

# **Factorial ANOVA**

## **(part 2)**

Lecture 17  
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# Recap: From our last class

- Factorial ANOVA ( $2 \times 2$ ,  $2 \times 3$ , ...)

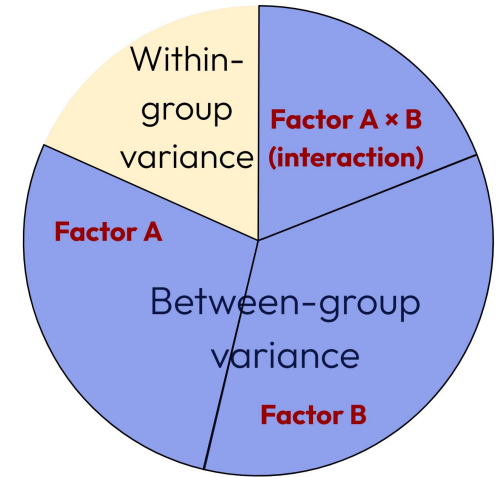
**2 x 2**  
**Design**  
(DV: ADHD symptoms)

**Factor B:**  
Heart Condition

Present

None

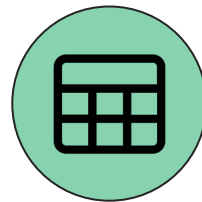
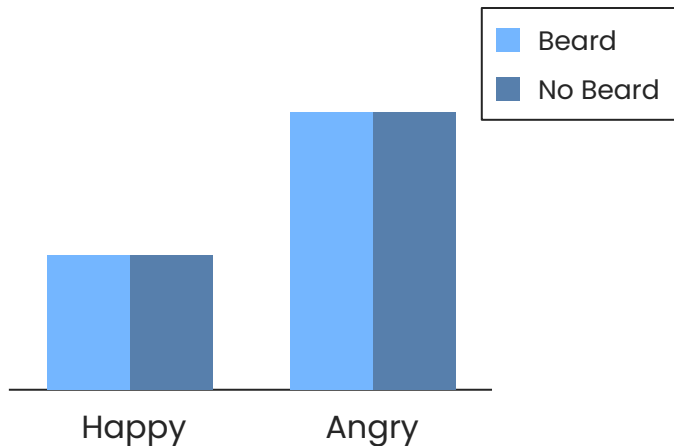
<b>Factor A:</b> ADHD medications	
Stimulant	Non-Stimulant
Has heart condition and on stimulant	Has heart condition and not on stimulant
No heart condition and on stimulant	No heart condition and not on stimulant



# Recap: Visually identify main effects & interaction



## “Eyeball” Method



## “Table” Method

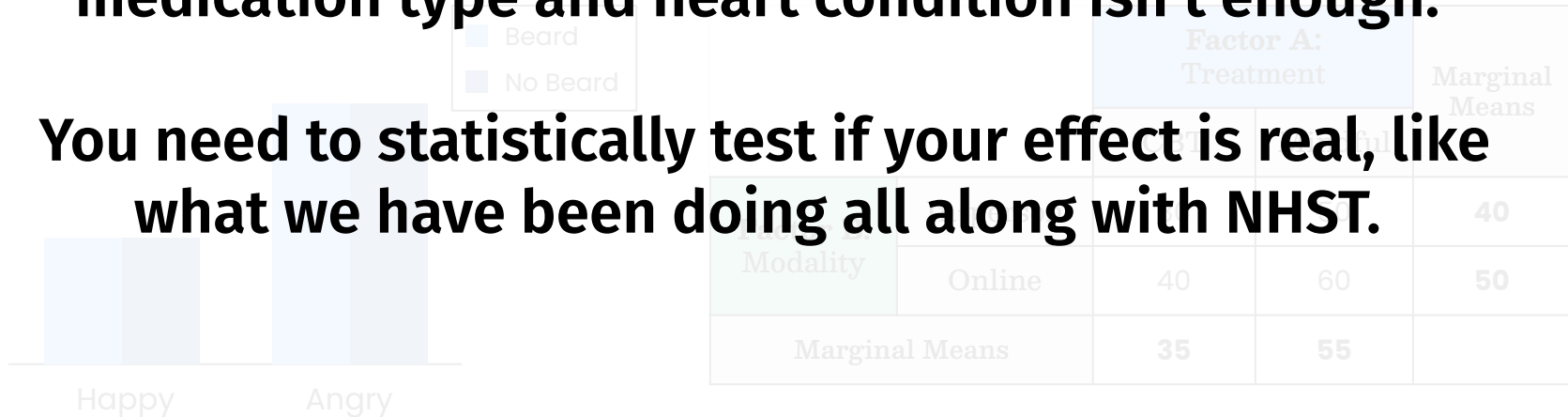
		Factor A: Treatment		Marginal Means
		CBT	Mindful	
Factor B: Modality	In-person	30	50	<b>40</b>
	Online	40	60	<b>50</b>
Marginal Means		<b>35</b>	<b>55</b>	

## Recap: Visually identify main effects & interaction

Going back to our example from last class...

If you're deciding which ADHD medication to recommend, just seeing an interaction between medication type and heart condition isn't enough.

You need to statistically test if your effect is real, like what we have been doing all along with NHST.



# TODAY'S PLAN

**01**

**Key Concepts**

**02**

**Factorial ANOVA Source  
Table**

**03**

**Worked Example**

**04**

**Exam 2 Information &  
Wrap Up**

# Learning objectives

- **Conduct** a two-way (two-factor) ANOVA, including measures of effect size, for both main effects and the interaction.
- Complete a two-way ANOVA **source table** (when given initial numbers).
- **Report and interpret** the results of a two-way ANOVA are reported in APA style.



# Key Concepts

# Let's think with what we already know...

Since our goal is to statistically test whether the main effects and interactions are real, we know based on our experience so far that:

- We need some kind of **statistic** to make **decisions** with!
  - In independent and paired t-tests, we used the t-statistic
  - In one-way ANOVA, we used the F-statistic

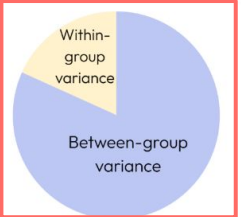
Okay, we are getting somewhere!

