Factorial ANOVA (part 1)

Lecture 16 Emma Ning, M.A.

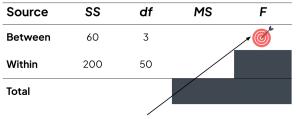
Woah, you've achieved a lot!

One-way ANOVA









Our goal is to get to the last column (our F-ratio)

- Family-Wise Error Rate
- Follow-up tests

Woah, you've achieved a lot!

You've already learned some of the most common statistical tests used in real life!

You have tools to answer most common questions.

But not these:

- Family-Wise Error Rate
- You helped your lab to determine the one best treatment of ADHD from 3 possible medications. It's adderall.

Woah, you've achieved a lot!

But now imagine someone asks you:
Would you recommend Adderall to every person with
ADHD?

What if some people have underlying heart conditions that make stimulants like Adderall risky?

Hm... we need another factor

TODAY'S PLAN









Learning objectives

- Differentiate one-way and factorial ANOVAs.
- Describe the structure of a factorial research design, especially a two-factor design, using the terms factor and level.
- Define and explain the concepts of main effects and interactions in factorial ANOVAs.
- Interpret graphs and tables to identify patterns that reflect main effects, interactions, or both.

01

The Factorial Design

Recap: One-way ANOVA

Gathers



Molly Tea



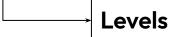
Tiger Sugar



Factor

Aka independent variable (IV): Bubble tea shops in Chicago

Levels are <u>options</u> of the factor



3 levels in our example (aka, 3 shops we are comparing)

Dependent variable (DV): Wait time

What is Factorial ANOVA?

Factorial ANOVA (often called X-Way ANOVA) examines the effect of two-or-more independent variables (factors) on a single dependent variable.

Our bubble tea example had only one factor (IV) – bubble tea shops in Chicago. This one factor has 3 levels.

But sometimes, having one factor is not enough to answer our question – like the example about using Adderall without considering underlying heart conditions.

What is Factorial ANOVA?

Remember: the statistical tests we're learning are of two or more indepenjust tools. es (factors) on a single dependent variable

We don't use them because they exist—we use them because they help us answer real questions.

And when one tool no longer gets the job done, we develop new ones.

One-Way ANOVA works great—until we realize that a single factor isn't enough to explain what's happening.

That's when we turn to Factorial ANOVA.

It wasn't invented just for fun—it was invented to solve a real problem that One-Way ANOVA couldn't.

So as we move forward, think about each new method not as "just another thing to memorize," but as a response to a limitation, a way to ask smarter questions about the world.

2 x 2 Design

(DV: ADHD symptoms)

Factor A:

ADHD medications

Stimulant

Non-Stimulant

Factor B: Heart Condition

Present

None

Has heart condition and on stimulant

No heart condition and on stimulant

Has heart condition and not on stimulant

No heart condition and not on stimulant

There are 4 cells in this example





Personality

Introvert

Extravert

Factor B: Chronotype

Early Bird

Introverts who are early birds Extraverts
who are
early birds

Night Owl

who are night owls

Extraverts who are night owls

There are **4 cells** in this example



Factor A:

Study Environment

Cafe

Library

Factor B: Time of Day

Morning

Students who study at **cafe** in **morning**

Students who study at **library** in **morning**

Afternoon

Students who study at **cafe** in **afternoon**

Students who study at **library** in **afternoon**

Evening

Students who study at **cafe** in **evening**

Students who study at **library** in **evening**

A quick note:

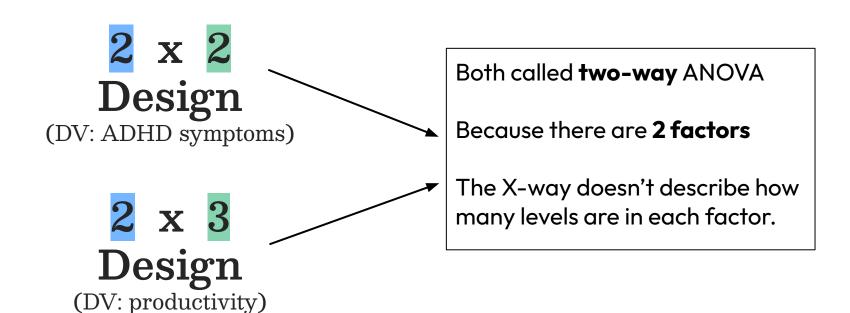


2 x 3
Design
(DV: productivity)

If you see two numbers multiplied (e.g., 2×3), that means there are 2 **factors**. Something like 2×3×2 means 3 **factors**. Each number shows how many **levels** are in that factor—so 2×3 means the first factor has 2 **levels**, the second has 3.

