



# Analysis and classification of kidney stones based on Raman spectroscopy

XIAOYU CUI,<sup>1,3</sup> ZEYIN ZHAO,<sup>1,3</sup> GEJUN ZHANG,<sup>2,\*</sup> SHUO CHEN,<sup>1</sup> YUE ZHAO<sup>1</sup> AND JIAO LU<sup>1</sup>

<sup>1</sup>Sino-Dutch Biomedical and Information Engineering School, Northeastern University, Shenyang 110167, China

<sup>2</sup>Department of Urology, the First Hospital of China Medical University, Shenyang 110001, China

<sup>3</sup>Authors contributed equally to this work

\*[gejunzhang1@gmail.org](mailto:gejunzhang1@gmail.org)

**Abstract:** The number of patients with kidney stones worldwide is increasing, and it is particularly important to facilitate accurate diagnosis methods. Accurate analysis of the type of kidney stones plays a crucial role in the patient's follow-up treatment. This study used microscopic Raman spectroscopy to analyze and classify the different mineral components present in kidney stones. There were several Raman changes observed for the different types of kidney stones and the four types were oxalates, phosphates, purines and L-cystine kidney stones. We then combined machine learning techniques with Raman spectroscopy. KNN and SVM combinations with PCA (PCA-KNN, PCA-SVM) methods were implemented to classify the same spectral data set. The results show the diagnostic accuracies are 96.3% for the PCA-KNN and PCA-SVM methods with high sensitivity (0.963, 0.963) and specificity (0.995, 0.985). The experimental Raman spectra results of kidney stones show the proposed method has high classification accuracy. This approach can provide support for physicians making treatment recommendations to patients with kidney stones

© 2018 Optical Society of America under the terms of the [OSA Open Access Publishing Agreement](#)

## 1. Introduction

Kidney stones are a global problem that seriously threatens human health [1]. The stones cause physical pain and lead to chronic kidney disease [2]. Recent statistics indicate the incidence of kidney stones is increasing worldwide, and the incidence rate usually varies from 2 to 20% [3–5]. The prevalence of kidney stones in adolescents and children is also increasing and has become common [6]. There are substantial social and medical consequences due to the high incidence of kidney stones. The treatment of urolithiasis in the United States costs 2 billion US dollars annually [7]. Additionally, treating kidney stones is a painful process for most patients. However, kidney stones are an extremely recurrent disease and survey data show 52% of patients relapse within 10 years [8] and 3% of patients experience renal failure because of urolithiasis [9]. Thus, preventing recurrence is critical.

The current recommendations for the treatment and prevention of kidney stones are based on the analysis of kidney stone types. Prompt and accurate detection of the kidney stones reduces treatment error and improves the prevention advice. It is valuable to perform precision treatment on patients with kidney stones. The current identification methods for kidney stone composition include infrared spectroscopy, chemical analysis and X-ray diffraction [10–12]. Infrared spectroscopy is currently the most practical method in hospitals, but its wide spectrum range makes it difficult to differentiate overlapped peaks and distinguish different types of kidney stones. In addition, this method can be easily disturbed by water and other particles. However, Raman spectroscopy is beginning have an important role in biomedicine [10].

Raman spectroscopy can provide the chemical composition, structure and spatial information of molecules. This approach could be useful in the biomedical field. Cells, tissues and organs in different states have different biochemical components and spectral

characteristics [11–13]. Raman spectroscopy plays an important role in the detection of kidney stones, clinical diagnosis and postoperative guidance. Many scholars have studied kidney stones by Raman spectroscopy [14–18].

The Raman spectroscopy method allows real-time, lossless and non-invasive measurements. In addition, it requires only minimal sample preparation. It has a better signal-to-noise ratio than X-ray diffraction, and the problem of spectral line overlap is less than FTIR and the detection time is short. However, no one has attempted to classify kidney stones using Raman spectroscopy combined with machine learning.

