

# A Hierarchical Bayesian Approach for Modeling Infant-Mortality and Wearout Failure Modes

Eric Mittman 1\*

Department of Statistics, Iowa State University  
and

Colin Lewis-Beck

Department of Statistics, Iowa State University

March 10, 2017

## Abstract

The text of your abstract. 100 or fewer words.

*Keywords:* 3 to 6 keywords, (don't reuse words appearing in title)

---

\*The authors gratefully acknowledge Bill Meeker for his comments and suggestions

# **1 Introduction**

## **1.1 Background**

This section will follow last paper.

## **1.2 Motivation**

This section will follow last paper.

## **1.3 Overview**

This section will follow last paper.

# **2 Data**

Introduce the data and show some summary statistics, but NOT box plots. Perhaps show an adjusted Kaplan Meier plots to show a Weibull lifetime distribution could be reasonable.

Possible plots (by drive model): avg. time on test vs. proportion failed total time on test (histogram) total records (by drive model)

# **3 Weibull Model**

## **3.1 Likelihood**

Write out the likelihood for the single Weibull with censoring and right truncation. This can come from the previous paper. Also mention why MLE model alone by brand has its limitations.

## **3.2 Hierarchical Model**

Write out the model, priors, etc for the single Weibull Distribution model.

### 3.3 Comparison of Approaches

Compare MLE estimates to Weibull and show improved precision due to pooling of information. This can follow the last paper in terms of the plots. I think this section should be shorter, however, since we are just warming up for the GFLP Model.

## 4 GFLP Model

### 4.1 Motivation

Point out limitation of single failure mode model (perhaps show a drive model with a kink in the distribution) and then present the GFLP Model. Could also discuss the bathtub hazard. Mention Wayne Nelson.

### 4.2 Model

Write out the full Bayes hierarchical model for the GFLP model

### 4.3 Computation

## 5 Data analysis

### 5.1 Results

Show some of the fits of the GFLP Model. Show parameter estimates with uncertainty. Mention some convergence statistics for the MCMC.

### 5.2 collapsing $\mu_1, \sigma_1$

Based on posterior plots, we might fit a simpler model...

### **5.3 Brand Comparisons**

How can we use this model to compare brands? Present comparisons of Quantiles, other parameters. Highlight how this model could be used in an applied sense. Quantiles by brand, etc.

## **6 Concluding Remarks and Extensions**

Review the advantages of fitting the GFLP model and offer future ideas.

### **SUPPLEMENTARY MATERIAL**

Put R Stan code here

## **References**