While factorial ANOVAs can include more than 2 factors, most of the time we focus on 2-factor designs. That's usually what people mean when they say "Factorial ANOVA."

In other words



As you notice, factorial ANOVA can have 2, or more than 2 factors.

Unlike One-Way ANOVA, where the single factor must have more than 2 levels (otherwise we'd just use a t-test), each factor in a factorial ANOVA can have as few as

two levels." levels are in each factor.

Two levels per factor is totally valid—you just need at least two factors to call it a factorial design.

In other words

One-way ANOVA → lower limit on the number of groups (>2)

Factorial ANOVA → lower limit on the number of levels within each factor (>=2)

AND

lower limit on the number of factors (>=2)

(DV: productivity)

Knowledge Check

Read your scenario and **identify the number of factors** and the **number of levels** for each factor.

Determine the **factorial design** (e.g., 2 × 2, 3 × 4) and write it clearly.

Draw the design on your notes (a table, matrix, or grid), with clear labels for each factor and its levels.

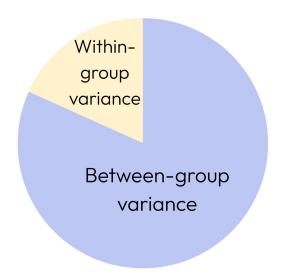
02 Main Effects & Interactions

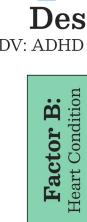
Let's approach the difference through this...

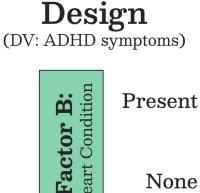
In one-way ANOVA we talked about "analyzing the variance" of the DV:

See how you can fit this factorial ANOVA into the variance pie:

Hint: "between" only had one factor before. What about now?







Stimulant Has heart Present condition and on stimulant



ADHD medications

Non-Stimulant

Factor A:

Has heart condition and not on stimulant

No heart condition and not on stimulant

We just break up the between-group variance!

Both of the factors are between-subjects / between groups!



Factor A: ADHD medications

Stimulant

Non-Stimulant

Factor B:
Heart Condition

Present

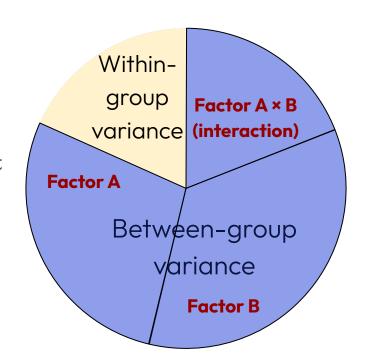
None

Has heart condition and on stimulant

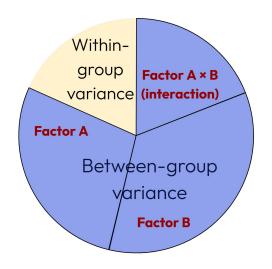
No heart condition and on stimulant

Has heart condition and not on stimulant

No heart condition and not on stimulant



Terminology in stats lingo



Factor A: ADHD medications

Factor B: Heart condition

Main effect is the independent influence of one factor (IV) on the dependent variable (DV), at the average level of the other factor.

The **main effect of Factor A** means that:

Does the type of ADHD medication reduce symptoms, regardless of whether someone has a heart condition?

That's what we mean when we say 'averaged across' the other factor."

See if you can explain the main effect of Factor B in groups!

2 x 2 Design

(DV: ADHD symptoms)



Present

None

Factor A:

ADHD medications

Stimulant

Non-Stimulant

Has heart condition and on stimulant

No heart condition and on stimulant

Has heart condition and not on stimulant

No heart condition and not on stimulant

Does ADHD symptom severity differ between **stimulants** and **non-stimulants**?

