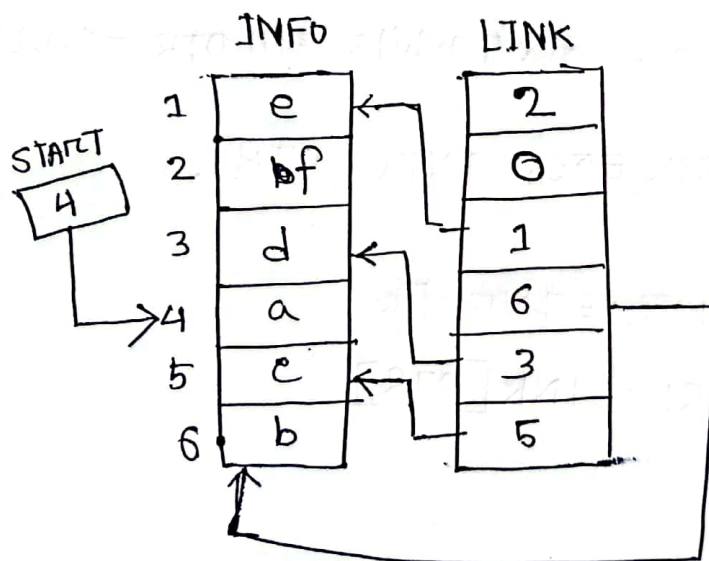
 Linked List: A linked list, or one-way list, is a linear collection of data elements, called nodes, where the linear order is given by means of pointers. That is, each node is divided into two parts: the first part contains the element information of the element and the second part, called the link field, contains the address of the next node in the list.



INFO [4] = a      LINK [4] = 6

INFO [6] = b      LINK [6] = 5

INFO [5] = c      LINK [5] = 3

INFO [3] = d      LINK [3] = 1

INFO [1] = e      LINK [1] = 2

INFO [2] = f      LINK [2] = NULL

## # Traversing a Linked list:→

Algorithm: Let LIST be linked list in memory. This algorithm traverses LIST, applying an operation PROCESS to each element of LIST. The variable PTR points to the node currently being processed.

count (START, INFO, LINK, PTR)

Step-1: Set  $PTR := START$ .

Step-2: Repeat step 3 and 4 while ~~set~~  $PTR \neq NULL$ .

Step-3: Apply PROCESS INFO [PTR].

Step-4: Set  ~~$PTR := INFO$~~   
 $PTR := LINK[PTR]$

Step-5: Exit.

# Print Information at each node of the list.

Algorithm:

PRINT (INFO, LINK, START)

Step-1: Set PTR := START.

Step-2: Repeat step 3 and 4 while PTR  $\neq$  NULL.

Step-3: PRINT: INFO [PTR].

Step-4: Set PTR := LINK [PTR].

Step-5: Exit.

# Finds the number, NUM of elements in a linked list.

Algorithm?

COUNT (START, INFO, LINK, NUM)

Step-1: set NUM := 0

Step-2: set PTR := START

Step-3: Repeat step-4 and 5 while PTR  $\neq$  NULL.

Step-4: set NUM := NUM + 1.

Step-5: set PTR := LINK [PTR]

Step-6: Exit.



# Array: List of elements of the same data type placed in a contiguous memory location.

# Traversing Linear Arrays:-

	0	1	2	3	4
LA	10	11	12	13	14
	LB				UB

Algorithm:- Here LA is linear array with lower bound (LB) and upper bound (UB). This algorithm traverse LA applying an operation PROCESS to each element of LA.

Step-1:- Set  $k := LB$ .

Step-2:- Repeat step-3 and 4 while  $k \leq UB$ .

Step-3:- Apply PROCESS to  $LA[k]$

Step-4:- set  $k := k + 1$ .

Step-5:- Exit.

## # Inserting into a Linear Array:

Algorithm: INSERT (LA, N, K, ITEM), LB)

Here, LA is a linear array with N elements and K is a positive integer such that  $K \leq N$ . This algorithm insert an element ITEM into the K-th position.

step-1: set  $j := N$ . /  $j := LB$

step-2: Repeat step-3 and 4 while  $j \geq K$ .

step-3: set  $LA[j+1] = LA[j]$

step-4: set  $j := j - 1$ .

step-5: set  $LA[K] := ITEM$

step-6: set  $N := N + 1$

step-7: Exit.

## # Deleting from a linear array:-

Algorithm:- DELETE(LA, N, K, ITEM)

Here, LA is linear array with N elements and K is a positive integer such that  $K \leq N$ . This algorithm deletes the K-th elements from LA.

Step-1:- set  $ITEM := LA[K]$ .

Step-2:- Repeat for  $j = K$  to  $N-1$ :

set  $LA[j] := LA[j+1]$

Step-3:- set  $N := N-1$

Step-4:- Exit.