Since factorial ANOVA is just an extension of one-way ANOVA, we should probably still use the F-statistic

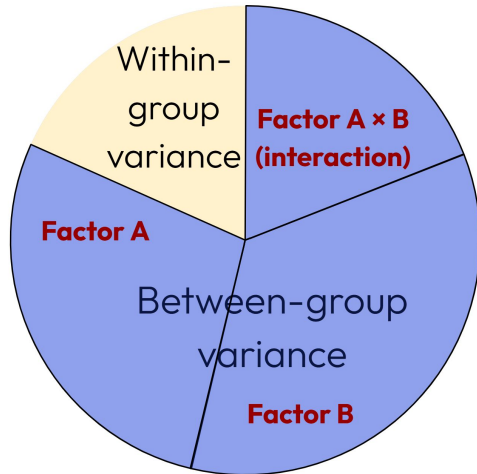
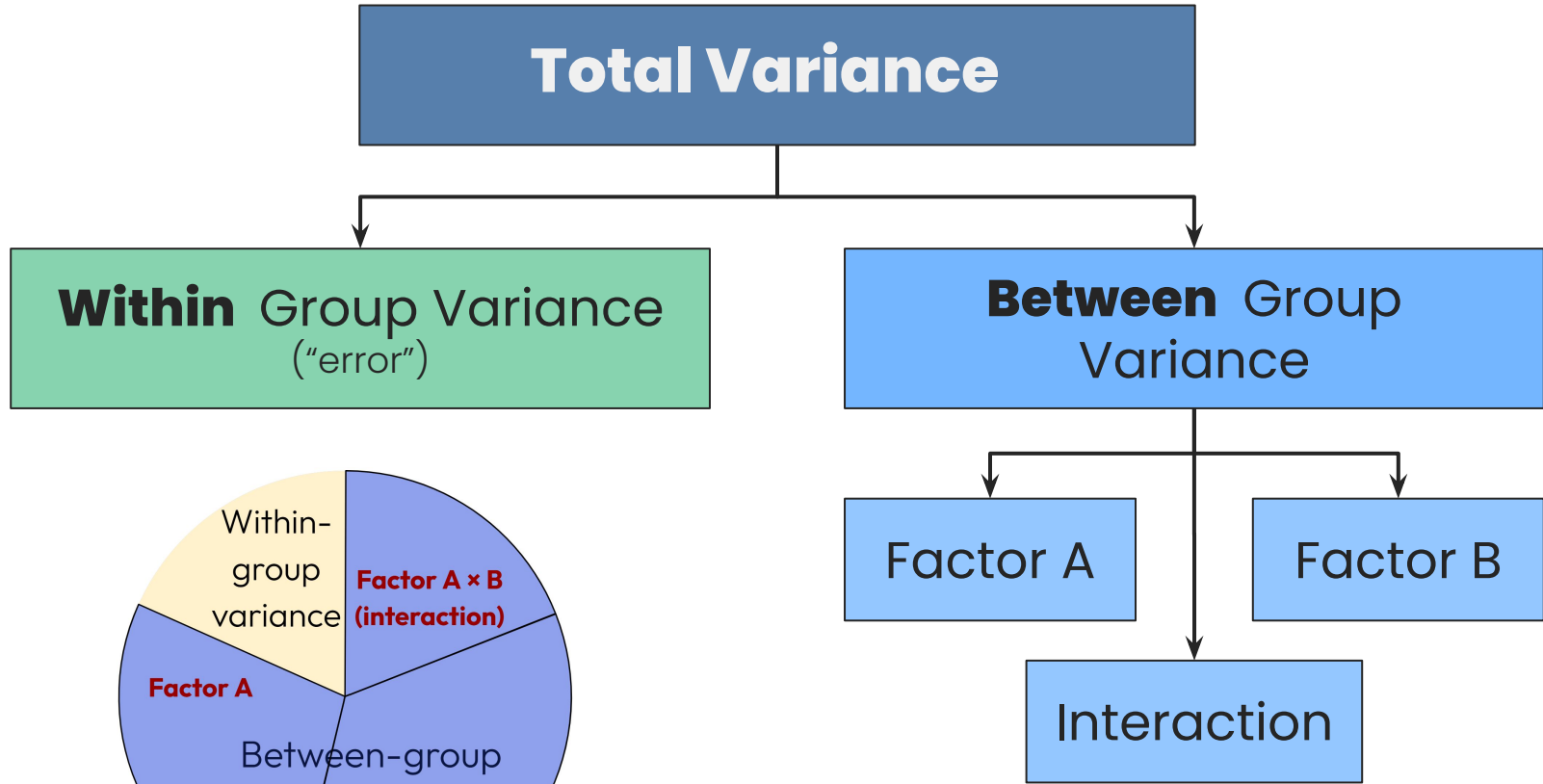


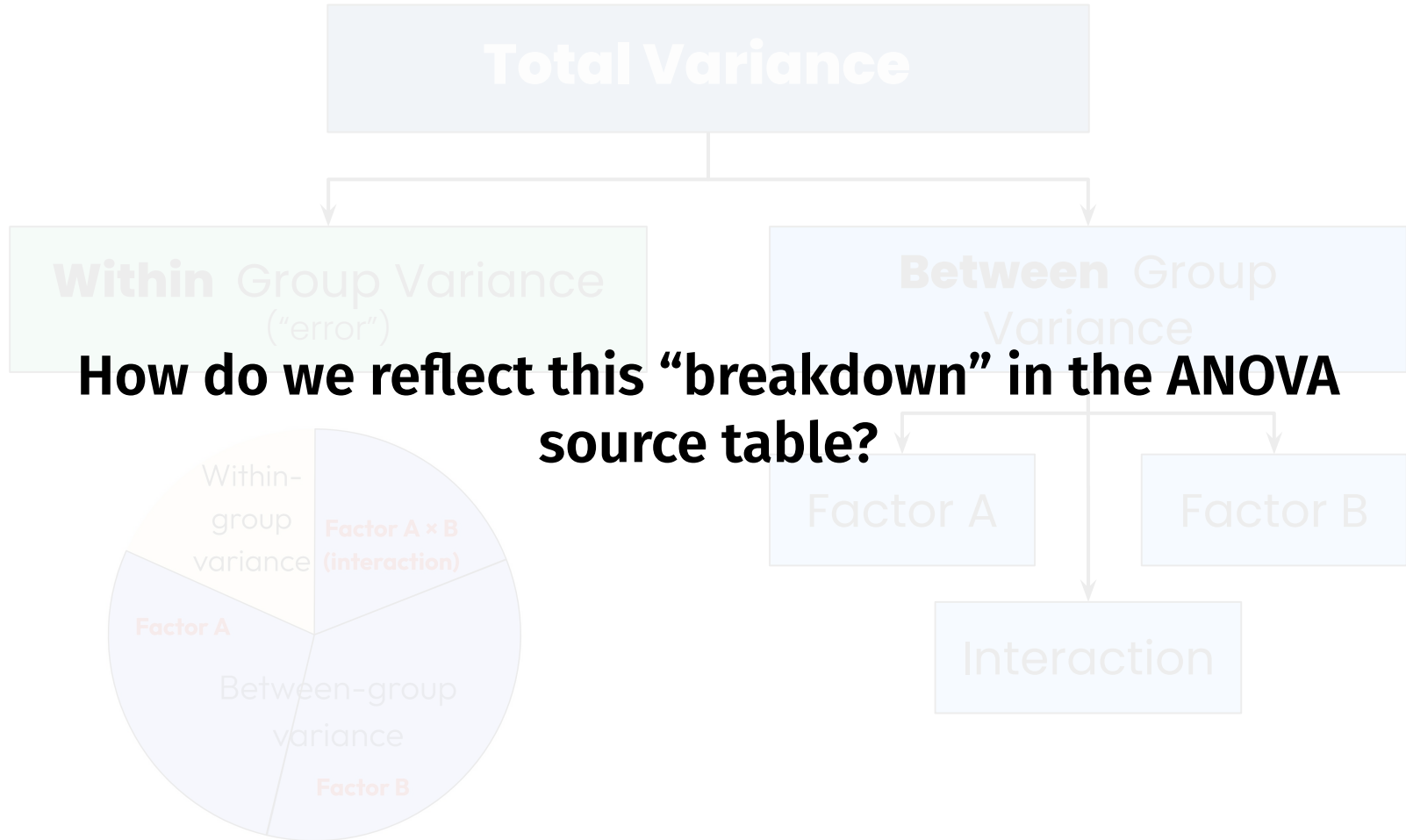
# Factorial ANOVA is just an extension of One-way ANOVA