2 x 2 Design (DV: ADHD symptoms)

Factor A:ADHD medications

Stimulant Non-Stimulant

Factor B: Heart Condition

Present

None

Has heart condition and on stimulant

No heart condition and on stimulant

No heart condition and not on stimulant

Has heart

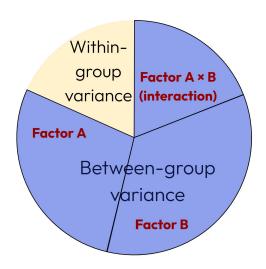
condition and

not on

stimulant

Does ADHD symptom severity differ between those who have heart and those who don't?

Terminology in stats lingo



Factor A: ADHD medications

Factor B: Heart condition

An **interaction** occurs when when the effect of one factor **depends on** the level of the other factor.

- Stimulants reduce ADHD symptoms more than non-stimulants. (main effect of Factor A)
- Heart condition status doesn't change ADHD symptom severity on its own. (No main effect of Factor B)
- But: Stimulants work well only for people without heart conditions, and don't help (or may even harm) those with heart conditions. (interaction)

The effect of medication depends on whether someone has a heart condition.

Terminology in stats lingo

Which medication would you recommend to treat

facADHD?ds on the level of the other factor.

- It depends...ts. (main effect of Factor A)
 - Heart condition status doesn't change ADHD

So which medication would you recommend to someone with a heart condition?

What about for someone without a heart condition?

The effect of medication depends on whether someone has a heart condition.

Let's assume for a second that there isn't an interaction...

Which medication would you recommend to treat ADHD?

In this case, the outcome only depends on one factor, most likely the ADHD med type

So you will make your recommendation based on which med type is more effective, you don't have to worry about whether someone has heart conditions

03

Eyeball & Table Method

Finding Main Effects & Interactions

How do we know if we have a main effect or an interaction?

We conduct the factorial ANOVA and look at the *p*-value that correspond to each factor & the interaction!

Each time we look at a *p*-value, we're essentially performing a little hypothesis test—just like in other NHST procedures.

We will leave the calculation to the next class. For now, we will talk about how to tell **visually** whether there are main effects or interactions.

Finding Main Effects & Interactions



"Eyeball" Method

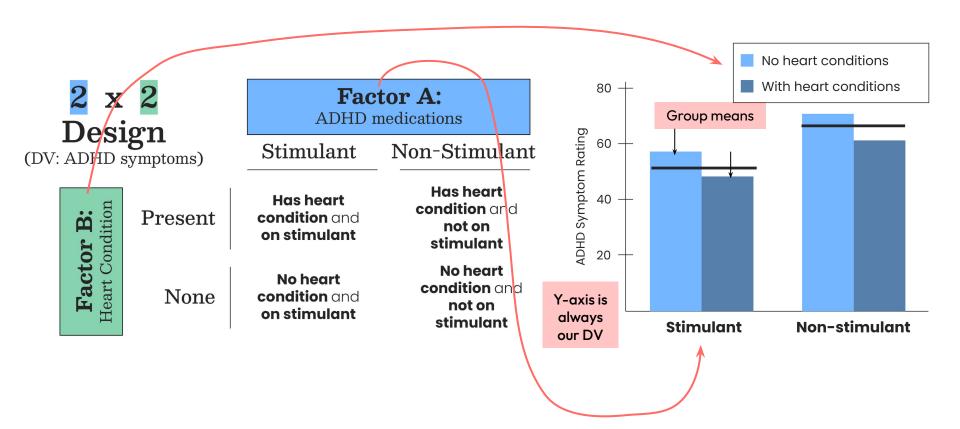
We can often spot main effects and interactions by **visually analyzing graphs**. We will learn some tricks for this today.



