

INFORMATION

$$\mathbf{a} \cdot \mathbf{b} = ab \cos \theta$$

$$\mathbf{a} \times \mathbf{b} = ab \sin \theta \hat{\mathbf{c}} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

$$\mathbf{v} \equiv \frac{d\mathbf{r}}{dt} \quad \mathbf{a} \equiv \frac{d\mathbf{v}}{dt} \quad \mathbf{v} = \int \mathbf{a} dt \quad \mathbf{r} = \int \mathbf{v} dt$$

$$v = u + at \quad \mathbf{a} = -g\mathbf{j}$$

$$x = ut + \frac{1}{2}at^2 \quad \mathbf{v} = \mathbf{u} - gt\mathbf{j}$$

$$v^2 = u^2 + 2ax \quad \mathbf{r} = \mathbf{u}t - \frac{1}{2}gt^2\mathbf{j}$$

$$s = r\theta \quad v = r\omega \quad a = \omega^2 r = \frac{v^2}{r}$$

$$\omega_f = \omega_i + \alpha t$$

$$\theta = \omega_i t + \frac{1}{2}\alpha t^2$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\theta$$

$$\mathbf{p} \equiv m\mathbf{v}$$

$$N1: \quad \text{if } \sum \mathbf{F} = 0 \text{ then } \delta\mathbf{p} = \mathbf{0}$$

$$N2: \quad \sum \mathbf{F} = m\mathbf{a}$$

$$N3: \quad \mathbf{F}_{AB} = -\mathbf{F}_{BA}$$

$$W = mg \quad F_r = \mu R$$

$$\boldsymbol{\tau} \equiv \mathbf{r} \times \mathbf{F}$$

$$\sum \mathbf{F}_x = \mathbf{0} \quad \sum \mathbf{F}_y = \mathbf{0} \quad \sum \boldsymbol{\tau}_P = \mathbf{0}$$

$$W \equiv \int_{\mathbf{r}_1}^{\mathbf{r}_2} \mathbf{F} d\mathbf{r} \quad W = \mathbf{F} \cdot \mathbf{s}$$

$$KE = \frac{1}{2}mv^2 \quad PE = mgh$$

$$P \equiv \frac{dW}{dt} = \mathbf{F} \cdot \mathbf{v}$$

$$F = kx \quad PE = \frac{1}{2}kx^2$$

$$\frac{dv}{v_e} = -\frac{dm}{m} \quad v_f - v_i = v_e \ln\left(\frac{m_i}{m_f}\right)$$

$$F = |v_e \frac{dm}{dt}|$$

$$F = k \frac{q_1 q_2}{r^2} \quad k = \frac{1}{4\pi\epsilon_0} \approx 9 \times 10^9 \text{ Nm}^2\text{C}^{-2}$$

$$\epsilon_0 = 8.854 \times 10^{-12} \text{ N}^{-1}\text{m}^{-2}\text{C}^2$$

$$\mathbf{E} \equiv \lim_{\delta q \rightarrow 0} \left(\frac{\delta \mathbf{F}}{\delta q} \right) \quad \mathbf{E} = k \frac{q}{r^2} \hat{\mathbf{r}}$$

$$V \equiv \frac{W}{q} \quad E = -\frac{dV}{dx} \quad V = k \frac{q}{r}$$

$$\Phi = \oint \mathbf{E} \cdot d\mathbf{A} = \frac{\sum q}{\epsilon_0}$$

$$C \equiv \frac{q}{V} \quad C = \frac{A\epsilon}{d}$$

$$E = \frac{1}{2} \frac{q^2}{C} = \frac{1}{2} qV = \frac{1}{2} CV^2$$

$$C = C_1 + C_2 \quad \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$R = R_1 + R_2 \quad \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$V = IR \quad V = E - IR$$

$$P = VI = \frac{V^2}{R} = I^2 R$$

$$K1: \quad \sum I_n = 0$$

$$K2: \quad \sum (IR's) = \sum (EMF's)$$

$$\mathbf{F} = q \mathbf{v} \times \mathbf{B} \quad d\mathbf{F} = i d\mathbf{l} \times \mathbf{B}$$

$$\mathbf{F} = i \mathbf{l} \times \mathbf{B} \quad \boldsymbol{\tau} = ni \mathbf{A} \times \mathbf{B}$$

$$v = \frac{E}{B} \quad r = \frac{m}{q} \frac{E}{BB_0} \quad r = \frac{mv}{qB}$$

$$T = \frac{2\pi m}{Bq} \quad KE_{\max} = \frac{R^2 B^2 q^2}{2m}$$

$$d\mathbf{B} = \frac{\mu_0}{4\pi} i \frac{d\mathbf{l} \times \hat{\mathbf{r}}}{r^2}$$

$$\oint \mathbf{B} \cdot d\mathbf{s} = \mu_0 \sum I \quad \mu_0 = 4\pi \times 10^{-7} \text{ NA}^{-2}$$

$$\phi = \int_{\text{area}} \mathbf{B} \cdot d\mathbf{A} \quad \phi = \mathbf{B} \cdot \mathbf{A}$$