	0	1	2	3	4	5	6	X
LA =	10	20	35	40	45	50	60	

$K=4$  ITEM

$LA[4] = 45$

for  $K=4$  to 6

$j=4$   $LA[j] = LA[j+1]$

~~45~~

## # Bubble sort:-

Algorithm: BUBBLE(DATA, N)

Here, DATA is an array with N elements. This algorithm sorts the elements in DATA.

Step-1: Repeat step 2 and 3 for  $K=1$  to  $N-1$ .

Step-2: set  $PTR:=1$ .

Step-3: Repeat while  $PTR \leq N-K$

Step-3: a) If  $DATA[PTR] > DATA[PTR+1]$

•  $DATA[PTR]$  and  $DATA[PTR+1]$   
interchange

b) set  $PTR:=PTR+1$ .

Step-4: Exit.



## # Linear Search:-

Algorithm:- **LINEAR**(DATA, N, ITEM, LOC)

Here, DATA is a linear array with N elements and ITEM is a given item of information. This algorithm finds the location LOC of ITEM in DATA or set  $LOC := 0$  if the search is unsuccessful.

Step-1:- Set  $DATA[N+1] := ITEM$ .

Step-2:- Set  $LOC := 1$ .

Step-3:- Repeat while  $DATA[LOC] \neq ITEM$ .

Set  $LOC := LOC + 1$ .

Step-4:- If  $LOC := N+1$   
then: Set  $LOC := 0$

Step-5:- Exit.

## # Binary Search:

Algorithm:- BINARY(DATA, LB, UB, ITEM, LOC)

Here, DATA is sorted array with lower bound (LB) and upper bound (UB), and ITEM is a given item of information. The variable START, END and MID denote, respectively, the starting, ending and middle location of a segment of elements of DATA.

Step-1:- Set  $START := LB$ ,  $END := UB$  and  $MID = INT((START + END) / 2)$

Step-2:- Repeat step -3 and 4 while  $START \leq END$  and  $DATA[MID] \neq ITEM$ .

Step-3:- IF  $ITEM < DATA[MID]$

Set  $END := MID - 1$ .

Else :

Set  $START := MID + 1$ .

Step-4:- Set  $MID := INT((START + END) / 2)$ .

Step-5:- IF  $DATA[MID] = ITEM$ . then

Set  $LOC := MID$ .

Else, set  $LOC := NULL$ .

Step-6:- Exit.

## # First Pattern Matching Algorithm:

Here, P and T are strings with lengths R and S, respectively and are sorted as arrays with one character per element. This algorithm find the INDEX of P in T.

$T = \text{abcde}$      $\text{Length}(T) = S$   
 $P = \text{cd}$      $\text{Length}(P) = R$

$MAX = S - R + 1$   
 $= 5 - 2 + 1$   
 $= 4$

Step-1: set  $K := 1$  and  $MAX := S - R + 1$ .

Step-2: Repeat step-3 to 5 while  $K \leq MAX$ .

Step-3: Repeat for  $L = 1$  to  $R$ : [Test each characters of P]  
 if  $P[L] \neq T[K+L-1]$  then go to step-5

Step-4: [Success] set  $INDEX := K$  and Exit.

Step-5: set  $K := K + 1$ .

Step-6: [Failure] Set  $INDEX := 0$

Step-7: Exit.

— 0 —

$K = 1$      $MAX = 4$

$K \leq MAX \checkmark$

$P[1] \neq T[1]$      $P[2] =$

$INDEX = 3$

$\begin{array}{l} 1 - a \\ 2 - b \\ 3 - c \\ 4 - d \end{array}$

## # Word / String Processing:

i) Insertion: Inserting a string in the middle of the text.

INSERT (text, position, string)

EX  $\rightarrow$  INSERT ("ABCDEFGH", 3, "XYZ")  
 $=$  "AB" || "XYZ" || "CDEFGH"  
 $=$  "ABXYZCDEFGH"

INSERT (T, K, S) = Substring (T, 1, K-1) || S || Substring  
 (T, K, Length(T) - K + 1)

This is, the initial substring of T before the position K, which has length K-1, is concatenated with the string S, and the result is concatenated with the remaining part of T, which begins in position K and has length = Length(T) - K + 1.



ii) Deletion: Deleting a string from the text.

DELETE (text, position, length)

EX →

DELETE ("ABCDEFGHI", 4, 2)  
= "ABC" || "FGHI"

DELETE (T, K, L) = Substring (T, 1, K-1) ||  
Substring (T, K+L, Length(T) - (K+L) + 1)

That is, the initial substring of T before position K is concatenated with the terminal substring of T beginning in position K+L. The length of the initial substring is K-1 and the length of the terminal substring is:  
(Length(T) - (K+L) + 1).