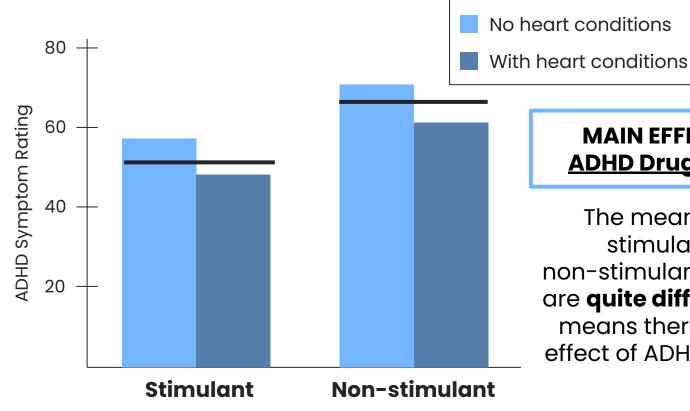
"Table" Method

Tables can give us **more precise information** and
can also help us decide
whether there are main
effects and/or interactions.

First, plotting the factorial ANOVA



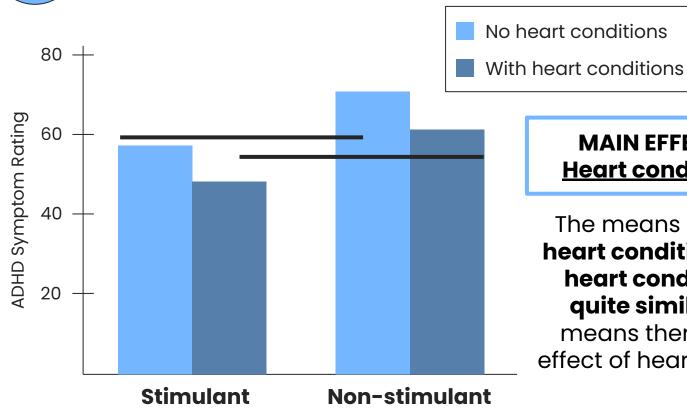




MAIN EFFECT of **ADHD Drug Type?**

The means for the stimulant and non-stimulant conditions are quite different, which means there is a main effect of ADHD drug type.

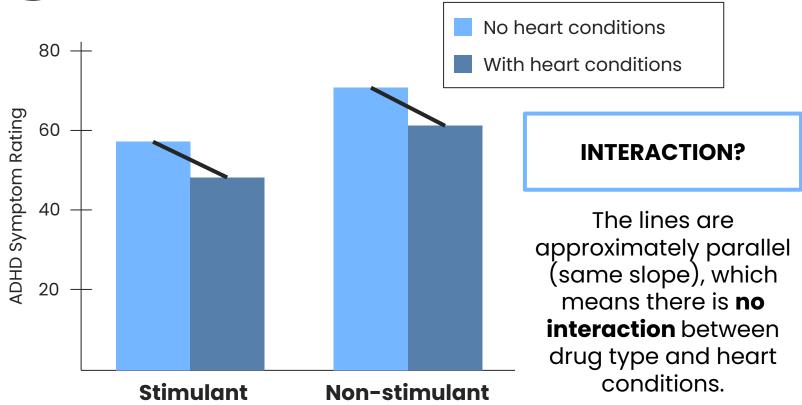




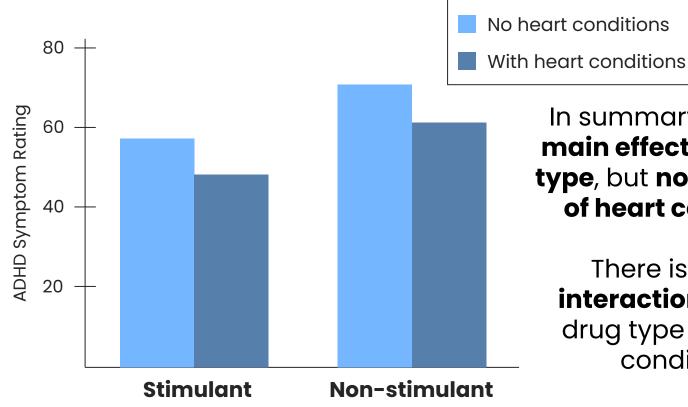
MAIN EFFECT of **Heart conditions?**

The means for the **has heart conditions** and **no** heart conditions are quite similar, which means there **no** main effect of heart conditions.









In summary, there is a main effect ADHD drug type, but no main effect of heart conditions.

There is also **no** interaction between drug type and heart conditions.