This is the one-way ANOVA source table:

Source	<i>SS</i>	<i>df</i>	<i>MS</i>	<i>F</i>
Between		$k - 1$	$SS_b / df_b$	$MS_b / MS_w$
Within		$N - k$	$SS_w / df_w$	
Total	$SS_b + SS_w$	$N - 1$		

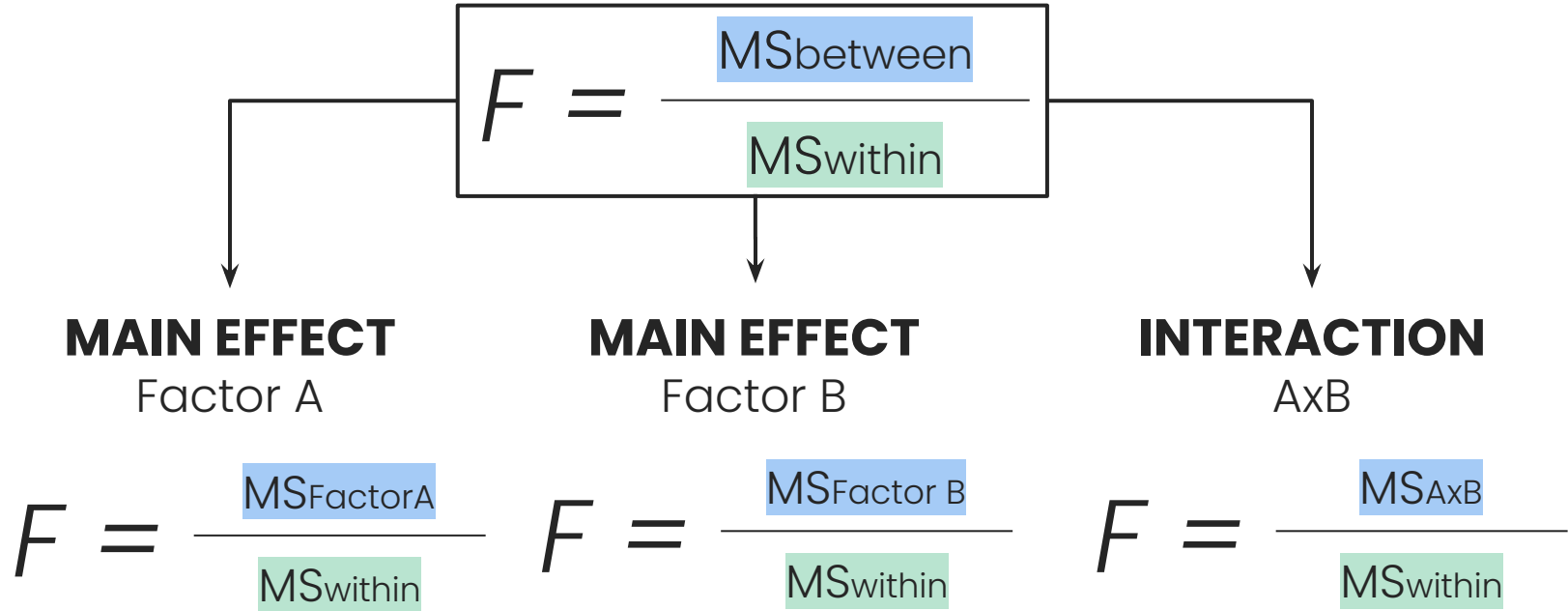
These will probably change!





# Three F-Ratios

Because of between-group variance is now **split into three**, we need to calculate **three separate F-ratios**



For *each* of the three F-ratios, we compare the calculated F-ratio to the  $F_{\text{crit}}$  to determine whether the main effects or interaction are “statistically significant.”

This is like doing 3 separate NHST tests!

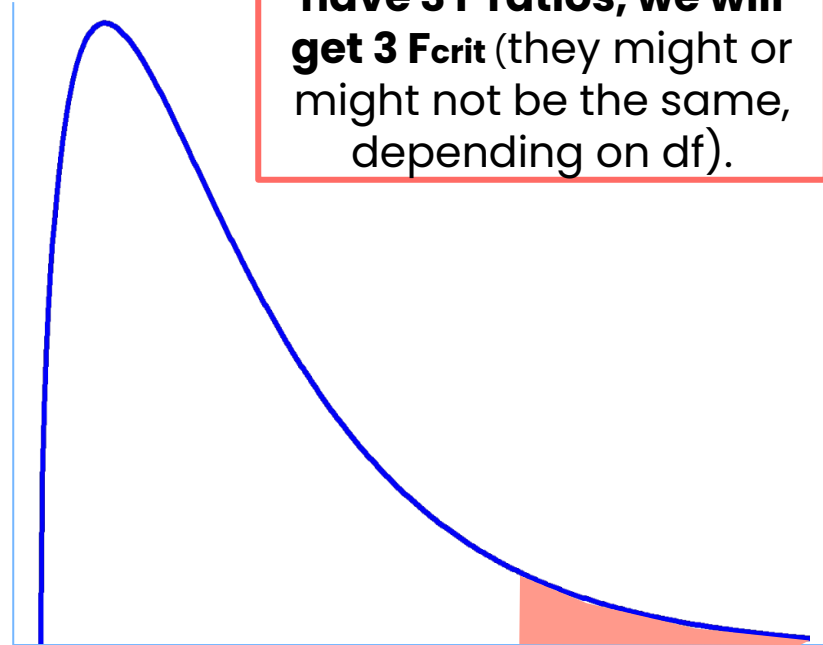
Our null: there is no effect

Our alternative: there is an effect

# Use an F-Table to find your critical value ( $F_{\text{CRIT}}$ )

$df_{\text{within}}$ (denominator)	$df_{\text{between}}$ (numerator)									
	1	2	3	4	5	6	7	8	9	10
1	161	200	216	225	230	234	237	239	241	242
2	18.51	19.00	19.16	19.25	19.30	19.33	19.36	19.37	19.38	19.39
3	10.13	9.55	9.28	9.12	9.01	8.94	8.88	8.84	8.81	8.78
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.78	4.74
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.63
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.34
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.13
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.97
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.86
12	4.75	3.88	3.49	3.26	3.11	3.00	2.92	2.85	2.80	2.76
13	4.67	3.80	3.41	3.18	3.02	2.92	2.84	2.77	2.72	2.67
14	4.60	3.74	3.34	3.11	2.96	2.85	2.77	2.70	2.65	2.60
15	4.54	3.68	3.29	3.06	2.90	2.79	2.70	2.64	2.59	2.55
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49

**Note:** We use the F-table to find the  $F_{\text{crit}}$ . **Since we have 3 F ratios, we will get 3  $F_{\text{crit}}$**  (they might or might not be the same, depending on df).



