



RIGA TECHNICAL UNIVERSITY

**FACULTY OF COMPUTER SCIENCE AND INFORMATION
TECHNOLOGY**

INSTITUTE OF APPLIED COMPUTER SYSTEMS

**Introduction to Operations Research
Assignment 6
Linear Programming**

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➤ Task

Data input:

- User stories code names (R.01, R.02, etc.)
- Sprints names (Sprint 1, Sprint 2, etc.)
- User story profitability
- User story points
- Sprint capacity
- User story interdependencies

Decision variables:

- What user stories can we fit in each sprint, by also taking into account their interdependencies?

Objective function:

- Maximize user story profitability.

Constraints:

- The total amount of user stories' points cannot exceed the sprint capacity.
- One user story can only be associated to one sprint (one sprint can have multiple user stories).
- If a user story (US_1) depends on an user story (US_2), then US_2 should be included in a sprint before or in the same sprint as US_1.

Example:

- Sprint 3: US_2 *or* Sprint 3: US_2, US_1
 - Sprint 4: US_1
-
- The interdependencies file is update to eliminate symmetry.
 - You consider only interdependencies among user stories included in your variant.
 - User stories are defined in Latvian. If you want to understand these then use Google Translate.
 - LinearProgramingHomeWork_variants.xlsx contains variant number for each student.
 - Sprint capacity and user story sizes are in the OperationsResearch.zip file.
 - Please take the Word document corresponding to you variant number.

➤ Answer

• My Variants (13)

Sprinta Nr.	1	2	3	4	5	6
Kapacitate p_i^{\max}	30	20	15	15	20	20

User Story	Rentabilitate U_j (10-100)	Story point P_j (1-10)
R.01	100	8
R.02	100	7
R.06	60	2
R.07	60	6
R.08	30	6
R.09	40	4
R.10	35	4
R.12	80	7
R.13	80	10
R.14	75	6
R.15	70	7
R.16	60	8
R.17	20	3
R.18	20	5
R.19	30	6
R.20	15	6
R.31	75	8
R.32	40	6

• Code in CPLEX Model File

```
{string} story = ...;
{string} sprint = ...;

float Sprint_Capacity[sprint] = ...;
float Profitability[story] = ...;
float User_Story_Points[story] = ...;
float Interdependencies[story][story] = ...;

dvar int+ matrix[sprint][story];

maximize
    sum(i in sprint, j in story)
        Profitability[j] * matrix[i][j];

subject to {
    forall(i in sprint)
        sum(j in story)
            User_Story_Points[j] * matrix[i][j] <= Sprint_Capacity[i];

    forall(i in story)
        sum(j in sprint)
            matrix[j][i] <= 1;

    forall(i in sprint)
        forall(j in story)
            forall(k in story: k < j)
                matrix[i][j] + Interdependencies[j][k] - matrix[i][k] <= 1;
}
```

- Code in CPLEX Data File

```
SheetConnection Sheet("CourseWork_Interdependences.xlsx");
story from SheetRead(Sheet, "'Sheet1'!A2:A19");
sprint from SheetRead(Sheet, "'Sheet1'!C20:H20");
Sprint_Capacity from SheetRead(Sheet, "'Sheet1'!C21:H21");
Profitability from SheetRead(Sheet, "'Sheet1'!C22:T22");
User_Story_Points from SheetRead(Sheet, "'Sheet1'!C23:T23");
Interdependencies from SheetRead(Sheet, "'Sheet1'!C2:T19");
```

- Screenshots

- CPLEX Model

```
1 /*****
2  * OPL 22.1.1.0 Model
3  * Author: Emir
4  * Creation Date: 1 Apr 2023 at 02:02:59
5  *****/
6
7 {string} story = ...;
8 {string} sprint = ...;
9
10 float Sprint_Capacity[sprint] = ...;
11 float Profitability[story] = ...;
12 float User_Story_Points[story] = ...;
13 float Interdependencies[story][story] = ...;
14
15 dvar int+ matrix[sprint][story];
16
17 maximize
18   sum(i in sprint, j in story)
19     Profitability[j] * matrix[i][j];
20
21 subject to {
22   forall(i in sprint)
23     sum(j in story)
24       User_Story_Points[j] * matrix[i][j] <= Sprint_Capacity[i];
25
26   forall(i in story)
27     sum(j in sprint)
28       matrix[j][i] <= 1;
29
30   forall(i in sprint)
31     forall(j in story)
32       forall(k in story: k < j)
33         matrix[i][j] + Interdependencies[j][k] - matrix[i][k] <= 1;
34 }
```

- CPLEX Data

```
1 /*****
2  * OPL 22.1.1.0 Data
3  * Author: Emir
4  * Creation Date: 1 Apr 2023 at 02:02:59
5  *****/
6
7 SheetConnection Sheet("CourseWork_Interdependences.xlsx");
8 story from SheetRead(Sheet, "'Sheet1'!A2:A19");
9 sprint from SheetRead(Sheet, "'Sheet1'!C20:H20");
10 Sprint_Capacity from SheetRead(Sheet, "'Sheet1'!C21:H21");
11 Profitability from SheetRead(Sheet, "'Sheet1'!C22:T22");
12 User_Story_Points from SheetRead(Sheet, "'Sheet1'!C23:T23");
13 Interdependencies from SheetRead(Sheet, "'Sheet1'!C2:T19");
```

