

Homework_02

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```
library(tidyverse)
```

```
## Warning: package 'tidyverse' was built under R version 4.3.2
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
```

```
## v dplyr      1.1.2      v readr      2.1.4
```

```
## v forcats    1.0.0      v stringr    1.5.0
```

```
## v ggplot2     3.4.3      v tibble     3.2.1
```

```
## v lubridate  1.9.2      v tidyr      1.3.0
```

```
## v purrr      1.0.2
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::filter() masks stats::filter()
```

```
## x dplyr::lag()     masks stats::lag()
```

```
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
cdi <- read.csv("https://dcgerard.github.io/stat_415_615/data/cdi.csv")
```

```
head(cdi)
```

```
##   id      county state area      pop percent_18_34 percent_65 physicians  beds
## 1  1 Los_Angeles  CA 4060 8863164      32.1      9.7      23677 27700
## 2  2      Cook    IL  946 5105067      29.2     12.4      15153 21550
## 3  3      Harris  TX 1729 2818199      31.3      7.1       7553 12449
## 4  4 San_Diego    CA 4205 2498016      33.5     10.9       5905  6179
## 5  5      Orange  CA  790 2410556      32.6      9.2       6062  6369
## 6  6      Kings  NY   71 2300664      28.3     12.4       4861  8942
##   crimes high_school bachelors poverty unemployment capita_income total_income
## 1 688936      70.0      22.3    11.6      8.0      20786      184230
## 2 436936      73.4      22.8    11.1      7.2      21729      110928
## 3 253526      74.9      25.4    12.5      5.7      19517       55003
## 4 173821      81.9      25.3     8.1      6.1      19588       48931
## 5 144524      81.2      27.8     5.2      4.8      24400       58818
## 6 680966      63.7      16.6    19.5      9.5      16803       38658
##   region
## 1      W
## 2      NC
## 3      S
## 4      W
## 5      W
## 6      NE
```

County Demographic Information

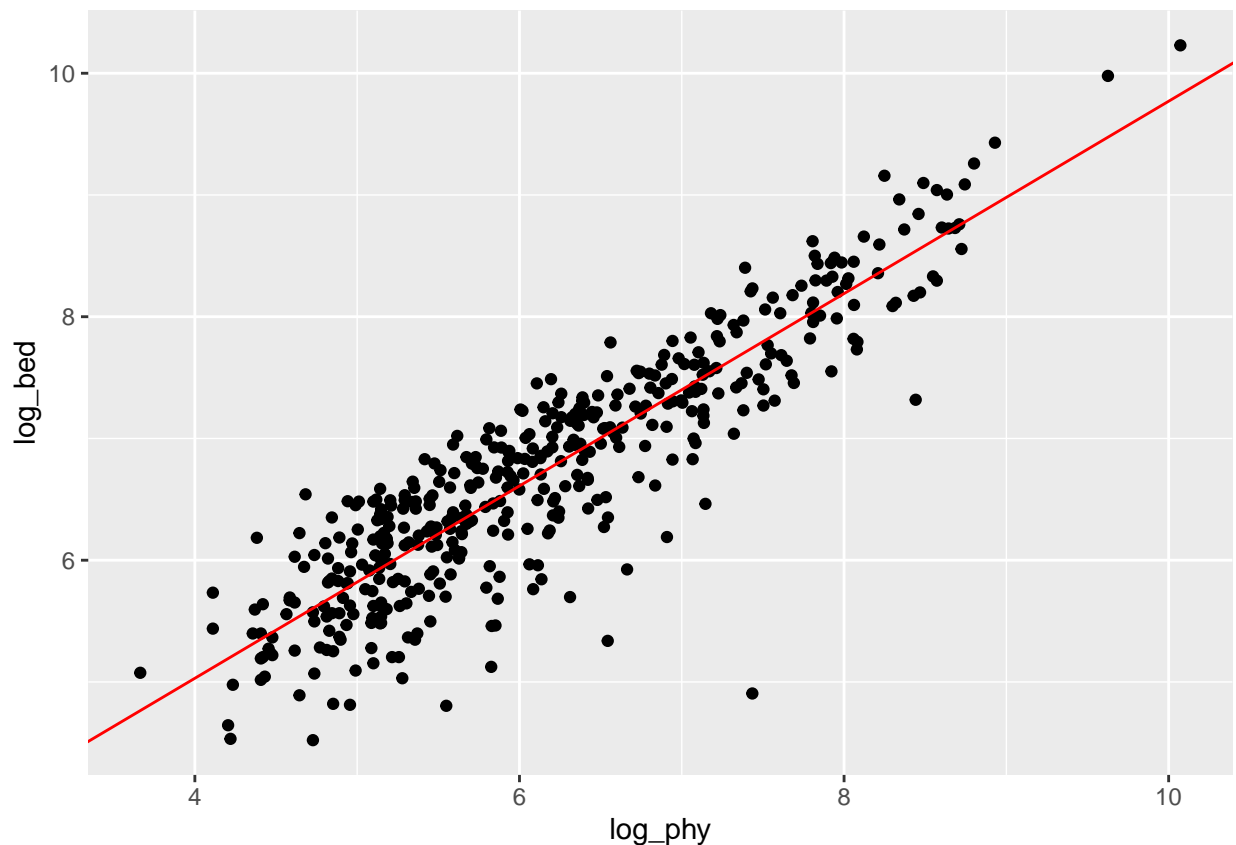
$$\log(y) = 1.87 + 0.79\log(x)$$

1. The given equation is an example of a **Power-law** relationship. In a power-law relationship, the dependent variable(y) is related to the independent variable(x) through the power function, expressed as: $y = y.C^{B1}$ where C is a constant and B1 is the exponent or slope of the line.
- 2.