# Effect Size

For a two-factor ANOVA, we compute **three** separate values for  $\eta^2$  (**eta-squared**): one measuring *the percentage of the variance explained* by 1) the main effect for factor A, 2) the main effect for factor B, and 3) the interaction.

## MAIN EFFECT

Factor A

$$\eta_p^2 = \frac{SS_A}{SS_A + SS_{\text{within}}}$$

## MAIN EFFECT

Factor B

$$\eta_p^2 = \frac{SS_B}{SS_B + SS_{\text{within}}}$$

## INTERACTION

AxB

$$\eta_p^2 = \frac{SS_{A \times B}}{SS_{A \times B} + SS_{\text{within}}}$$

We call these **partial eta-squared** ( $\eta_p^2$ ). There's also regular **eta-squared** ( $\eta^2$ ). Since reporting one is sufficient, we won't go into the calculation for  $\eta^2$ .



# **Factorial ANOVA Source Table**



# Factorial ANOVA Source Table

Source	SS	df	MS	F
Between				
→ Factor A				
→ Factor B				
→ Interaction				
Within				
Total				

*Our between group variance is now split into 3 parts*

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>		$k - 1$		
→ Factor A		$k_A - 1$		
→ Factor B		$k_B - 1$		
→ Interaction ( $A \times B$ )		$df_A \times df_B$		
<b>Within</b>		$N - k$		
<b>Total</b>		$N - 1$		

**TIP 1:** Start with **df** calculations (**k** = # of **cells**, **k<sub>A</sub>** = # of levels for Factor A, **k<sub>B</sub>** = # of levels for Factor B, **N** = total sample size)

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>		<b>5</b>		
→ Factor A		1		
→ Factor B		2		
→ Interaction (AxB)		2		
<b>Within</b>		18		
<b>Total</b>				

**TIP 2:**  $SS_{\text{between}} = SS_A + SS_B + SS_{A \times B}$   
 $df_{\text{between}} = df_A + df_B + df_{A \times B}$

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	<b>120</b>	<b>5</b>		
→ Factor A	70	1		
→ Factor B	40	2		
→ Interaction (AxB)	10	2		
<b>Within</b>		18		
<b>Total</b>				

**TIP 2:**  $SS_{\text{between}} = SS_A + SS_B + SS_{A \times B}$   
 $df_{\text{between}} = df_A + df_B + df_{A \times B}$

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	120	5		
→ Factor A	70	1		
→ Factor B	40	2		
→ Interaction (AxB)	10	2		
<b>Within</b>	180	18		
<b>Total</b>	300	23		

**TIP 3:**  $SS_{\text{total}} = SS_{\text{between}} + SS_{\text{within}}$   
 $df_{\text{total}} = df_{\text{between}} + df_{\text{within}}$

# Factorial ANOVA Source Table

Source	SS	df	MS	F
Between	120	5		
→ Factor A	70	1		
→ Factor B	40	2		
→ Interaction (AxB)	10	2		
Within	180	18		
Total				

**TIP 4: Divide across** to get your four MS values.

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	120	5		
→ Factor A	70	1	70	
→ Factor B	40	2	20	
→ Interaction (AxB)	10	2	5	
<b>Within</b>	180	18	10	
<b>Total</b>				

**TIP 4: Divide across** to get your four MS values.

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	120	5		
→ Factor A	70 ÷	1	→ 70	?
→ Factor B	40 ÷	2	→ 20	?
→ Interaction (AxB)	10 ÷	2	→ 5	?
<b>Within</b>	180 ÷	18	→ 10	
<b>Total</b>				

**TIP 4: Divide across** to get your four MS values.



# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	120	5		<b><math>MS_A/MS_B/MS_{A \times B}</math></b> are your 3 numerators
→ Factor A	70	1	<b>70</b>	
→ Factor B	40	2	<b>20</b>	
→ Interaction ( $A \times B$ )	10	2	<b>5</b>	
<b>Within</b>	180	18	<b>10</b>	<b><math>MS_{within}</math></b> is your denominator
<b>Total</b>				

**TIP 5:** Divide  **$MS_A$** ,  **$MS_B$** , and  **$MS_{A \times B}$**  by  **$MS_{within}$**  (three calculations)

# Factorial ANOVA Source Table

Source	SS	df	MS	F
<b>Between</b>	120	5		
→ Factor A	70	1	70	7
→ Factor B	40	2	20	2
→ Interaction ( $A \times B$ )	10	2	5	0.5
<b>Within</b>	180	18	10	
<b>Total</b>				

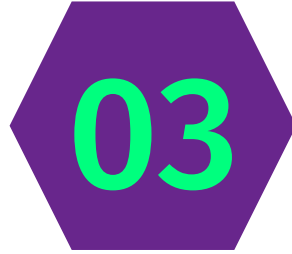
**TIP 5:** Divide  $MS_A$ ,  $MS_B$ , and  $MS_{A \times B}$  by  $MS_{within}$  (three calculations)

# Practice: Factorial ANOVA

Source	SS	df	MS	F
Between	75	3		
→ Factor A	50	1		
→ Factor B	20	1		
→ Interaction				
Within	500	100		
Total				

# Practice: Factorial ANOVA

Source	SS	df	MS	F
Between	75	3		
→ Factor A	50	1	50	10
→ Factor B	20	1	20	4
→ Interaction	5	1	5	1
Within	500	100	5	
Total	575	103		



# Worked Example

# Example Problem

A psychologist wants to know if the effectiveness of learning format (video vs. podcast) depends on the age of the learner. They conduct a 2 (**Age**: Teens vs. Adults)  $\times$  2 (**Format**: Video vs. Podcast) factorial ANOVA. Their dependent variable (DV) is performance on a comprehension quiz about the material. The psychologist recruits 24 participants, evenly distributed across the 4 cells of the study design (6 participants per condition).

