

2. Given another system,  $B\mathbf{r} = \mathbf{t}$ ,

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$$\begin{aligned} \textcircled{1} &: \begin{bmatrix} 4 & 6 & 2 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9 \end{bmatrix} \\ \textcircled{2} &: \begin{bmatrix} 3 & 4 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 7 \end{bmatrix} \\ \textcircled{3} &: \begin{bmatrix} 2 & 8 & 13 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 2 \end{bmatrix} \end{aligned}$$

We wish to convert this to echelon form, by using elimination. Starting with the first row,  $\textcircled{1}$ , if we divide the whole row by 4, then the top-left element of the matrix becomes 1,

$$\begin{aligned} \textcircled{1}' &: \begin{bmatrix} 1 & 3/2 & 1/2 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \end{bmatrix} \\ \textcircled{2}' &: \begin{bmatrix} 3 & 4 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 7 \end{bmatrix} \\ \textcircled{3}' &: \begin{bmatrix} 2 & 8 & 13 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 2 \end{bmatrix} \end{aligned}$$

Next, we need to fix the second row. This results in the following,

$$\begin{aligned} \textcircled{1}'' &: \begin{bmatrix} 1 & 3/2 & 1/2 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \end{bmatrix} \\ \textcircled{2}'' &: \begin{bmatrix} 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} -1/2 \end{bmatrix} \\ \textcircled{3}'' &: \begin{bmatrix} 2 & 8 & 13 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 2 \end{bmatrix} \end{aligned}$$

What steps did we take?

- ☒ The new second row,  $\textcircled{2}''$  is the old second row minus three times the old first row, then all multiplied by -2, i.e.,  $\textcircled{2}'' = [\textcircled{2}' - 3\textcircled{1}'] \times (-2)$ .
- ☐ The new second row,  $\textcircled{2}''$  is the old second row minus three, i.e.,  $\textcircled{2}'' = \textcircled{2}' - 3$ .
- ☐ The new second row,  $\textcircled{2}''$  is the old second row minus two times the old first row, i.e.,  $\textcircled{2}'' = [\textcircled{2}' - 2\textcircled{1}']$ .
- ☐ The new second row,  $\textcircled{2}''$  is the old second row divided by four minus the old first row, i.e.,  $\textcircled{2}'' = \textcircled{2}'/4 - \textcircled{1}'$ .

☒ **Correcto**

We've made the new second row a linear combination of previous rows.

3. From the previous question, our system is almost in echelon form.

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$$\begin{array}{l} \textcircled{1}'' \\ \textcircled{2}'' \\ \textcircled{3}'' \end{array} \begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 2 & 8 & 13 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ 2 \end{bmatrix}$$

Fix row 3 to be a linear combination of the other two. What is the echelon form of the system?

☒  $\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ 0 \end{bmatrix}$

☐  $\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ 1/2 \end{bmatrix}$

☐  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ -1/4 \end{bmatrix}$

☐  $\begin{bmatrix} 1 & 3/2 & 1/2 \\ 0 & 1 & 1 \\ 0 & 5 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 9/4 \\ -1/2 \\ -5/2 \end{bmatrix}$

☒ **Correcto**

This system is now in echelon form.

4. Taking your answer from the previous part, use back substitution to solve the system.

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What is the value of  $\begin{bmatrix} a \\ b \\ c \end{bmatrix}$ ?

☒  $\mathbf{r} = \begin{bmatrix} 3 \\ -1/2 \\ 0 \end{bmatrix}$

☐  $\mathbf{r} = \begin{bmatrix} 9/4 \\ -1/2 \\ 0 \end{bmatrix}$

☐  $\mathbf{r} = \begin{bmatrix} 3/2 \\ 1/2 \\ 1 \end{bmatrix}$

☐  $\mathbf{r} = \begin{bmatrix} 9 \\ 7 \\ 2 \end{bmatrix}$

☒ **Correcto**  
Well done!

5. Let's return to the apples and bananas from Question 1.

Take your answer to Question 1 and convert the system to echelon form. I.e.,

$$\begin{bmatrix} 1 & A'_{12} & A'_{13} \\ 0 & 1 & A'_{23} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} s'_1 \\ s'_2 \\ s'_3 \end{bmatrix}.$$

Find values for  $A'$  and  $s'$ .