Research Example

Factor A: Emotion

Happy

Angry







Clean-Shaven

Beard

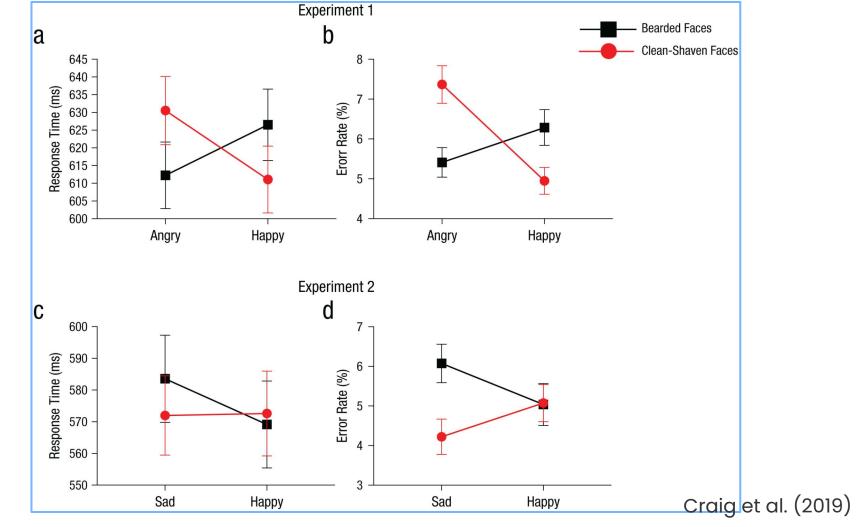


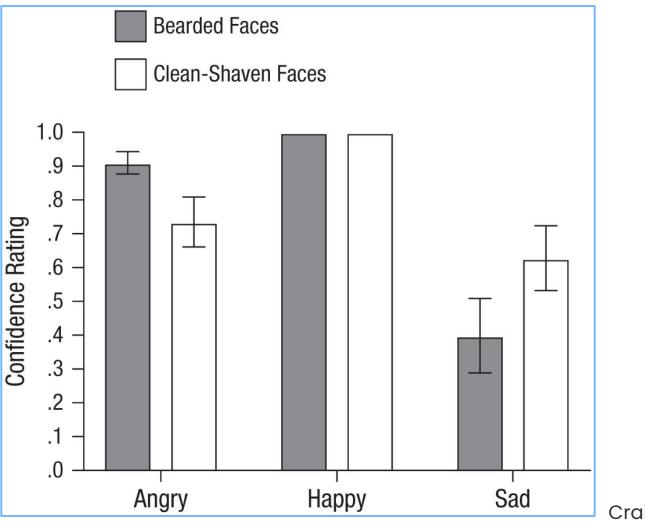


Craig et al. (2019) investigated whether beards enhance recognition of threatening expressions like anger.

They presented participants with photographs of the same men bearded and clean-shaven posing as either happy or angry.

Participants were asked to categorize each face as either 'happy' or 'angry' as quickly and accurately as possible.





Craig et al. (2019)





MAIN EFFECT EMOTION?

The means for the angry and happy conditions are **very different**, which means there **is** a main effect.