```
reg_table <- mutate(cdi, log_phy = log(physicians),  
                     log_bed = log(beds)) %>%  
  select(log_phy, log_bed)  
head(reg_table)
```

```
##      log_phy  log_bed  
## 1 10.072259 10.229188  
## 2  9.625954  9.978131  
## 3  8.929700  9.429396  
## 4  8.683555  8.728912  
## 5  8.709795  8.759198  
## 6  8.488999  9.098515
```

```
ggplot(data = reg_table, aes(x = log_phy, y = log_bed)) +  
  geom_point() +  
  geom_abline(slope = 0.79, intercept = 1.87, color = "red")
```



$$3. \log(y) = 1.87 + 0.79\log(x)$$

$$y = 1.87 \cdot x^{0.79}$$

4. For every C number of beds in a hospital, there is $C^{0.79}$ as many physicians, on average.

$$\log(y) = 6.26 + 0.022x$$

5. The given equation is an example of a **Exponential growth/decline** relationship. In a exponential growth/decline relationship, the dependent variable(y) is related to the independent variable(x) through the exponential function, expressed as: $y = y.exp(C*B1)$ where C is a constant and B1 is slope of the line.

6. For every unit higher in beds in the hospital, there is $\exp(0.022)$ times more beds, on average.

Rephrase: For each unit in beds, there is a 2.2% times more bachelors degree holders, on average.

7. **6.26** is the y-intercept of the regression line.

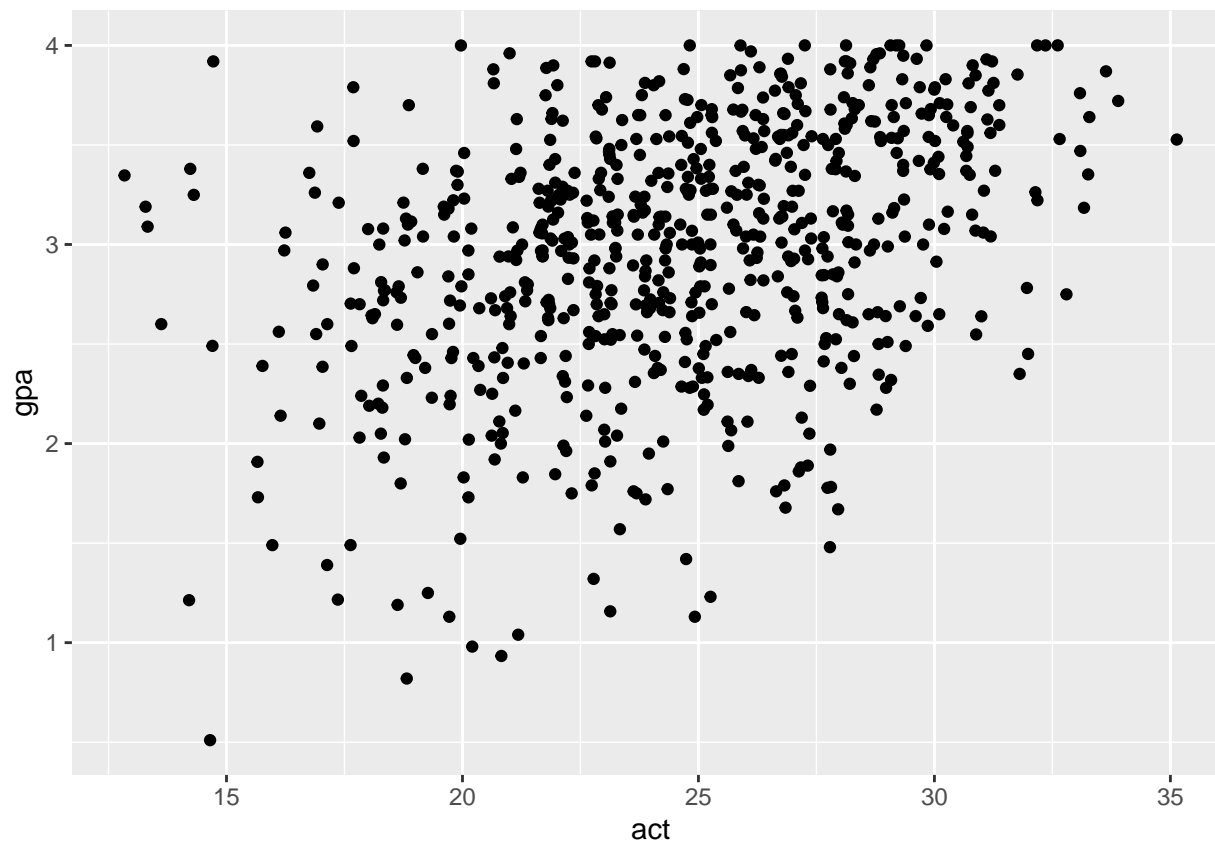
University Admissions Data

```
uad <- read.csv("https://dcgerard.github.io/stat_415_615/data/university.csv")
head(uad)
```

```
##   id  gpa rank act year
## 1  1 0.98  61  20 1996
## 2  2 1.13  84  20 1996
## 3  3 1.25  74  19 1996
## 4  4 1.32  95  23 1996
## 5  5 1.48  77  28 1996
## 6  6 1.57  47  23 1996
```

1.

```
ggplot(uad, aes(x = act, y = gpa)) +
  geom_jitter()
```



From the above plot, there is an association between gpa and act of students. Although the association is a little faint, the graph shows a positive association between the variables.

2. **0.058**: For every unit score in $ACT(x)$, student's GPA is higher by 0.058, on average. **1.56**: This is the GPA score when ACT score is 0.

Miscellaneous

1. No I won't be happy, the economy is recovered and I am expecting to get the same value as my old salary or more. Decreasing my salary by 10% and later increasing it by another 10% will not get the same old value.