Therefore, analysis and classification of kidney stones by Raman spectroscopy is completely effective. Raman spectroscopy is now combined with machine learning in medical diagnostics [19, 20]. In this study, we used micro-Raman spectroscopy to analyze kidney stones by percutaneous nephroscope lithotripsy. The contributions of this paper are as follows. First, we first used Raman spectroscopy in combination with machine learning methods to classify kidney stones, compared to methods already used in hospitals. Raman spectroscopy is faster and takes less time. Second, 135 samples of kidney stones were collected. This is the first time that a large-scale sample analysis has been performed compared to previous studies. Third, using a variety of machine learning models for comparison, it was found that most models are well-suited for the classification of kidney stones.

## 2. Materials and methods

### 2.1 Sample

The major crystalline components of human urinary tract stones are listed in Table 1.

**Table 1. The chemical name, composition, mineral name of the most common components of urinary tract calculi [21].**

Chemical name	Mineral name	Chemical formula
<b>Oxalates</b>		
·Calcium oxalate monohydrate	Whewellite	$\text{CaC}_2\text{O}_4 \cdot \text{H}_2\text{O}$
·Calcium oxalate dihydrate	Weddellite	$\text{CaC}_2\text{O}_4 \cdot 2\text{H}_2\text{O}$
<b>Phosphates</b>		
·basic calcium phosphate	Apatite	$\text{Ca}_5(\text{PO}_4)_3(\text{OH})$
·Calcium hydrogen phosphate	Brushite	$\text{CaHPO}_4 \cdot 2\text{H}_2\text{O}$
·Magnesium ammonium phosphate hexahydrate	Struvite	$\text{MgNH}_4\text{PO}_4 \cdot 6\text{H}_2\text{O}$
<b>Purines</b>		
·Uric acid		$\text{C}_5\text{H}_4\text{N}_4\text{O}_3$
·Monosodium urate monohydrate		$\text{NaC}_5\text{H}_3\text{N}_4\text{O}_3 \cdot \text{H}_2\text{O}$
<b>Other</b>		
·L-cystine		$(-\text{SCH}_2\text{CHNH}_2\text{COOH})_2$

A total of 135 kidney stone samples were obtained from patients at the First Hospital of China Medical University. The numbers of different types of kidney stones were 34 for L-cystine kidney stones, 34 for purines kidney stones, 32 for phosphates kidney stones and 35 for oxalates kidney stones. The mean patient age was 62 years. The oldest patient was 88 years old, and the youngest patient was 31 years old. All kidney stones were obtained by percutaneous nephroscope lithotripsy. The stones were washed with deionized water to remove debris such as blood, mucus and gypsum. The experimental procedure in this study was performed after obtaining written permission from the First Hospital of China Medical University and the patients. The washed kidney stones were dried in a moisture proof box for 1 hour. The oven-dried kidney stone samples were ground into a fine powder by using an agate mortar and pestle. In addition, we photobleached all kidney stone samples to reduce the effect of fluorescence.

## 2.2 Raman spectroscopy

The spectrum from the kidney stone samples were recorded in the spectral range of  $200\text{ cm}^{-1}$  to  $1700\text{ cm}^{-1}$  by using a Raman system (Horiba JY HR Evolution, France), which can provide a spectral resolution of  $1\text{ cm}^{-1}$ . A 785 nm diode laser with spatial resolution of  $1\mu\text{m}$  was used as an excitation source. The power of the laser is 19.2 mW, and the kidney stone samples were excited by a 20x microscope objective lens (NA = 0.40).

We measured three different locations for each sample during the collection of Raman spectra of kidney stones. Each spectrum was acquired with an integration time of 1s and accumulated 5 times.

## 2.3 Preprocessing

The spectra collected using the Horiba JY HR evolution Raman spectrometer yielded noise and fluorescence background. The noise was removed by Savitzky-Golay and the fluorescence background was also removed [22, 23]. Savitzky-Golay filters are widely used for data stream smoothing and reducing noise. The most important feature of this kind of filter is the filtering ensures the shape and width of the signal while filtering out noise. The fifth-order polynomial fit was used to estimate the fluorescence background and then subtract from the original spectrum. In order to compare the changes in spectral shape and relative peak intensity in different urine samples, all the Raman spectra were normalized.