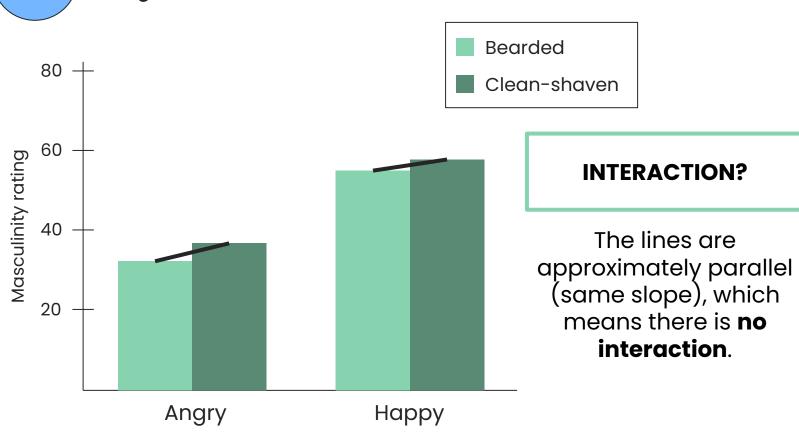




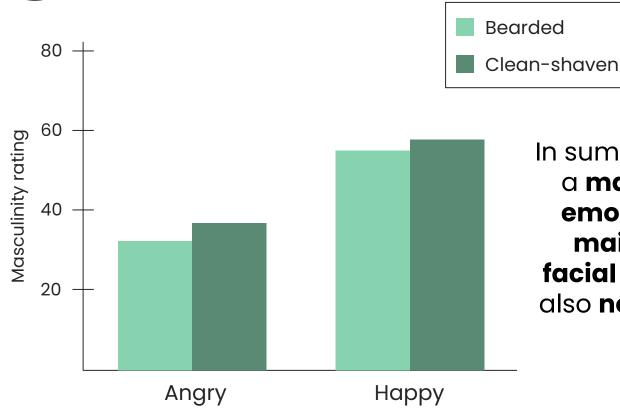
MAIN EFFECT FACIAL HAIR?

The means for the bearded and clean-shaven conditions are similar which means there is **not** likely main effect.









In summary, there is a main effect of emotion, but no main effect of facial hair. There is also no interaction.





MAIN EFFECT EMOTION?

The means for the angry and happy conditions are **very different**, which means there **is** a main effect.

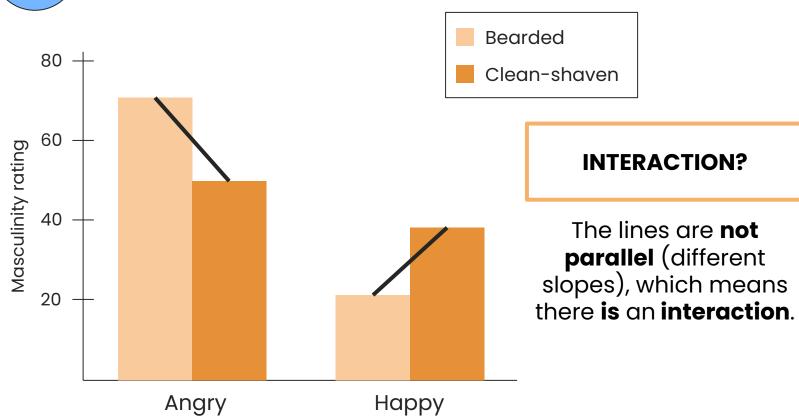




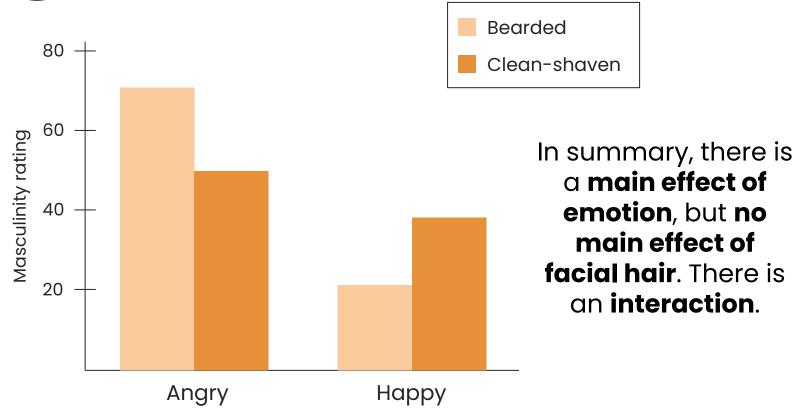
MAIN EFFECT FACIAL HAIR?

The means for the bearded and clean-shaven conditions are similar which means there is **not** likely main effect.