- **Output**

Solution with objective 860		
Name	Value	
Data (6)		
Interdependencies	[[1 0 1 0 0 1 0 0 1 0 0 1 1 0 0 0 0 1] [0 1 0 0 1 0 0 0 0 1 0 1 1 0 0 1 1 0] [0 0 1 1 0 1 1 0 0 0 0 1 1 1 1 0 0 0] [0 0 0 1 0 1 0 1 0 0 1 1 0 0 0 0 0 0] [0 0 1 0 1 0 0 1 1 0 0 1 1 1 0 1 0 0] [0 1 0 0 0 1 0 0 0 0 1 1 0 0 0 0 0 0]]	
Profitability	[100 100 60 60 30 40 35 80 80 75 70 60 20 20 30 15 75 40]	
sprint	("Sprint1" "Sprint2" "Sprint3" "Sprint4" "Sprint5" "Sprint6")	
Sprint_Capacity	[30 20 15 15 20 20]	
story	("R.01" "R.02" "R.06" "R.07" "R.08" "R.09" "R.10" "R.12" "R.13" "R.14" "R.15" "R.16" "R.17" "R.18" "R.19" "R.20" "R.31" "R.32")	
User_Story_Points	[8 7 2 6 6 4 4 7 10 6 7 8 3 5 6 6 8 6]	
Decision variables (1)		
matrix	[[1 1 0 0 0 1 1 0 0 0 0 0 0 1 0 0 0] [0 0 1 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0] [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0] [0 0 0 0 0 0 0 1 0 0 0 0 1 1 0 0 0 0] [0 0 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0] [0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]]	

• **Results**

- **User Stories**

R.01, R.02, R.06, R.07, R.08, R.09, R.10, R.12, R.13, R.14, R.15, R.16, R.17, R.18, R.19, R.20, R.31, R.32

- **Sprints**

Sprint1, Sprint2, Sprint3, Sprint4, Sprint5, Sprint6

- **Matrix**

[[1,1,0,0,0,1,1,0,0,0,0,0,0,0,1,0,0,0,0
[0,0,1,0,1,0,0,0,0,0,0,0,1,0,0,0,0,0,0]
[0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]
[0,0,0,0,0,0,0,0,1,0,0,0,0,0,1,1,0,0,0]
[0,0,0,1,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0]
[0,0,0,0,0,0,0,0,0,0,0,0,1,1,0,0,0,0,0]]

- **Profit**

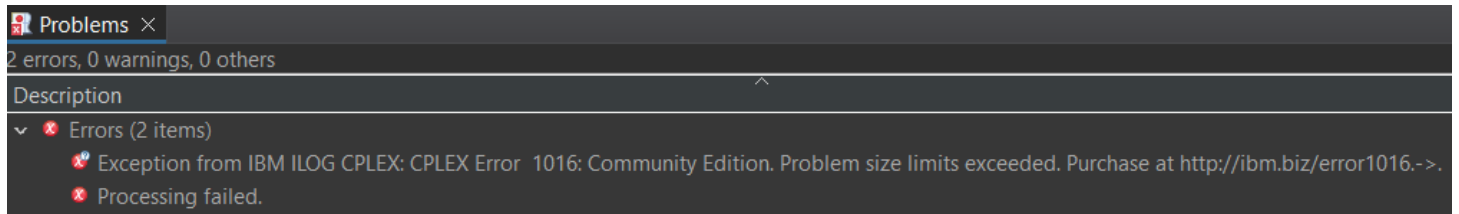
	R.01	R.02	R.06	R.07	R.08	R.09	R.10	R.12	R.13	R.14	R.15	R.16	R.17	R.18	R.19	R.20	R.31	R.32
Sprint1	100	100				40	35								30			
Sprint2			60		30							60						
Sprint3																		
Sprint4								80					20	20				
Sprint5				60					80									
Sprint6										75	70							

- **Capacity**

	R.01	R.02	R.06	R.07	R.08	R.09	R.10	R.12	R.13	R.14	R.15	R.16	R.17	R.18	R.19	R.20	R.31	R.32
Sprint1	8	7				4	4								6			
Sprint2			2		6							8						
Sprint3																		
Sprint4								7					3	5				
Sprint5				6					10									
Sprint6										6	7							

- **Annotation**

Because of the error below, I deleted one of the user stories (R33) given in the variant file and did the homework in this way. So, I just deleted one column and thus got rid of the following error.



- **Conclusion**

In this assignment, I first combined the user stories into an Excel file based on the variant number (13) assigned to me. I have also added the "Sprint Number, Sprint Capacity, Sprint Profitability and User Story Scores" attributes to this Excel file. I created a CPLEX data file by writing the necessary codes to use the data in this Excel file. Then I wrote a code where I could use this data and created the CPLEX model file. I added the Excel file to the CPLEX project folder I created and ran the code. I got the data and decision variables that I used in the output and showed them in the assignment as well. I created the profitability and capacity tables according to the output matrix created under the name of decision variables and completed the homework.

As a result, in this assignment, I found the most optimized way by using sample files with project management decisions, I learned where OPL is used and how to use CPLEX.