## 2.4 Classification and quantification

Principal Component Analysis (PCA) is a statistical method that reduces the dimensions of high-dimensional data to simplify complex data sets. A dependent-sample t test was conducted to select the most diagnostically significant PCs ( $P < 0.05$ ).

There were two classifiers adopted for identification analysis; KNN and SVM. Both of these classifiers are well studied for classification problems and have been used in the fields of biophotonics, pattern recognition and classification for many years. The KNN algorithm is a mature and basic classification and regression method proposed by Cove and Hart in 1967 [24]. For a newly arrived instance the KNN algorithm predicts the category of the new instance by means of majority voting according to the category of its  $k$  nearest neighbor training set instances. The following algorithm is used:

**Input:** Training data set

$$T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}$$

where  $x_i \in \chi \subseteq \mathbf{R}^n$  is the feature vector of the instance,  $y_i \in Y \subseteq \{c_1, c_2, \dots, c_k\}$  is the class of the instance,  $i = 1, 2, \dots, N$ ; the instance feature vector  $x$ ;

**Output:** Class  $y$  to which instance  $x$  belongs

1. According to the given distance metric,  $k$  points in the training set  $t$  are found to be nearest to  $x$ , and the neighborhood of  $x$  covering the  $k$  points is denoted as  $N_k(x)$ ;

2. Determine the class  $y$  of  $x$  according to the classification decision rule (such as majority vote) in  $N_k(x)$ :

$$Y = \arg \max_{c_j} \sum_{x_i \in N_k(x)} I(y_i = c_j), i = 1, 2, \dots, N; j = 1, 2, \dots, K$$

where  $I$  is the indicator function,  $i = 1$  when  $y_i = c_j$ , otherwise  $i = 0$ .

The standard SVM was proposed by Cortes and Vapnik [25]. This is a supervised learning algorithm that implements network parameter selection by minimizing structural risk minimization. The support vector machine can realize non-linear mapping of input vectors to high-dimensional feature space through nonlinear kernel function and can achieve effective classification. This makes the sample linearly feasible within this feature space. The following kernel functions are used in this study:

$$\text{Linear: } K(x_i, x_j) = x_i^T x_j$$

$$\text{Polynomial kernel: } K(x_i, x_j) = (x_i^T x_j)^d$$

$$\text{Gaussian radial basis function (RBF): } K(x_i, x_j) = \exp \frac{-\|x_i - x_j\|^2}{2\sigma^2}$$

### 3. Results and discussion

#### 3.1 Spectral preprocessing

The data preprocessing substantially improved the Raman spectra quality. The Raman spectrum was smoother and the Raman peaks of different kidney stones were distinguished.

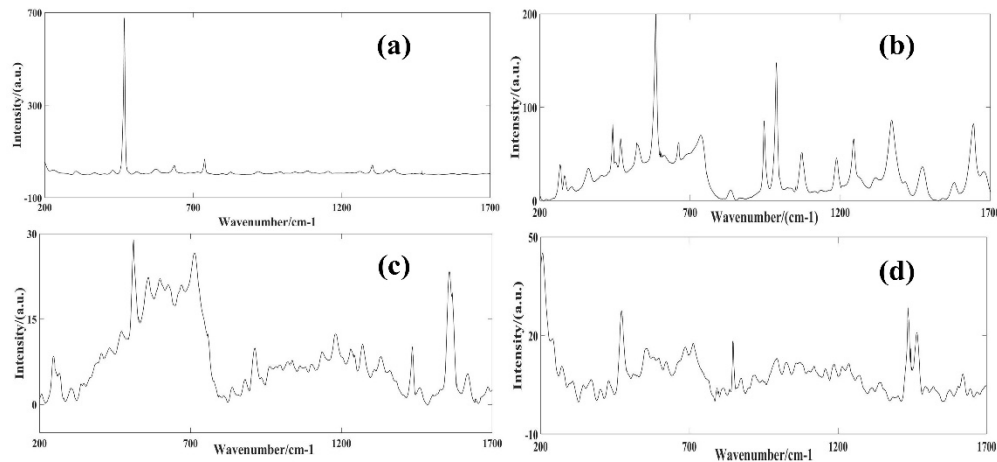


Fig. 1. Typical Raman spectra of kidney stones after preprocessing.