Algorithm:-

Step-1: Set K := INDEX(T, P)

Step-2: Repeat while K ≠ 0

a) [delete P from T]

Set T := DELETE (T, INDEX(T, P), LENGTH(P))

b) [update index].

Set K := INDEX(T, P).

Step-3: Write T

Step-4: Exit.

iii) Replacement: Replacing one string in the text by another.

$\text{REPLACE}(\text{text}, \text{pattern1}, \text{pattern2})$

EX  $\rightarrow \text{REPLACE}(\text{"ABCDEFGH"}, \text{"CD"}, \text{"WXYZ"})$

$= \text{"AB"} || \text{"WXYZ"} || \text{"EFGH"}$

$= \text{"ABWXYZ EFGH"}$

$\text{REPLACE}(T, P_1, P_2)$

$K := \text{INDEX}(T, P_1)$

$T := \text{DELETE}(T, K, \text{Length}(P_1))$

$\text{INSERT}(T, K, P_2)$

The first two steps delete  $P_1$  from  $T$ , and the third step insert  $P_2$  in the position  $K$  from which  $P_1$  was deleted.

step-1: set  $K := \text{INDEX}(T, P_1)$

step-2: Repeat while  $K \neq 0$

a) set  $T := \text{REPLACE}(T, P_1, P_2)$

b) set  $K := \text{INDEX}(T, P_1)$

step-3: write:  $T$

step-4: Exit.

## String Operations:-

i) Length:- The number of characters in a string is called its length. we will write,

$\text{LENGTH}(\text{string})$

$\text{LENGTH}(\text{'COMPUTER'}) = 8$

ii) Substring:- Accessing a substring from a given string requires three pieces of information i) The string itself, ii) the position of the first character of the substring in the given string and iii) the length of the substring. we can write,

$\text{SUBSTRING}(\text{string}, \text{initial}, \text{length})$

EX  $\rightarrow$  string = "ABCDEFGH"

$\text{SUBSTRING}(\text{string}, 4, 3)$   
= "DEF"

iii) Concatenation:- Let,  $S_1$  and  $S_2$  be strings. The concatenation of  $S_1$  and  $S_2$ , which we denote by  $S_1 || S_2$ , is the string consisting of characters  $S_1$  followed by the characters of  $S_2$ .

EX  $\rightarrow$   $S_1 = \text{"MARK"}$      $S_2 = \text{"TWIN"}$

$\therefore S_1 || S_2 = \text{"MARKTWIN"}$



IV Indexing:- Indexing also called pattern matching, refers to finding the position where a string pattern  $P$  first appears in a given text  $T$ . We call this operation INDEX and write,

$\text{INDEX}(\text{text}, \text{pattern})$

EX  $\rightarrow \text{INDEX}(\text{"calcutta"}, \text{"cutta"}) = 4$

# Time complexity  $\rightarrow$  Amount of time taken up by an algorithm or code as function of input size.

Linear search Analysis

Worst Case  $\rightarrow$  The worst

1	-8	2	3	5
---	----	---	---	---

case occurs when ITEM is the last element in the array DATA or is not there at all. In either situation, we have

$$C(n) = n$$

Accordingly,  $C(n) = n$  is the worst-case-complexity of the Linear search algorithm.

Average Case  $\rightarrow$

Here we assume that ITEM does appear in DATA, and that is equally likely to occur at any position in the



array. Accordingly, the number of comparisons  $C$  can be any of the numbers  $1, 2, 3, \dots, n$  and each number occurs with possibility  $p = \frac{1}{n}$

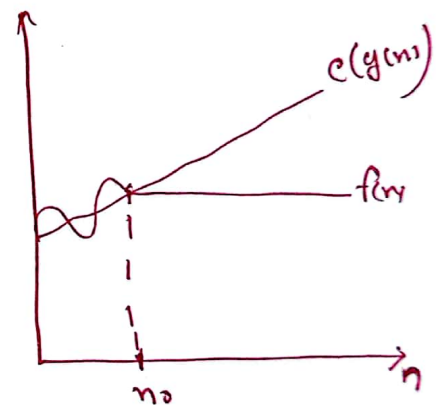
$$\therefore C(n) = \frac{n+1}{2}$$

This agrees with our intuitive feeling that the average number of comparisons need to find the location of ITEM is approximately equal to half the number of elements in the DATA List.

### # Big O Notation:-

$O(g(n)) = f(n)$ : There exist positive constant  $c$  and  $n_0$  such that

$$0 \leq f(n) \leq c g(n) \text{ for all } n \geq n_0$$



$O$ -notation gives an upper bound for a function to within a constant factor. we write,  $f(n) = O(g(n))$  if there are positive constant  $n_0$  and  $c$  such that to the right of  $n_0$  the value of  $f(n)$  always lies on or below.