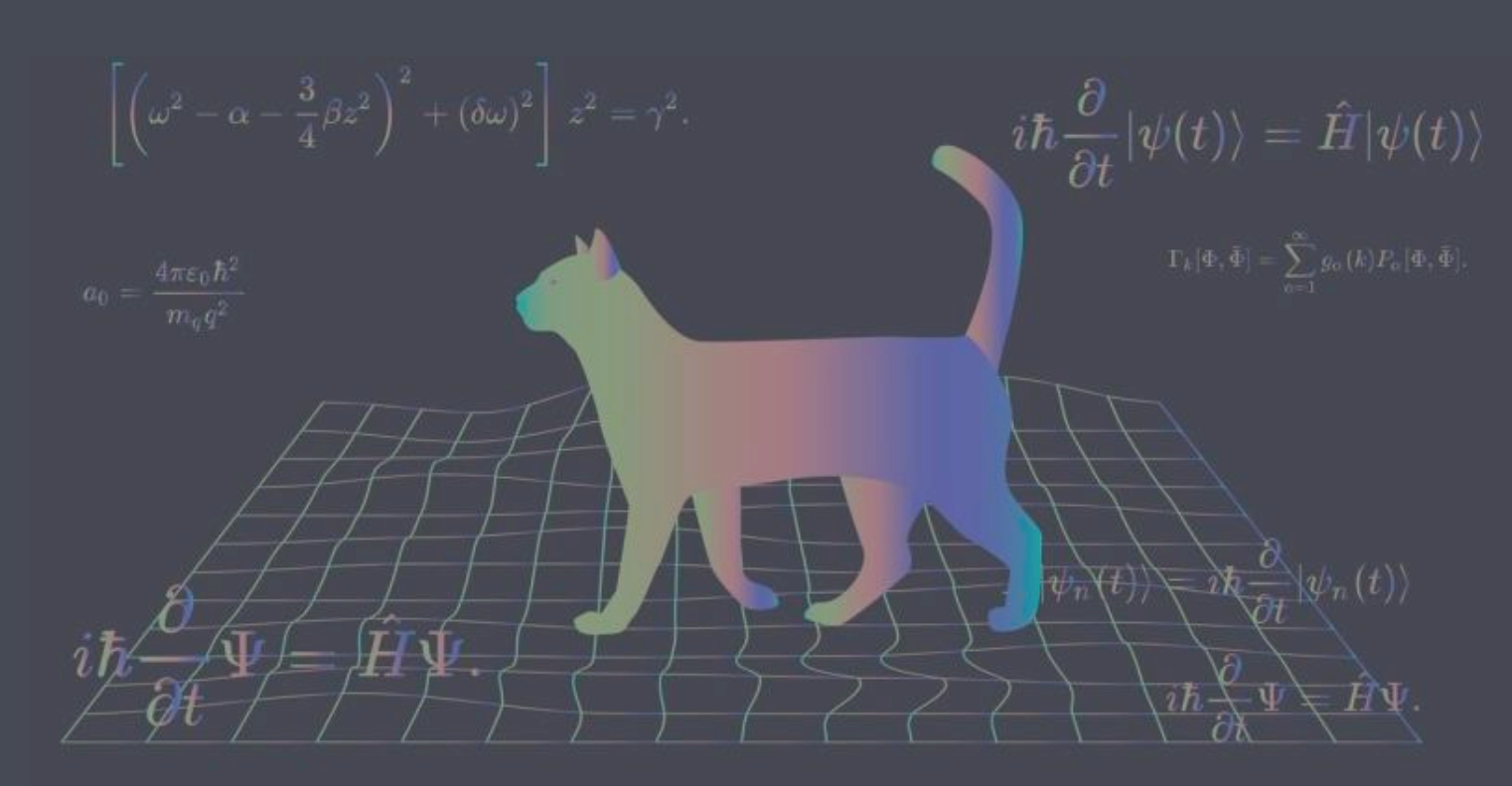
Discussion



- There is a potential performance benefit to incorporating quantum layers
- The hybrid algorithm with quantum and classical layers outperforms the customized sequential model, and in many cases, the classical CNN as well
- At later dates, the value of the cryptocurrency was more difficult to predict than earlier dates
- Due to time constraints, although the models were run on Braket QPU and Simulators, the runs did not terminate in time to plot their results