Figure 1 shows the typical Raman spectra for the kidney stones in four different categories. The spectral intensities of the samples were different from each other. Specific assignments of individual peaks could be found in Table 2. The Raman spectrum of L-cystine stones, as shown in Fig. 1(a), have a strong S-S stretching in Raman peak at  $499 \text{ cm}^{-1}$ . There are some faint Raman bands at  $614, 679, 1341, 1387, 1408 \text{ cm}^{-1}$ . Figure 1(b) shows that Raman spectra of uric acid stones have four main characteristic peaks at  $626, 997, 1039$  and  $1405 \text{ cm}^{-1}$ . There are two more peaks at  $1501$  and  $1648 \text{ cm}^{-1}$ . Figure 1(c) shows Raman spectra of phosphate stones, mostly caused by phosphate. In the composed calcium phosphate, the spectrum mainly appears in the  $\text{HPO}_4^{2-}$  and  $\text{PO}_4^{3-}$  bands in the spectral range of  $900\text{--}1000 \text{ cm}^{-1}$ . The intense band in the range of  $1000\text{--}1100 \text{ cm}^{-1}$  belongs to the bending vibration of the  $\text{PO}_4^{3-}$  group. Figure 1(d) shows Raman spectra of oxalate stones. Compared to other stones, Oxalate stones are caused by oxalate ions ( $\text{COO}^-$  or  $\text{CO}_2^-$ ) with 16 bands, 4 bands near  $1476, 1398$ , and  $594 \text{ cm}^{-1}$ . The Raman spectra showed distinct doublets at  $1493$  and  $1468 \text{ cm}^{-1}$ . The sharp bands at  $1462 \text{ cm}$  and  $1473 \text{ cm}^{-1}$  were COM and COD scaled by  $C = O$  oscillations and C-Osymmetry..

Table 2. Raman spectral data of kidney stones [17, 26, 27]

COM	COD	L-cystine	Uric acid	HA	MAPH	Assignments
			1683			Stretching vibration of C=O
1631	1629		1650			C=O Stretching
1614						Asymmetric COO– stretching
						C-O asymmetric stretching
1471	1476		1593			C-N stretching
						Symmetric COO– stretching
1462,1489	1462,1473					Vibration of C=O
1398	1417					Symmetric C=O stretching
		1408				C-H bending and COO- stretching
		1387				C-H bending
862,896		1341				C-C stretching
	1305					O-C-O stretching mode
			1286			O=H deformation
			1121,1231			Ring vibration
			997, 1037,	1086		v3(PO4):
			1404			Highly mixed vibration: (1) ring
				961, 997, 1068		P-O Stretching
					941	v 1(PO4)
	912					Shift C–C stretching
			782			N-H out of plane and in-plan
		614, 679				C-S stretching
			634			Ring breathing mode
				590		v4 stretching of phosphate
				584, 599		Phosphate Bands
				567	524	v4(PO4)
			471, 569, 625			Skeletal ring deformation
503,594	598					O–C–O bending/Water libration
	504					O–C–O bending
		499				S-S stretching
				434	434	δ(O–P–O)
				428		v2 stretching of phosphate

### 3.2 Principal component analysis

The PCA was performed to reduce the number of variables in the analysis. The data presented in Table 3 show the first four principal components of the Raman spectrum of the kidney stone sample retained 94.94% of the original data. There is a substantial amount of original information compressed into principal component 1, principal component 2 and principal component 3. These three principal components account for 89.19% of the original information. Figure 3 shows the pc 1, the pc 2 and the pc 3 scores. The different types of kidney stones are well distinguished. The scores of different types of kidney stones are within their respective regions without interfering with each other. In addition, the dispersion of points in each region of the kidney stone sample is relatively small and further shows that

Raman spectroscopy combined with principal component analysis can distinguish kidney stone types. The PCA was performed to reduce the number of variables in the analysis.