		Factor A: Age	
		Teens	Adults
Factor B: Format	Video	85	65
	Podcast	90	80

# Worked Example

Source	SS	df	MS	F
<b>Between</b>				
→ Factor A (age)	25			
→ Factor B (format)	75			
→ Interaction (AxB)	40			
<b>Within</b>	100			
<b>Total</b>				

Where shall we start?

# Worked Example

Source	SS	df	MS	F
<b>Between</b>		$k - 1$		
→ Factor A (age)	25	$k_A - 1$		
→ Factor B (format)	75	$k_B - 1$		
→ Interaction (AxB)	40	$df_A \times df_B$		
<b>Within</b>	100	$N - k$		
<b>Total</b>		$N - 1$		

Start with **df** calculations (**k** = # of cells, **k<sub>A</sub>** = # of levels for Factor A, **k<sub>B</sub>** = # of levels for Factor B, **N** = total sample size)



# Worked Example

Source	SS	df	MS	F
<b>Between</b>		<b>3</b>		
→ Factor A (age)	25	<b>1</b>		
→ Factor B (format)	75	<b>1</b>		
→ Interaction (AxB)	40	<b>1</b>		
<b>Within</b>	100	<b>20</b>		
<b>Total</b>		<b>23</b>		

Start with **df** calculations (**k** = # of cells, **k<sub>A</sub>** = # of levels for Factor A, **k<sub>B</sub>** = # of levels for Factor B, **N** = total sample size)

# Worked Example

Source	SS	df	MS	F
<b>Between</b>	<b>140</b>	3		
→ Factor A (age)	25	1		
→ Factor B (format)	75	1		
→ Interaction (AxB)	40	1		
<b>Within</b>	100	20		
<b>Total</b>	<b>240</b>	23		

$$\mathbf{SS_{between}} = SS_A + SS_B + SS_{A \times B}$$

$$\mathbf{SS_{between}} = 25 + 75 + 40 = \mathbf{140}$$

$$\mathbf{SS_{total}} = SS_{between} + SS_{within}$$

$$\mathbf{SS_{total}} = 140 + 100 = \mathbf{240}$$

# Worked Example

Source	SS	df	MS	F
<b>Between</b>	140	3		
→ Factor A (age)	25 ÷	1	→ 25	
→ Factor B (format)	75 ÷	1	→ 75	
→ Interaction (AxB)	40 ÷	1	→ 40	
<b>Within</b>	100 ÷	20	→ 5	
<b>Total</b>	240	23		

**Divide across** to get your four MS values.

# Worked Example

Source	SS	df	MS	F
<b>Between</b>	140	3		
→ Factor A (age)	25	1	25	numerators
→ Factor B (format)	75	1	75	
→ Interaction (AxB)	40	1	40	
<b>Within</b>	100	20	5	
<b>Total</b>	240	23		denominator

Divide **MS<sub>A</sub>**, **MS<sub>B</sub>**, and **MS<sub>AxB</sub>** by **MS<sub>within</sub>** (three calculations)

# Worked Example

<b>Source</b>	<b>SS</b>	<b>df</b>	<b>MS</b>	<b>F</b>
<b>Between</b>	140	3		
→ Factor A (age)	25	1	25	<b>5</b>
→ Factor B (format)	75	1	75	<b>15</b>
→ Interaction (AxB)	40	1	40	<b>8</b>
<b>Within</b>	100	20	5	
<b>Total</b>	240	23		

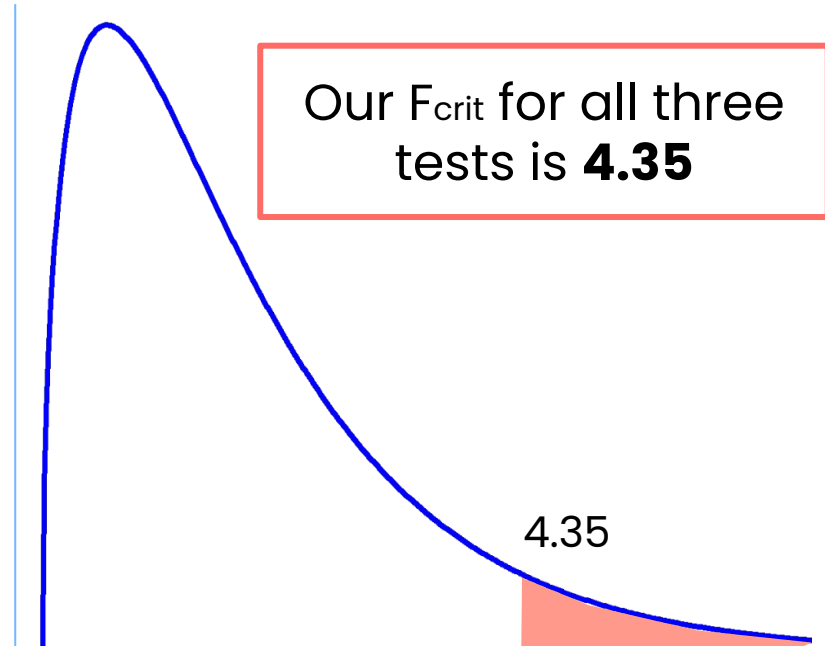
# Worked Example

Source	SS	df	MS	F
<b>Between</b>	140	3		
→ Factor A (age)	25	1	25	5
→ Factor B (format)	75	1	75	15
→ Interaction ( $A \times B$ )	40	1	40	8
<b>Within</b>	100	20	5	
<b>Total</b>	240	23		

Because  $df_A$ ,  $df_B$ ,  $df_{A \times B}$   
**all equal 1**, we will  
have the same  $F_{crit}$   
for all three F-ratios.

# F<sub>crit</sub>

<b>df<sub>within</sub></b> (denominator)	<b>df<sub>between</sub></b> (numerator)									
	1	2	3	4	5	6	7	8	9	10
1	161	200	216	225	230	234	237	239	241	242
2	18.51	19.00	19.16	19.25	19.30	19.33	19.36	19.37	19.38	19.39
3	10.13	9.55	9.28	9.12	9.01	8.94	8.88	8.84	8.81	8.78
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.78	4.74
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.63
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.34
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.13
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.97
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.86
12	4.75	3.88	3.49	3.26	3.11	3.00	2.92	2.85	2.80	2.76
13	4.67	3.80	3.41	3.18	3.02	2.92	2.84	2.77	2.72	2.67
14	4.60	3.74	3.34	3.11	2.96	2.85	2.77	2.70	2.65	2.60
15	4.54	3.68	3.29	3.06	2.90	2.79	2.70	2.64	2.59	2.55
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49
17	4.45	3.59	3.20	2.96	2.81	2.70	2.62	2.55	2.50	2.45
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41
19	4.38	3.52	3.13	2.90	2.74	2.63	2.55	2.48	2.43	2.38
20	4.35	3.49	3.10	2.87	2.71	2.60	2.52	2.45	2.40	2.35



For *each* of the three F-ratios, we compare the calculated F-ratio to the  $F_{\text{crit}}$  to determine whether the main effects or interaction are “statistically significant.”



