

# Activity: Integrated Resistors

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## I. CALCULATIONS

For any integrated resistor with a nominal temperature  $T_{ref}$  and temperature coefficient  $\alpha$ , the temperature dependence is modeled by

$$R = R_{ref}[1 + \alpha(T - T_{ref})]$$

where  $R_{ref}$  is the resistance at  $T = T_{ref}$ .

Suppose  $R_{n+}$  is an  $n^+$  polysilicon resistor with the following parameters:

- $R_{shn} = 100\Omega/\square$
- $T_C = -800\text{ppm}/^\circ\text{C}$  at  $T_{NOM} = 27^\circ\text{C}$

similarly,  $R_{p+}$  is a  $p^+$  polysilicon resistor with the following parameters:

- $R_{shp} = 180\Omega/\square$
- $T_C = 200\text{ppm}/^\circ\text{C}$  at  $T_{NOM} = 27^\circ\text{C}$

The series resistance  $R_{tot}$  is equal to:

$$R_{tot} = R_{ref,n}[1 + \alpha_n(T - T_{ref})] + R_{ref,p}[1 + \alpha_p(T - T_{ref})]$$

For a temperature independent device, the CTAT and PTAT parameters must cancel each other. Since the resistors have the same widths,

$$\begin{aligned}\alpha_n R_{ref,n}(T - T_{ref}) &= -\alpha_p R_{ref,p}(T - T_{ref}) \\ \alpha_n R_{ref,n} &= -\alpha_p R_{ref,p} \\ \frac{R_{ref,n}}{R_{ref,p}} &= \frac{-\alpha_p}{\alpha_n} \\ \frac{R_{sh,n} \cdot l_n}{R_{sh,p} \cdot l_p} &= \frac{-\alpha_p}{\alpha_n} \\ \frac{l_n}{l_p} &= \frac{-\alpha_p R_{sh,p}}{\alpha_n R_{sh,n}} = 0.45 \\ l_n &= 0.45 \cdot l_p\end{aligned}$$

Substituting the lengths,

$$R_{sh,n} \frac{l_n}{w_n} + R_{sh,p} \frac{l_p}{w_p} = 1k\Omega$$

Since  $w = 2\mu\text{m}$ ,  $l_n = 4\mu\text{m}$  and  $l_p \approx 8.8888\mu\text{m}$

## II. SIMULATIONS

The resistance is obtained by measuring the current across a 1V DC source.

The plots are shown below

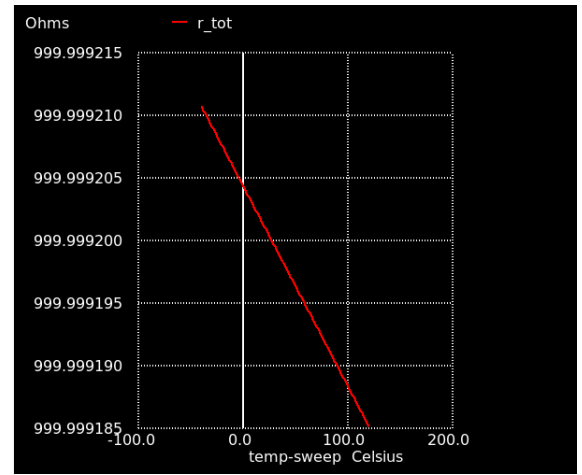


Fig. 1. TEMP SWEEP:  $-40^\circ\text{C}$  to  $125^\circ\text{C}$

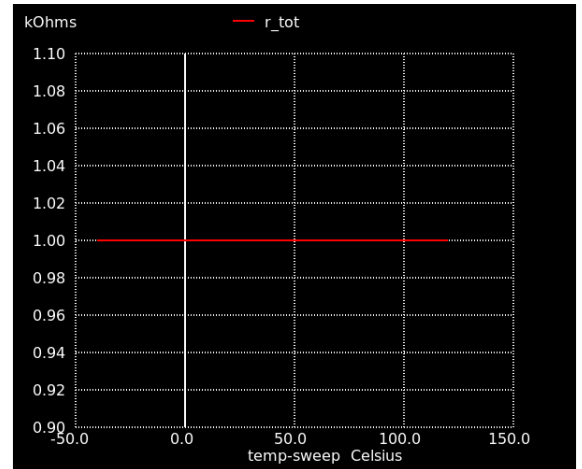


Fig. 2. A zoomed out Fig. 1

The resulting resistance is temperature independent, as expected.