**Table 3. Explanation of variance for the top 6 principal components of samples**

PC	PC1	PC2	PC3	PC4
contribution%	66.67%	12.40%	10.12%	5.75%
Cumulative contribution%	66.67%	79.07%	89.19%	94.94%

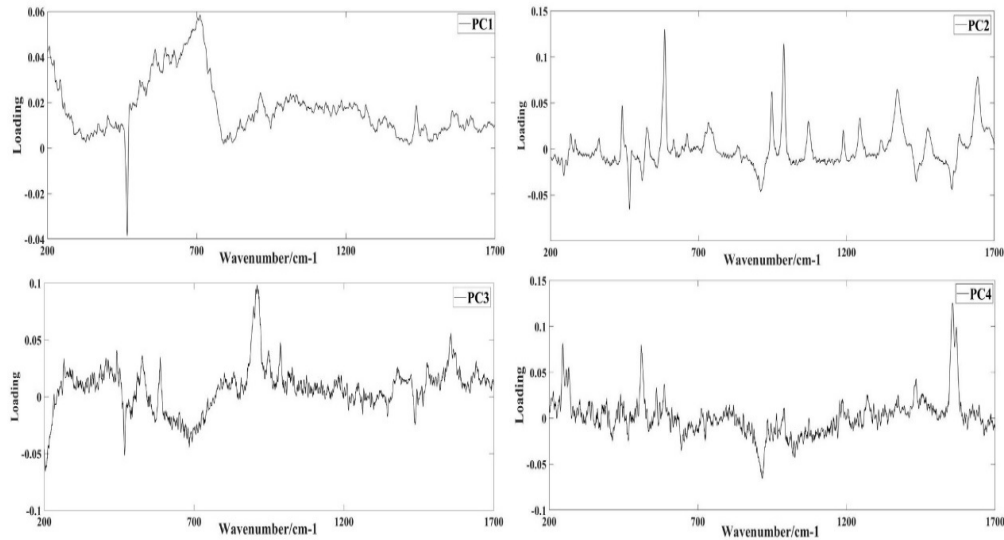


Fig. 2. The spectra of first five principal components in PCA.

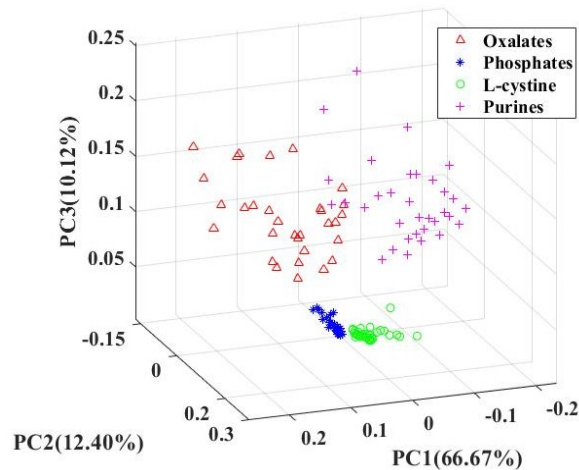


Fig. 3. 3D plot of the first principal component (PC1) versus the second principal component (PC2) and the third principal component (PC3) for kidney stones.

The spectra also contain redundant data and noise, which limit the efficiencies of the KNN and SVM techniques. It is critical to reduce the dimensions of the spectral data using the PCA technique to simplify the implementation of the SVM algorithm and to improve the performance. Therefore, PCA can accurately capture changes in different types of stones, reduce the dimensions for subsequent machine learning of the data, and reduce calculations.