# Make Your Decisions

$F_{crit} = 4.35$

Source	SS	df	MS	F
<b>Between</b>	140	3		
→ Factor A (age)	25	1	25	5
→ Factor B (format)	75	1	75	15
→ Interaction (AxB)	40	1	40	8
<b>Within</b>	100	20	5	
<b>Total</b>	240	23		

**Main Effect** (Factor A)

5 > 4.35  
significant

**Main Effect** (Factor B)

15 > 4.35  
significant

**Interaction**

8 > 4.35  
significant

# Effect Size

Source	SS	df	MS	F
<b>Between</b>	140	3		
→ Factor A (age)	25	1	25	<b>5</b>
→ Factor B (format)	75	1	75	<b>15</b>
→ Interaction (AxB)	40	1	40	<b>8</b>
<b>Within</b>	100	20	5	
<b>Total</b>	240	23		

Source	SS
<b>Between</b>	140
→ Factor A (age)	25
→ Factor B (format)	75
→ Interaction (AxB)	40
<b>Within</b>	100
<b>Total</b>	240

# Effect Size

## MAIN EFFECT

Factor A

$$\eta^2_p = \frac{SS_A}{SS_A + SS_{\text{within}}}$$

$$\eta^2_p = \frac{25}{25 + 100}$$

$$= .20$$

## MAIN EFFECT

Factor B

$$\eta^2_p = \frac{SS_B}{SS_A + SS_{\text{within}}}$$

$$\eta^2_p = \frac{75}{75 + 100}$$

$$= .43$$

## INTERACTION

AxB

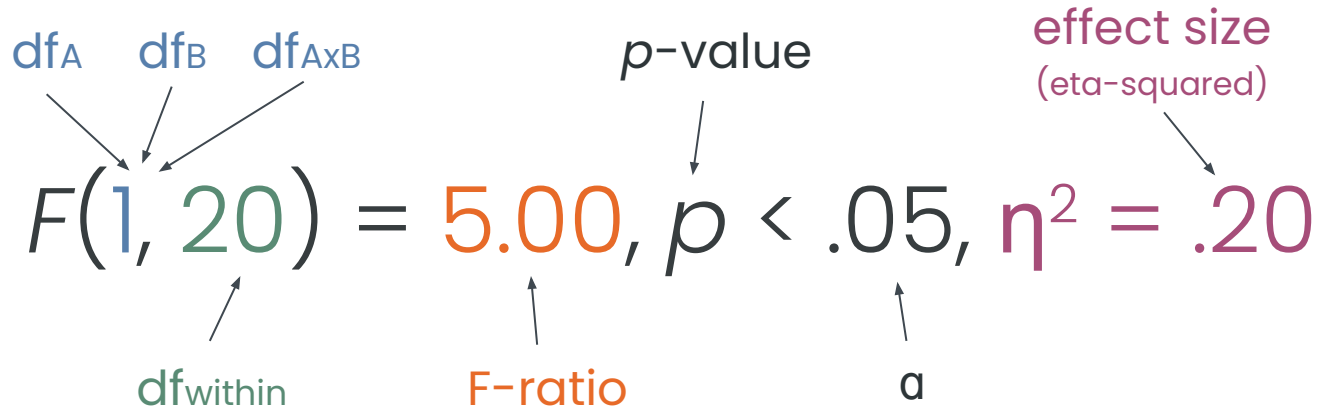
$$\eta^2_p = \frac{SS_{A \times B}}{SS_A + SS_{\text{within}}}$$

$$\eta^2_p = \frac{40}{40 + 100}$$

$$= .29$$

# Interpretation Template

(example for **factor A**)



The diagram illustrates the components of an F-test result. It features the equation  $F(1, 20) = 5.00, p < .05, \eta^2 = .20$ . Arrows point from descriptive labels to specific parts of the equation: 'df<sub>A</sub>' points to the first '1', 'df<sub>B</sub>' points to the '20', and 'df<sub>AxB</sub>' points to the '20'. 'p-value' points to the ' $p < .05$ ' part. 'effect size (eta-squared)' points to the ' $\eta^2 = .20$ ' part. 'df<sub>within</sub>' points to the '20' in the denominator of the F-ratio. 'F-ratio' points to the '5.00'. 'α' points to the '.05'.

df<sub>A</sub> df<sub>B</sub> df<sub>AxB</sub>

$F(1, 20) = 5.00, p < .05, \eta^2 = .20$

df<sub>within</sub> F-ratio α

p-value

effect size  
(eta-squared)

# Interpretation Template

A  $\_ \times \_$  factorial ANOVA was conducted to examine the effects of **[Factor A]** and **[Factor B]** on **[DV]**.

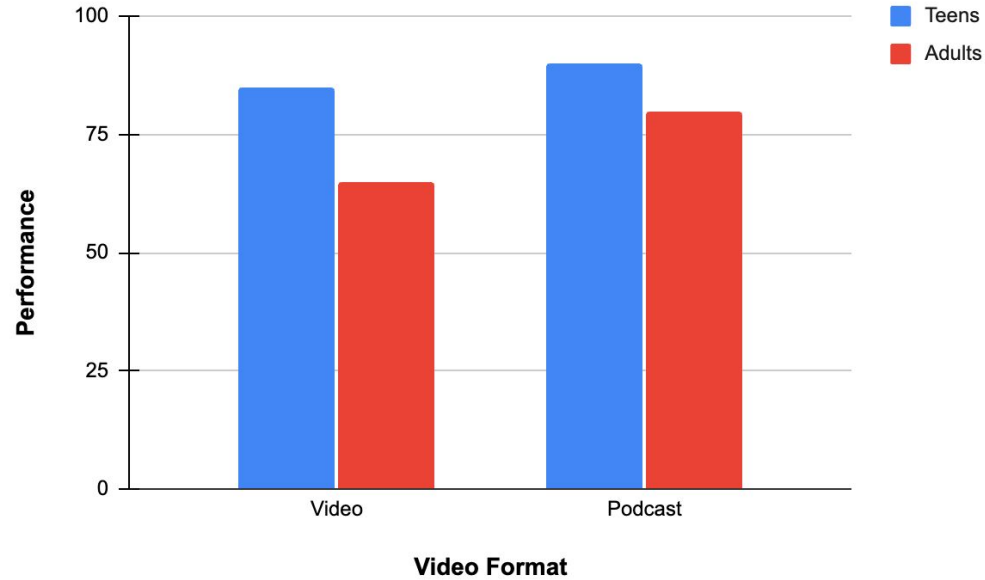
There *[was/was not]* a main effect of **[Factor A]**,  $F(?, ?) = ?, p (< \text{ or } >) .05$  and *[was/was not]* main effect of **[Factor B]**,  $F(?, ?) = ?, p (< \text{ or } >) .05$ .