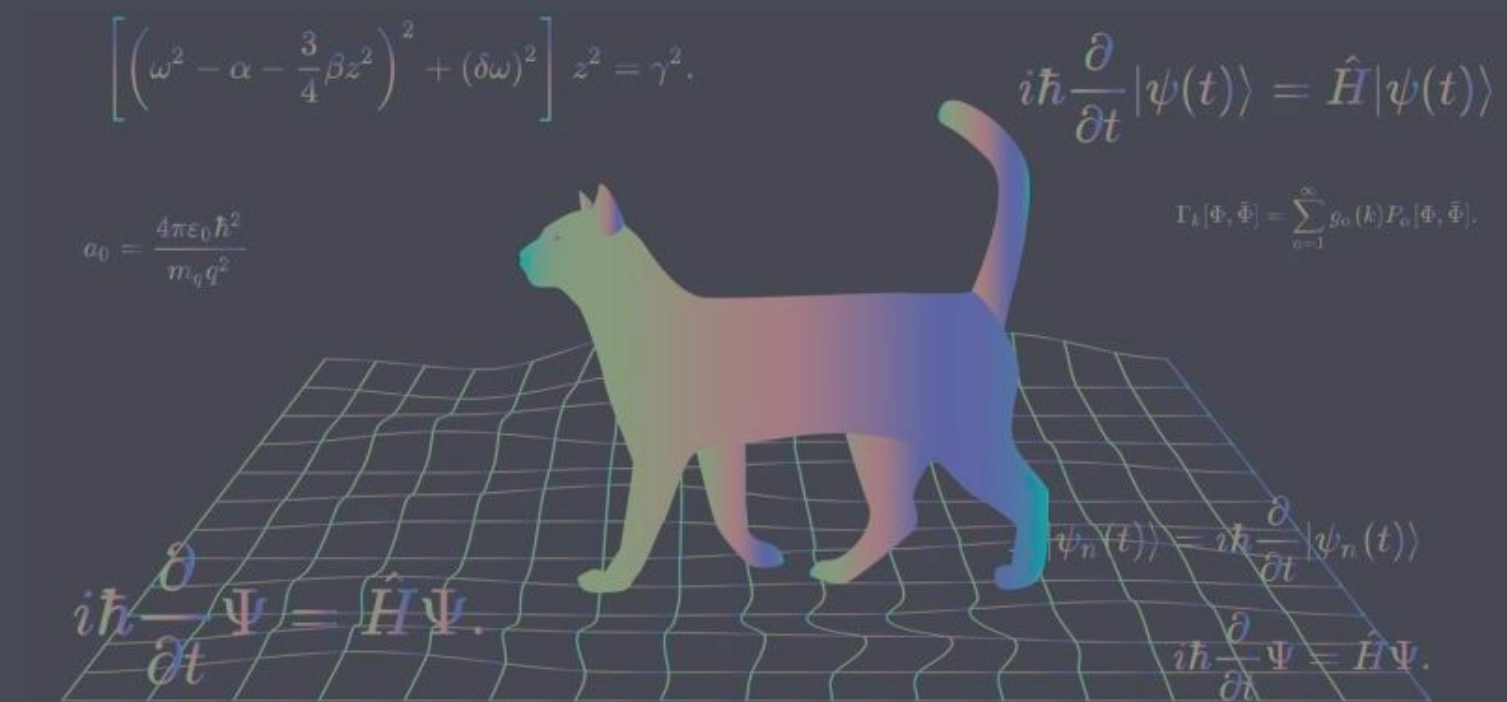
Conclusion

- Forecasting cryptocurrency prices is an important and challenging problem
- This project focused on smaller training and testing sizes, using recent data to make predictions about the near future
- Two quantum and one classical algorithm were used to forecast cryptocurrency prices
- The customized sequential quantum model was much slower to run and did not perform as well as the other two algorithms
- The hybrid quantum and CNN algorithm did perform well, at many points better than the purely classical CNN, indicating a performance benefit to incorporating quantum layers



Future Work

- Implement more classical and quantum algorithms, particularly recurrent algorithms such as LSTM and QRNN
- Continue to explore different parameter choices and layer structures to improve models
- Run on Braket QPUs, and use more shots
- Use different cryptocurrencies
- Predict different features e.g. Close price



Sources

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