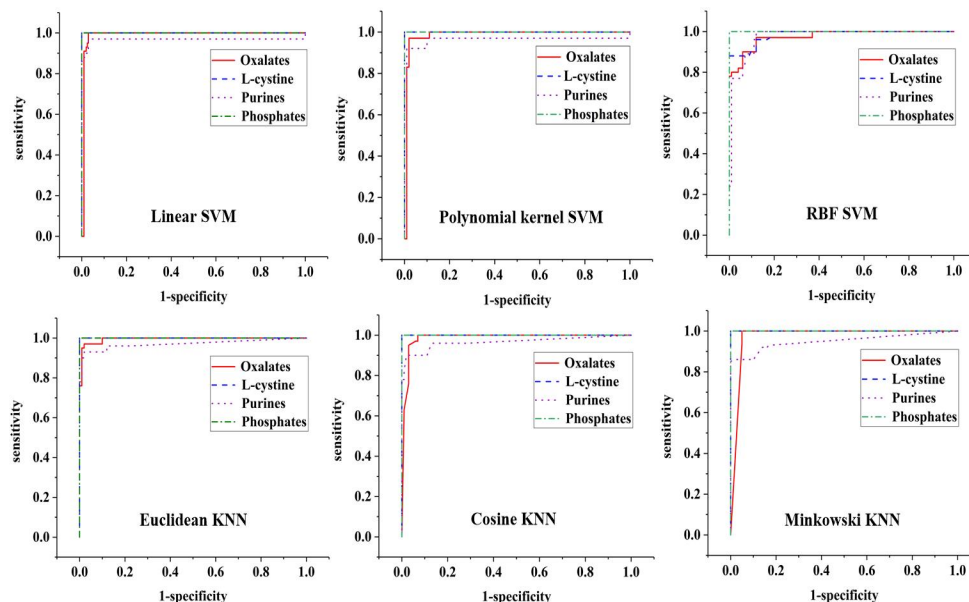
### 3.3 Classification

An accurate discrimination algorithm is required to properly use all of the information contained in Raman spectra for the classification. The KNN and SVM models were developed for the classification of Raman spectra of kidney stones. The classification model was evaluated by using a 5-fold cross validation approach. This approach divides the whole data set into 5-subsets. For each of the sub-sets we use one as the test set and the remaining four as training sets. The overall process is repeated 5 times to predict all the samples stepwise. This method makes full use of all the samples.

**Table 4. Classification results for the samples in the validation set.**

Classifier	Classification accuracy%
<b>KNN</b>	
·Euclidean knn	96.3%
·Cosine knn	94.8%
·Minkowski knn	94.8%
<b>SVM</b>	
·Linear SVM	96.3%
·Polynomial kernel SVM	96.3%
·RBF SVM	88.1%

The distance measure is used to determine the spatial distance of the individual. A longer distance indicates there is a greater difference between individuals. We chose three different distance formulas (Euclidean, Cosine and Minkowski) in the KNN for comparison. The KNN algorithm with three different distance formulas achieved acceptable results in the classification of kidney stones. The Euclidean distance KNN algorithm yielded the best results. The data show the classification accuracy was 98.8%. We also chose three different kernels (Linear, Polynomial and Gaussian) in the SVM algorithm for comparison. Similar to the RBF, the other two SVM algorithms also achieved very good classification accuracy values of 96.3% (Table 4). These are considered high quality results for the classification of kidney stones.



**Fig. 4. Receiver operating characteristic (ROC) curve of discrimination results for Raman spectra utilizing the PCA-SVM and PCA-KNN based spectral classification.**

**Table 5. Each case was classified by the functions derived from all cases other than that case**

	Oxalates	Phosphates	Purines	L-cystine
<b>Sensitivity</b>				
Euclidean KNN	0.97	1	0.88	1
Cosine KNN	0.97	1	0.82	1
Minkowski KNN	1	0.76	0.95	1
Linear SVM	0.91	1	0.94	1
Polynomial kernel SVM	0.97	1	1	0.88
RBF SVM	0.97	0.94	0.74	0.88
<b>Specificity</b>				
Euclidean KNN	0.95	1	0.99	1
Cosine KNN	0.94	1	0.99	1
Minkowski KNN	0.90	1	1	1
Linear SVM	0.98	1	1	1
Polynomial kernel SVM	0.96	1	1	0.99
RBF SVM	0.85	1	0.99	1

The performance of the model is usually evaluated based on accuracy, sensitivity, and specificity. We further confirmed the performance of the diagnostic model developed by the KNN and SVM algorithms using a receiver operating characteristic (ROC) for all classification algorithms (Fig. 4). The ROC curve is a graph that illustrates the performance of the binary classifier system because of its varying threshold of discrimination. The integrated area under the ROC curve (AUC) is a quantitative indicator used to represent the classifier performance. The sensitivity is the ability to correctly classify all patients with this disease and all patients without the disease are correctly identified with specificity (Table 5). The larger AUC value means that the classifier has higher prediction accuracy. These results confirm the polynomial kernel SVM algorithm produces better diagnostic accuracy than other algorithms.