There *[was/was not]* a significant **interaction** between **[Factor A]** and **[Factor B]**,  $F(?, ?) = ?, p (< \text{ or } >) .05$

# Interpretation

A  $2 \times 2$  factorial ANOVA was conducted to examine the effects of *age* and *learning format* on *comprehension scores*. There was a significant **main effect of age**,  $F(1, 20) = 5.00, p < .05$  and a significant **main effect of format**,  $F(1, 20) = 15.00, p < .05$ . There was also a significant **interaction** between age and format,  $F(1, 20) = 8.00, p < .05$ .

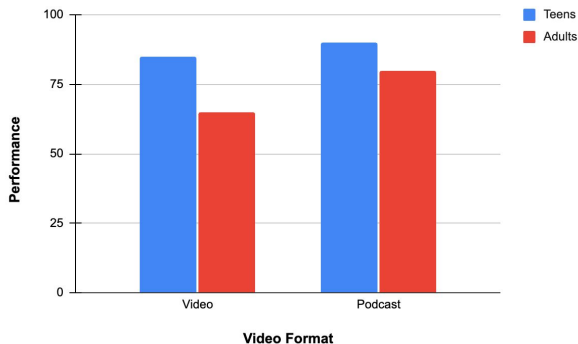
# Means Plot



# Interpretation, plain English

**If** there is a significant interaction, you should **only** write a plain-English interpretation **when a means plot is provided**. Without the plot, simply report the result in APA format (as shown on the previous slide).

*Interactions are tricky to interpret without visualizing them, so only interpret them when you can see the means plot.*



Overall, participants performed better when listening to the podcast than when watching the video, and teens performed better than adults. However, the effect of format depended on age: teens' performance stayed about the same across formats, whereas adults performed worse when switching from podcast to video.



# ICA 17

You conduct a study with a 2 x 2 factorial design examining the effect of personality (factor A) and caffeine (factor B) on mood. You split group **N = 84** participants into groups of 21 per cell/condition. (assume  $\alpha = .05$ )

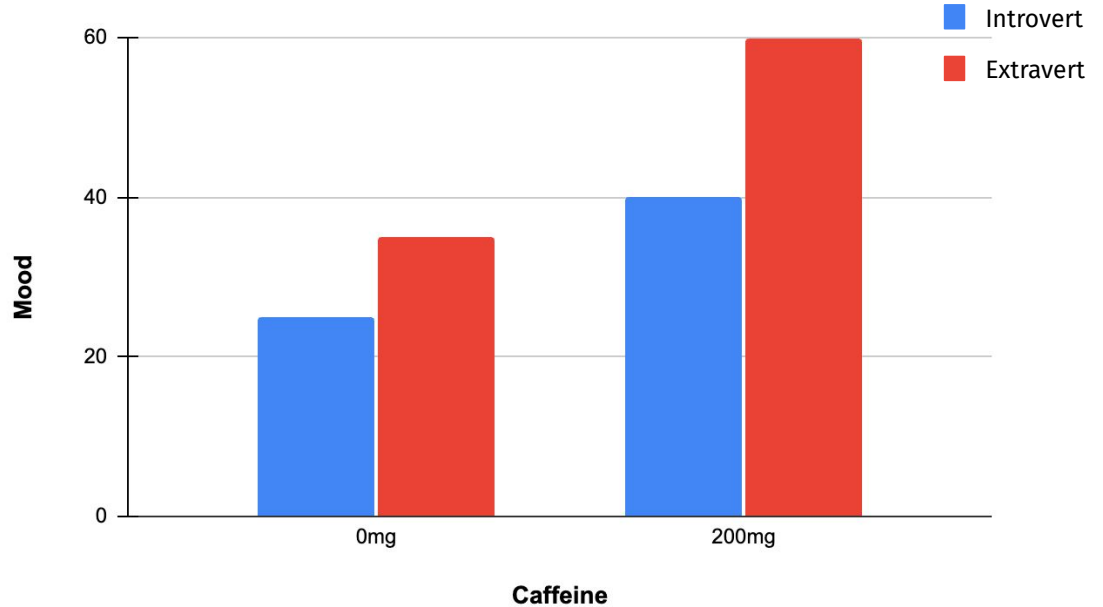
Using the formulas and the tips you learned, complete the table, calculate the effect size, and state decide whether there is a ...

- **Main effect** for factor A (personality)?
- **Main effect** for factor B (caffeine)?
- **Interaction?**

		Factor A: Personality	
		Introvert	Extravert
Factor B: Caffeine	0mg	25	35
	200mg	40	60

From our group means, we also get the means plot

		Factor A: Personality	
		Introvert	Extravert
Factor B: Caffeine	0mg	25	35
	200mg	40	60



# ICA 17 Source Table

Source	SS	df	MS	F
Between	100			
→ Factor A (personality)	10	1		
→ Factor B (caffeine)	50	1		
→ Interaction (AxB)				
Within	400	80		
Total		83		

<b><i>df</i>within</b> (denominator)	<b><i>df</i>between</b> (numerator)									
	1	2	3	4	5	6	7	8	9	10
<b>1</b>	161	200	216	225	230	234	237	239	241	242
<b>2</b>	18.51	19.00	19.16	19.25	19.30	19.33	19.36	19.37	19.38	19.39
<b>3</b>	10.13	9.55	9.28	9.12	9.01	8.94	8.88	8.84	8.81	8.78
<b>4</b>	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96
<b>5</b>	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.78	4.74
<b>6</b>	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06
<b>7</b>	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.63
<b>8</b>	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.34
<b>9</b>	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.13
<b>10</b>	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.97
<b>11</b>	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.86
<b>12</b>	4.75	3.88	3.49	3.26	3.11	3.00	2.92	2.85	2.80	2.76
<b>13</b>	4.67	3.80	3.41	3.18	3.02	2.92	2.84	2.77	2.72	2.67
<b>14</b>	4.60	3.74	3.34	3.11	2.96	2.85	2.77	2.70	2.65	2.60
<b>15</b>	4.54	3.68	3.29	3.06	2.90	2.79	2.70	2.64	2.59	2.55
<b>16</b>	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49
<b>17</b>	4.45	3.59	3.20	2.96	2.81	2.70	2.62	2.55	2.50	2.45
<b>19</b>	4.38	3.52	3.13	2.90	2.74	2.63	2.55	2.48	2.43	2.38
<b>21</b>	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32
<b>22</b>	4.30	3.44	3.05	2.82	2.66	2.55	2.47	2.40	2.35	2.30
<b>23</b>	4.28	3.42	3.03	2.80	2.64	2.53	2.45	2.38	2.32	2.28
<b>24</b>	4.26	3.40	3.01	2.78	2.62	2.51	2.43	2.36	2.30	2.26
<b>25</b>	4.24	3.38	2.99	2.76	2.60	2.49	2.41	2.34	2.28	2.24