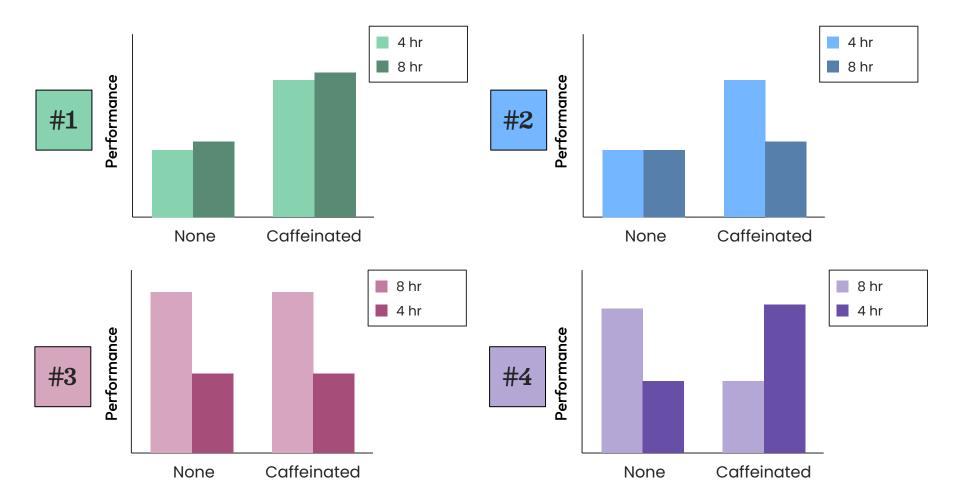
ICA 16

Researchers examine whether the effect of **caffeine** on **cognitive performance** depends on how much **sleep** someone had the night before.

IVs: Caffeine: None vs. Caffeinated;

Sleep Quality: Well-rested (8h) vs. Sleep-deprived (4h)

DV: **Performance** on a sustained attention task (0-100)





"Table" Method (main effects)

For main effects, we **compare the difference in the marginal means** for both factors to see if it is *more than the error*.

		Factor A: Treatment		Marginal Means
		CBT	Mindful.	Means
Factor B:	In-person	30	50	
Modality	Online	40	60	
Marginal Means				

Error: 15



"Table" Method (main effects)

		Factor A: Treatment		Marginal Means
		CBT	Mindful.	Ivicalis
Factor B: Modality	In-person	30	50	40
	Online	40	60	50
Marginal Means		35	55	

<u>no</u> main effect of

modality

Error: 15

20



a main effect of treatment



"Table" Method (interaction)

If the **change** in the cell means is **about the same**, then there is **no interaction**.

		Factor A: Treatment			Marginal Means	
		CBT		Mindful.		ivicalis
Factor B: Modality	In-person	30	+2	20	50	40
	Online	40	+2	20	60	50
Marginal Means		35			55	

Error: 15

"Table" Method (example)

Are there any **main effects** or **interactions**?

		Factor A: Treatment		Marginal Means
			Mindful.	Ivicalis
Factor B: Modality	In-person	5	9	
	Online	7	4	
Marginal Means				

Error: 1.0

"Table" Method (example)

Are there any main effects or interactions?

			Factor A: Treatment	
		CBT	Mindful.	Means
Factor B: Modality	In-person	5	9	7
	Online	7	4	5.5
Marginal Means		6	6.5	

Error: 1.0

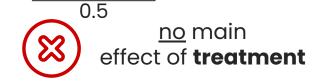


"Table" Method (example)

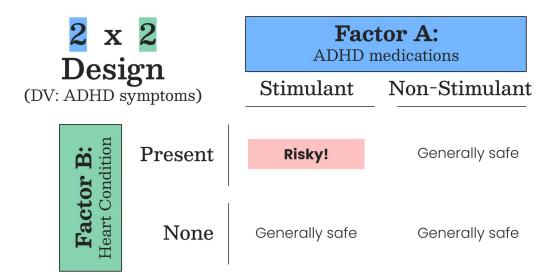
Are there any main effects or interactions?

between modality Treatment Marginal Means	
and treatment CBT Mindful.	
Factor B: In-person 5 +4 9 7	
Modality Online 7 -3 4 5.5 a	main
	fect of odality

Error: 1.0



Interactions change your entire story



In our ADHD example, stimulants may show a main effect of reducing symptoms overall.
But the interaction tells us something more important:
Stimulants help one group (no heart condition) but may worsen symptoms or have no effect for the other group (with heart condition).

IF there is an interaction: You have to interpret the main effect in light of the interaction—because the effect isn't the same across groups.

04 Wrap Up

Key Takeaways

- Factorial ANOVA
 - Terms (levels, factors, 2x2, 2x3...)
 - O WHY?
 - Main effect & interaction
 - Partitioning our variance pie into main effect & interaction
- Spotting main effects & interaction using eyeball & table methods