#### 4. Conclusions

This study demonstrates the use of Raman spectroscopy combined with machine learning techniques can classify spectral data obtained from different kidney stones. The combination of Raman spectroscopy and statistical tools has great potential for the effective diagnosis and study of kidney stones. This is the first report classifying kidney stones according to Raman spectroscopy combined with machine learning methods.

It is feasible to classify kidney stones optically. We used Raman spectroscopy combined with PCA to investigate the identification of kidney stones. Our findings indicate kidney stone samples could be satisfactorily discriminated. The PCA methods can considerably simplify the complexity of calculation without sacrificing the performance of the algorithm. The experimental results show the proposed classification algorithms are effective methods and the KNN and SVM achieved high classification accuracy. Thus, there is potential to provide an effective and accurate diagnostic means for kidney stone detection. Future research should consider the potential effects of different optical methods in classifying kidney stones more carefully. Additionally, further work is required to disentangle the complexities in multi-component kidney stone classification. The research in our laboratory is using different optical imaging methods to accurately diagnose kidney stones. We hope this technique will determine the clinical advantage of Raman spectroscopy in the diagnosis of kidney stone types.

#### Funding

National Natural Science Foundation of China (61501101, 61605025); Natural Science Foundation of Liaoning Province (201601015); Program for Innovation Talents in Universities of Liaoning Province (LR2016031); Fundamental Research Funds for the Central Universities (N171904006, N171902001).



## Disclosures

The authors declare that there are no conflicts of interest related to this article.