<b><i>df</i>within</b> (denominator)	<b><i>df</i>between</b> (numerator)									
	1	2	3	4	5	6	7	8	9	10
<b>26</b>	4.22	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22
<b>27</b>	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.30	2.25	2.20
<b>28</b>	4.20	3.34	2.95	2.71	2.56	2.44	2.36	2.29	2.24	2.19
<b>29</b>	4.18	3.33	2.93	2.70	2.54	2.43	2.35	2.28	2.22	2.18
<b>30</b>	4.17	3.32	2.92	2.69	2.53	2.42	2.34	2.27	2.21	2.16
<b>32</b>	4.15	3.30	2.90	2.67	2.51	2.40	2.32	2.25	2.19	2.14
<b>34</b>	4.13	3.28	2.88	2.65	2.49	2.38	2.30	2.23	2.17	2.12
<b>36</b>	4.11	3.26	2.86	2.63	2.48	2.36	2.28	2.21	2.15	2.10
<b>38</b>	4.10	3.25	2.85	2.62	2.46	2.35	2.26	2.19	2.14	2.09
<b>40</b>	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.07
<b>42</b>	4.07	3.22	2.83	2.59	2.44	2.32	2.24	2.17	2.11	2.06
<b>44</b>	4.06	3.21	2.82	2.58	2.43	2.31	2.23	2.16	2.10	2.05
<b>46</b>	4.05	3.20	2.81	2.57	2.42	2.30	2.22	2.14	2.09	2.04
<b>48</b>	4.04	3.19	2.80	2.56	2.41	2.30	2.21	2.14	2.08	2.03
<b>50</b>	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07	2.02
<b>60</b>	4.00	3.15	2.76	2.52	2.37	2.25	2.17	2.10	2.04	1.99
<b>70</b>	3.98	3.13	2.74	2.50	2.35	2.23	2.14	2.07	2.01	1.97
<b>80</b>	3.96	3.11	2.72	2.48	2.33	2.21	2.12	2.05	1.99	1.95
<b>100</b>	3.94	3.09	2.70	2.46	2.30	2.19	2.10	2.03	1.97	1.92
<b>200</b>	3.89	3.04	2.65	2.41	2.26	2.14	2.05	1.98	1.92	1.87
<b>400</b>	3.86	3.02	2.62	2.39	2.23	2.12	2.03	1.96	1.90	1.85
<b>1,000</b>	3.85	3.00	2.61	2.38	2.22	2.10	2.02	1.95	1.89	1.84
<b>∞</b>	3.84	2.99	2.60	2.37	2.21	2.09	2.01	1.94	1.88	1.83

# ICA 17 Source Table

Source	SS	df	MS	F
<b>Between</b>	100	3		
→ Factor A (personality)	10	1	10	2 ✓
→ Factor B (caffeine)	50	1	50	10 ✓
→ Interaction (AxB)	40	1	40	8 ✓
<b>Within</b>	400	80	5	
<b>Total</b>	500	83		

Our  $F_{crit}$  for all three tests is **3.96**

Source	SS
Between	100
→ Factor A (personality)	10
→ Factor B (caffeine)	50
→ Interaction (AxB)	40
Within	400
Total	500

# Effect Size

## MAIN EFFECT

Factor A

$$\eta^2_p = \frac{SS_A}{SS_A + SS_{within}}$$

$$\eta^2_p = \frac{10}{10 + 400}$$

$$= .02$$

## MAIN EFFECT

Factor B

$$\eta^2_p = \frac{SS_B}{SS_A + SS_{within}}$$

$$\eta^2_p = \frac{50}{50 + 400}$$

$$= .11$$

## INTERACTION

AxB

$$\eta^2_p = \frac{SS_{AxB}}{SS_A + SS_{within}}$$

$$\eta^2_p = \frac{40}{40 + 400}$$

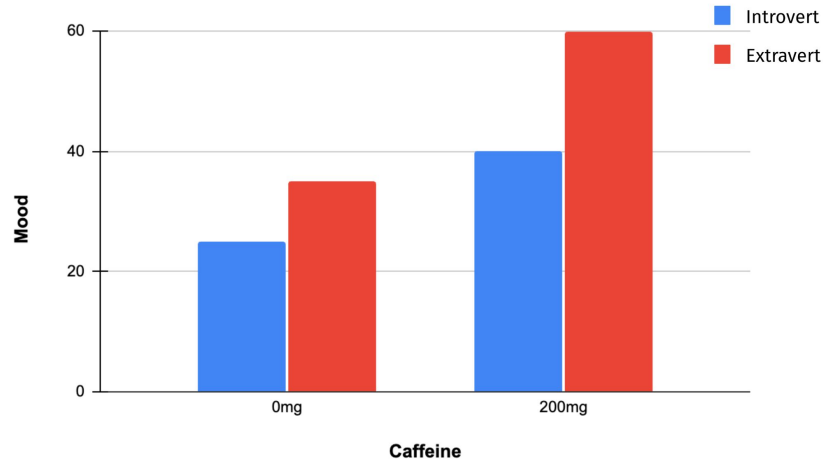
$$= .09$$

# Interpretation

A **2 × 2** factorial ANOVA was conducted to examine the effects of *personality* and *caffeine* on *mood*.

There was a significant **main effect of personality**,  $F(1, 80) = 2.00, p < .05$  and a significant **main effect of caffeine**,  $F(1, 80) = 10.00, p < .05$ . There was also a significant **interaction** between personality and mood,  $F(1, 80) = 8.00, p < .05$ .

# Interpretation, plain English



Overall, participants reported better moods when they consumed caffeine, and extraverts tended to have higher moods than introverts. However, caffeine **boosted mood more strongly** for extraverts than for introverts.





# **Exam 2 Information & Wrap Up**

# SOME EXAM 2 KEY TOPICS

**Make sure you know these concepts well!**

Independent-samples t-test

Paired-samples t-test

One-way ANOVA

2-way (factorial) ANOVA

Calculation of t-statistic &/ F-ratio

Calculation of effect size & 95% CI

**\*\*Interpretation\*\***

Type 1 & Type 2 errors, Power

Between vs within subjects design & pros &  
cons

One-way ANOVA follow-ups

Interaction interpretation

**Note: see learning objectives for each lecture as a “study guide”**

# EXAM 2 INFORMATION & FORMAT

- Exam will cover content on **lectures 9 – 17**
- Exam 2 will occur in class and will last **75 minutes**
- You are allowed **one double-sided hand-written page of notes**
- It will be mostly **short-answer questions**
- You will be given a **formula sheet** and **t-table & F-table**
- You should ***show all your work***, including formulas
- Round to **two decimal places** (e.g., 10.21, 120.43)

**Bring your calculator!!!**

# Announcements

- Shelby is giving this Thursday's lecture!
  - She will give you lots of examples on menopause
- No lab this Friday, I will post the practice exam on Friday, you can work on it on your own, and the following Tuesday's lecture is for Q&A
- No homework this week. Focus on treating the Practice Exam as an actual exam