$$\epsilon = -N \frac{d\phi}{dt} \quad \epsilon = NAB\omega \sin(\omega t)$$

$$f = \frac{1}{T} \quad k \equiv \frac{2\pi}{\lambda}$$

$$\omega \equiv 2\pi f \quad v = f\lambda$$

$$y = f(x \mp vt)$$

$$y = a \sin k(x - vt) = a \sin(kx - \omega t) \\ = a \sin 2\pi \left(\frac{x}{\lambda} - \frac{t}{T} \right)$$

$$P = \frac{1}{2} \mu v \omega^2 a^2 \quad v = \sqrt{\frac{T}{\mu}}$$

$$s = s_m \sin(kx - \omega t)$$

$$\Delta p = \Delta p_m \cos(kx - \omega t)$$

$$I = \frac{1}{2} \rho v \omega^2 s_m^2$$

$$n(\text{db's}) \equiv 10 \log \frac{I_1}{I_2} = 10 \log \frac{I}{I_0}$$

$$\text{where } I_0 = 10^{-12} \text{ W m}^{-2}$$

$$f_r = f_s \left(\frac{v \pm v_r}{v \mp v_s} \right)$$

$$\text{where } v \equiv \text{speed of sound} = 340 \text{ m s}^{-1}$$

$$y = y_1 + y_2$$

$$y = [2a \sin(kx)] \cos(\omega t)$$

$$\underline{N} : x = m(\frac{\lambda}{2}) \quad \underline{AN} : x = (m + \frac{1}{2})(\frac{\lambda}{2})$$

$$(m = 0, 1, 2, 3, 4, \dots)$$

$$y = [2a \cos(\frac{\omega_1 - \omega_2}{2} t)] \sin(\frac{\omega_1 + \omega_2}{2} t)$$

$$f_B = |f_1 - f_2|$$

$$y = [2a \cos(\frac{k\Delta}{2})] \sin(kx - \omega t + \frac{k\Delta}{2})$$

$$\Delta = d \sin \theta$$

$$\underline{Max} : \Delta = m\lambda \quad \underline{Min} : \Delta = (m + \frac{1}{2})\lambda$$

$$I = I_0 \cos^2(\frac{k\Delta}{2})$$

$$E = hf \quad c = f\lambda$$

$$\text{KE}_{\text{max}} = eV_0 = hf - \phi$$

$$\mathbf{L} \equiv \mathbf{r} \times \mathbf{p} = \mathbf{r} \times m\mathbf{v}$$

$$L = rmv = n(\frac{h}{2\pi})$$

$$\delta E = hf = E_i - E_f$$

$$r_n = n^2(\frac{h^2}{4\pi^2 m k e^2}) = n^2 a_0$$

$$E_n = -\frac{ke^2}{2a_0}(\frac{1}{n^2}) = -\frac{13.6}{n^2} \text{ eV}$$

$$\frac{1}{\lambda} = \frac{ke^2}{2a_0}(\frac{1}{n_f^2} - \frac{1}{n_i^2}) = R_H(\frac{1}{n_f^2} - \frac{1}{n_i^2})$$

$$(n = 1, 2, 3, \dots) \quad (k \equiv \frac{1}{4\pi\epsilon_0})$$

$$E^2 = p^2 c^2 + (m_0 c^2)^2$$

$$E = m_0 c^2 \quad E = pc$$

$$\lambda = \frac{h}{p} \quad (p = m_0 v \text{ (nonrelativistic)})$$

$$\Delta x \Delta p_x \geq \frac{h}{\pi} \quad \Delta E \Delta t \geq \frac{h}{\pi}$$

$$\frac{dN}{dt} = -\lambda N \quad N = N_0 e^{-\lambda t}$$

$$R \equiv \left| \frac{dN}{dt} \right| \quad T_{\frac{1}{2}} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda}$$

MATH:

$$ax^2 + bx + c = 0 \rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

y	dy/dx	$\int y dx$
x^n	$n x^{(n-1)}$	$\frac{1}{n+1} x^{n+1}$
e^{kx}	$k e^{kx}$	$\frac{1}{k} e^{kx}$
$\sin(kx)$	$k \cos(kx)$	$-\frac{1}{k} \cos kx$
$\cos(kx)$	$-k \sin(kx)$	$\frac{1}{k} \sin kx$

where $k = \text{constant}$

$$\text{Sphere: } A = 4\pi r^2 \quad V = \frac{4}{3}\pi r^3$$

CONSTANTS:

$$g = \text{acceleration due to gravity} = 10 \text{ ms}^{-2}$$

$$1 \text{ u} = 1.660 \times 10^{-27} \text{ kg} = 931.50 \text{ MeV}$$

$$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$$

$$1 \text{ Ci} = 3.7 \times 10^{10} \text{ Bq}$$

$$c = 3.00 \times 10^8 \text{ ms}^{-1}$$

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$e \equiv \text{electron charge} = 1.602 \times 10^{-19} \text{ C}$$

$$R_H = 1.09737 \times 10^7 \text{ m}^{-1}$$

$$a_0 = \text{Bohr radius} = 0.0529 \text{ nm}$$

particle	mass(u)	mass(kg)
e	$5.485\,799\,031 \times 10^{-4}$	$9.109\,390 \times 10^{-31}$
p	1.007\,276\,470	$1.672\,623 \times 10^{-27}$
n	1.008\,664\,904	$1.674\,928 \times 10^{-27}$