

ON THE EXPECTED VALUE OF RECURRENT GAMES OF CHANCE

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ABSTRACT. We define a recurrent game of chance, then provide formulas for calculating its expected value

1. INTRODUCTION

Recurrent game of chance definition.

A betting game that starting with an original bet and a set of probabilities associated with different payoffs recursively applies this game conditions to the result of each successive step of the game.

x_0 initial ammount

2. SIMPLE EXAMPLE

x_0 is the original ammount.

Two possible outcames for each step with equal probability defined as having the current amount multiplied by one of two coefficients (b , b') with equal probability.

$$p(b) = p(b') = 0.5$$

$$b > b' > 0$$

Result of the recurrence at infinity:

if $b' > 1/b$ tends to infinity

if $b' < 1/b$ tends to 0

if $b' = 1/b$ tends to x_0

Explain result geometrically–

Rant about $b' = 1/b$ is the exact definition of a fair game.. go on about pascal triangle and binomial distribution

3. MULTIPLE OUTCAMES WITH EQUAL PROBABILITY

m number of possible outcames, each with same probability and associated with a coefficient b_1 to b_m

Result of the recurrence at infinity:

$$\text{Let's define } s = \prod_{i=1}^m b_i$$

if $s > 1$ tends to infinity

if $s < 1$ tends to 0

if $s = 1$ tends to x_0

Prove algebraically.

4. MULTIPLE OUTCOMES EACH WITH IT'S OWN PROBABILITY

m number of possible outcomes, each with it's own coefficient b_i and it's own probability p_i

Result of the recurrence at infinity:

Let's define $s = \prod_{i=1}^m m p_i b_i$

if $s > 1$ tends to infinity

if $s < 1$ tends to 0

if $s = 1$ tends to x_0

Examine distributions of probabilities.. this one is harsher.. to prove

Define expected value of recurrence r_n

$$r_0 = x_0$$

$$r_n = s r_{n-1}$$

Explain based on the definition of the general expected value formula

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