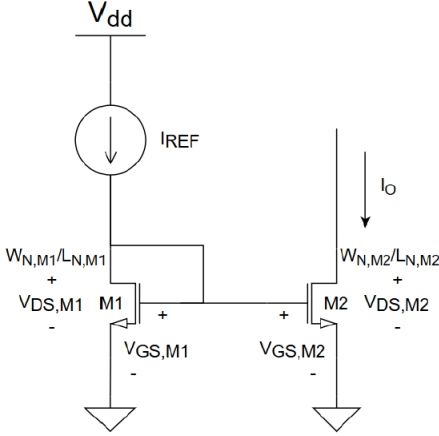


Consider the current mirror shown below.



For any long - channel NMOS,

$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

Solving for V_{GS} in terms of I_{DS} ,

$$V_{GS} = \left(\frac{I_{DS}}{\frac{1}{2} \mu_n C_{ox} \frac{W}{L} (1 + \lambda V_{DS})} \right)^{\frac{1}{2}} + V_{TH}$$

Notice that $V_{GS,M1} = V_{GS,M2}$. If the transistors have the same mobility μ_n , gate-oxide capacitance C_{ox} and threshold voltage V_{TH} ,

Since $I_{DS,M1} = I_{REF}$ and $I_{DS,M2} = I_O$,

$$\frac{I_{REF}}{\frac{W_1}{L_1} (1 + \lambda_1 V_{DS,1})} = \frac{I_O}{\frac{W_2}{L_2} (1 + \lambda_2 V_{DS,2})}$$

Finally,

$$I_O = I_{REF} \cdot \frac{\frac{W_2}{L_2} (1 + \lambda_2 V_{DS,2})}{\frac{W_1}{L_1} (1 + \lambda_1 V_{DS,1})}$$

If both transistors are sized in a way that they have the same lengths, then,

$$I_O = I_{REF} \cdot \frac{W_2 (1 + \lambda V_{DS,2})}{W_1 (1 + \lambda V_{DS,1})}$$

$$A_v \geq 25, g_{mn} \geq 1mS.$$

We can start with $r_{on} = r_{op}$ so that $r_{on}||r_{op} = \frac{1}{2}r_{on}$.

$$\text{Thus, } A_v = \frac{1}{2}g_{mn}r_{on}$$

$$\text{Obtaining } r_{on}, \text{ we get } r_{on} = \frac{2A_v}{g_{mn}} = 50k\Omega = r_{op}.$$

$$\text{Since } r_{on} = 50k\Omega \text{ and } g_{mn} \geq 1mS,$$

$$g_{mn}r_{on} \geq 50, \text{ and the minimum } g_{mn}r_{on} = 50$$

$$\text{We know that } A_v = g_{mn}(r_{on}||r_{op})$$

$$\text{Thus, } \frac{1}{g_{mn}r_{op}} = \frac{1}{A_v} - \frac{1}{g_{mn}r_{on}}$$

$$\text{Solving for } r_{op} \text{ we get } r_{op} = 65.064k\Omega \approx 65k\Omega$$

$$k_{multiplier} = \frac{1mS}{8uS} = 125$$

$$W_N = 62.5um, I_{DN} = 101.7uA$$