## References

- O. W. Moe, "Kidney stones: pathophysiology and medical management," *Lancet* **367**(9507), 333–344 (2006).
- R. T. Alexander, B. R. Hemmelgarn, N. Wiebe, A. Bello, C. Morgan, S. Samuel, S. W. Klarenbach, G. C. Curhan, and M. Tonelli, "Kidney stones and kidney function loss: a cohort study," *BMJ* **345**, e5287 (2012).
- P. J. S. Osther, *Epidemiology of Kidney Stones in the European Union* (Springer London, 2013).
- G. E. Tasian, M. E. Ross, L. Song, D. J. Sas, R. Keren, M. R. Denburg, D. I. Chu, L. Copelovitch, C. S. Saigal, and S. L. Furth, "Annual incidence of nephrolithiasis among children and adults in South Carolina from 1997 to 2012," *Clin. J. Am. Soc. Nephrol.* **11**(3), 488–496 (2016).
- G. Zeng, Z. Mai, S. Xia, Z. Wang, K. Zhang, L. Wang, Y. Long, J. Ma, Y. Li, S. P. Wan, W. Wu, Y. Liu, Z. Cui, Z. Zhao, J. Qin, T. Zeng, Y. Liu, X. Duan, X. Mai, Z. Yang, Z. Kong, T. Zhang, C. Cai, Y. Shao, Z. Yue, S. Li, J. Ding, S. Tang, and Z. Ye, "Prevalence of kidney stones in China: an ultrasonography based cross-sectional study," *BJU Int.* **120**(1), 109–116 (2017).
- G. E. Tasian, A. E. Kabarriti, A. Kalmus, and S. L. Furth, "Kidney stone recurrence among children and adolescents," *J. Urol.* **197**(1), 246–252 (2017).
- M. S. Pearle, E. A. Calhoun, and G. C. Curhan, "Urologic diseases in America project: urolithiasis," *J. Urol.* **173**(3), 848–857 (2005).
- J. Uribarri, M. S. Oh, and H. J. Carroll, "The first kidney stone," *Ann. Intern. Med.* **111**(12), 1006–1009 (1989).
- G. C. Curhan, "Epidemiology of stone disease," *Urol. Clin. North Am.* **34**(3), 287–293 (2007).
- C. Otto, C. J. D. Grauw, J. J. Duindam, N. M. Sijtsma, and J. Greve, "Applications of micro-Raman imaging in biomedical research," *J. Raman Spectrosc.* **28**(2-3), 143–150 (1997).
- K. Christian, M. Johanna, A. Werner, B. Kathrin, G. M. Tesfay, H. Robert, A. Abbas, W. Stefan, B. Andreas, N. F. Wilhelm, and S. Florian, "Raman difference spectroscopy: a non-invasive method for identification of oral squamous cell carcinoma," *Biomed. opt. Express* **5**(9), 3252–3265 (2014).
- C. A. Lieber, H. E. Nethercott, and M. H. Kabeer, "Cancer field effects in normal tissues revealed by Raman spectroscopy," *Biomed. Opt. Express* **1**(3), 975–982 (2010).
- S. Feng, R. Chen, J. Lin, J. Pan, G. Chen, Y. Li, M. Cheng, Z. Huang, J. Chen, and H. Zeng, "Nasopharyngeal cancer detection based on blood plasma surface-enhanced Raman spectroscopy and multivariate analysis," *Biosens. Bioelectron.* **25**(11), 2414–2419 (2010).
- K. S. Muhammed, A. Chawla, M. Mallya, B. K. Barik, V. K. Unnikrishnan, V. B. Kartha, and C. Santhosh, "LIBS-Raman: an effective complementary approach to analyze renal-calculi," *J. Biophotonics* **11**, 201700271 (2018).
- C. G. Kontoyannis, N. C. Bouropoulos, and P. G. Koutsoukos, "Urinary stone layer analysis of mineral components by Raman spectroscopy, IR spectroscopy, and X-ray powder diffraction: a comparative study," *Appl. Spectrosc.* **51**(8), 1205–1209 (1997).
- C. G. Kontoyannis, N. C. Bouropoulos, and P. G. Koutsoukos, "Raman spectroscopy: A tool for the quantitative analysis of mineral components of solid mixtures. The case of calcium oxalate monohydrate and hydroxyapatite," *Vib. Spectrosc.* **15**(1), 53–60 (1997).
- Y. C. Chiu, H. Y. Yang, S. H. Lu, and H. K. Chiang, "Micro-Raman spectroscopy identification of urinary stone composition from ureteroscopic lithotripsy urine powder," *J. Raman Spectrosc.* **41**(2), 136–141 (2009).
- Y. Chiu, Y. Y. Huang, P. A. Chen, S. H. Lu, A. W. Chiu, and H. K. Chiang, "Quantitative and multicomponent analysis of prevalent urinary calculi using Raman spectroscopy," *J. Raman Spectrosc.* **43**(8), 992–997 (2012).
- S. Khan, R. Ullah, A. Khan, N. Wahab, M. Bilal, and M. Ahmed, "Analysis of dengue infection based on Raman spectroscopy and support vector machine (SVM)," *Biomed. Opt. Express* **7**(6), 2249–2256 (2016).
- Q. Li, Q. Gao, and G. Zhang, "Classification for breast cancer diagnosis with Raman spectroscopy," *Biomed. Opt. Express* **5**(7), 2435–2445 (2014).
- I. Mandel and N. Mandel, *Structure and Compositional Analysis of Kidney Stones* (Humana Press, 2007).
- Z. M. Zhang, S. Chen, and Y. Z. Liang, "Baseline correction using adaptive iteratively reweighted penalized least squares," *Analyst (Lond.)* **135**(5), 1138–1146 (2010).
- A. Savitzky and M. J. E. Golay, "Smoothing and Differentiation of Data by Simplified Least Squares Procedures," *Anal. Chem.* **36**(8), 1627–1639 (1964).
- T. Cover and P. Hart, *Nearest Neighbor Pattern Classification* (IEEE Press, 1967).
- C. Cortes and V. Vapnik, "Support-vector networks," in *Machine Learning* (Chapman and Hall, 1995), pp. 273–297.
- R. Selvaraju, A. Raja, and G. Thirupathi, "Chemical composition and binary mixture of human urinary stones using FT-Raman spectroscopy method," *Spectrochim. Acta A Mol. Biomol. Spectrosc.* **114**, 650–657 (2013).
- H. S. Hsu, and S. Y. Lin, *Fast Identification and Differentiation of Mineral Components in Prostate Stones using a Portable Fiber-Optic Raman Spectroscopy* (IOS Press, 2014).